## Supplement of

# An efficient approach for inverting rock exhumation from thermochronologic age-elevation relationship 

Yuntao Tian et al.<br>Correspondence to: Yuntao Tian (tianyuntao@mail.sysu.edu.cn)

The copyright of individual parts of the supplement might differ from the article licence.


Figure S1. The Pecube model for synthesizing surface and borehole AFT and AHe age data. The model calculates evolving thermal field of a 30-km-thick crustal block using a combination of geothermal, rock exhumation (grey arrows), and a steady-state topographic parameters. Spheres mark the samples from which synthetic thermochronologic ages were calculated.


Figure S2. The best-fit model for the synthetic dataset I (a), II (b), III (c) and IV (d) using surface samples. First row: Comparison between the observed (in black) and predicted (in blue) AER. Second row: plots of observed and modeled ages. Third row: Histories of exhumation and geothermal gradients. The black line marks the "true" exhumation history used for simulating the age dataset, whereas the blue thick and thin lines are the mean and one standard deviation of the inverted exhumation. The red dash and solid lines are the history of the geothermal gradients, predicted by the a priori and a posterior models, respectively, whereas the cyan line and polygon denotes the modern geothermal gradient. Fourth and bottom row: Plots of the resolution and correlation matrix.

Tables S1. Synthetic age dataset generated by Pecube models and used in the Figures 9 and S2.

| Elevation | Age (Ma), <br> model-a | Age (Ma), <br> model-b | Age (Ma), <br> model-c | Age (Ma), <br> model-d | Age type |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 2000.00 | 9.38 | 8.27 | 7.90 | 15.94 | AFT |
| 1707.11 | 9.28 | 8.14 | 7.57 | 14.94 | AFT |
| 1000.00 | 8.82 | 7.68 | 6.18 | 10.90 | AFT |
| 292.89 | 8.25 | 7.14 | 4.76 | 6.89 | AFT |
| 0.00 | 7.91 | 6.79 | 4.09 | 5.16 | AFT |
| -500.00 | 7.28 | 6.15 | 3.34 | 3.78 | AFT |
| -1000.00 | 6.64 | 5.48 | 2.69 | 2.97 | AFT |
| -1500.00 | 5.98 | 4.82 | 2.09 | 2.30 | AFT |
| -2000.00 | 5.28 | 4.12 | 1.54 | 1.69 | AFT |
| 2000.00 | 7.22 | 6.21 | 3.23 | 3.43 | AHe |
| 1707.11 | 7.14 | 6.13 | 3.13 | 3.32 | AHe |
| 1000.00 | 6.82 | 5.78 | 2.73 | 2.87 | AHe |
| 292.89 | 6.44 | 5.34 | 2.28 | 2.38 | AHe |
| 0.00 | 6.20 | 5.03 | 2.02 | 2.09 | AHe |
| -500.00 | 5.57 | 4.11 | 1.49 | 1.56 | AHe |
| -1000.00 | 4.62 | 2.93 | 0.99 | 1.04 | AHe |
| -1500.00 | 3.19 | 1.76 | 0.53 | 0.57 | AHe |
| -2000.00 | 1.59 | 0.83 | 0.21 | 0.23 | AHe |

