



Stabilising large grains in self-forming steep channels

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Abstract. It is understood that the interaction between sediment supply and discharge drives first-order behaviour of alluvial deposits. The influence of the grain size distribution over the mobility and resultant evolution is, however, unclear. Four experiments were conducted in a scaled physical model for two grain size distributions, analogous to a one-dimensional self-formed alluvial fan. We demonstrate the unsuitability of the median grain size as a predictor of deposit behaviour at flows when the material is not equally mobile. The results instead suggest, during conditions of unequal mobility, that the largest grains control the transport efficiency of the overall sediment mixture, and thus also the morphodynamics of the deposit and its tendency to store or evacuate material. Deposits appear to show a dependence upon the rate of material supply more strongly when the likelihood of its motion is less equally distributed (i.e. under partial transport conditions). If the coarse fraction (e.g. greater than 84th percentile) is instead mobile due to increased discharge or because of their relative size, transport rates will increase and the behaviour of the mixtures converge to a common state, with morphology influenced by the material's mobility.

1 Introduction

Gravel bed rivers adjust their boundaries from the grain to the reach scale in response to the supplied sediment and water discharges (Leopold and Maddock, 1953; Lane, 1955; Howard and Kerby, 1983; Madej and Ozaki, 1996; Eaton and Church, 2004; Hassan et al., 2007). The feedbacks and interactions between antecedent flow and sediment discharge control river channel form (Fukuoka, 1989) and thereby influence channel response, e.g. as a response to flow increases (Masteller and Finnegan, 2017). Natural channels are likely to experience a distribution of flow rates and, therefore, corresponding modes of transport (e.g. Ashworth and Ferguson, 1989; Warburton, 1992). Central to the behaviour of gravel bed rivers is this response to their environment as the flow does not regularly or greatly exceed the threshold of sediment mobility (e.g. Church, 2006). In a channel the aggradation or degradation of material will lead to changes in its elevation, representing a balance between the amount of energy and material provided to it. Lane (1955) proposed that grade represents this balance as

$$\frac{Q_b}{QS} \propto \frac{1}{D}, \quad (1)$$

wherein the left-hand side of the proportionality represents the sediment transport efficiency, given by the ratio between sediment supply (Q_b) and the product of discharge (Q) and slope (S). The right-hand side is the reciprocal of the sediment flux calibre (D). Church (2006) recast this relation in a dimensionally balanced version, which can be written as follows:

$$\frac{Q_b}{QS} \propto \frac{d}{D}, \quad (2)$$

where d is the flow depth. In Church's version, D is specifically defined to be the median bed surface size, based on the understanding of the hiding and/or exposure processes controlling the entrainment of sediment from a mixture.

Accordingly, mixtures of the same median grain size, under the same water and sediment discharges, should form to the same slope because of their equal transport efficiency. Transport efficiency (η) is defined in the same manner as by Bagnold (1966), in that it relates the work rate of the flow

to the stream power available and describes the efficiency of the system in converting stream power into work (i.e. sediment transport) and is therefore higher in more efficient systems. That is, systems with higher η values will organise to lower slopes, because they are more capable of transporting the supplied material, as described by its discharge. Here, it is reformulated by neglecting the mass flux term from its original form, instead replicating the dimensionless, volumetric consideration used by Eaton and Church (2011):

$$\eta = \frac{Q_b}{QS}, \quad (3)$$

whereby it functions as a relationship between the system's mass and energy inputs, outputs, and processes.

The validity of using a single characteristic grain size as a descriptor of a whole system's state is, however, fundamentally flawed. We know that surficial adjustment, bedforms, and macroforms modulate bed material sediment transport rate, acting to dissipate energy and provide stability to the overall channel (Cherkauer, 1973; Montgomery and Buffington, 1997; Venditti et al., 2017). For example, it has been thought that grains may stabilise through rotation (Masteller and Finnegan, 2017), their organisation into cells (Church et al., 1998; Monsalve and Yager, 2017), and the formation of alternate bars and patches (Lisle et al., 1991; Dietrich et al., 2006; Nelson et al., 2010). One of the most well studied of these adjustment phenomena is the coarsening of the bed surface due to the preferential removal of fines or their kinetic sieving into the subsurface, until an armour layer develops that approximately equalises the threshold entrainment stress of the bed (Parker and Klingeman, 1982; Parker et al., 1982b; Andrews, 1983). Armour may develop in both sediment-starved reaches as static armour (Sutherland, 1987; Dietrich et al., 1989; Parker and Sutherland, 1990; Kondolf, 1997; Vericat et al., 2006; Nelson et al., 2009) or where sediment supply is present as a mobile armour layer (Parker and Klingeman, 1982; Andrews and Parker, 1987; Parker, 1990). It is the formation of an armour layer that prevents continued transport of the material and stabilises the channel against further deformative work. In addition, MacKenzie and Eaton (2017) demonstrated that it is the largest grains found in the bed material that control channel stability during degradation because of their role in protecting the underlying fine grains. Their work concludes that bed stability cannot be fundamentally linked to the median bed surface grain size, as in sediment transport models developed by Parker (1990) and Wilcock and Crowe (2003).

In contrast to this, our knowledge of the processes stabilising aggrading systems is substantially lacking in direct study; the omission of their explicit focus in the *Treatise of Geomorphology* is noticeable, in comparison to the myriad of studies based on degrading channels. Systems undergoing aggradation may range in degrees of confinement (i.e. from valley bottoms to alluvial fans), but they are characterised by either a competence or capacity-driven accumulation of sedi-

ment relative to their current energy flux. Aggrading systems are often studied, but they are often treated at a greater scale (i.e. channel planform) in the field (e.g. Gilbert, 1917; Harvey, 1991; Benda and Dunne, 1997) or neglected in non-fan experiments. For example, Madej (1982) attributed increases in sediment transport rates to channel geometry changes induced by aggradation in the channel, rather than the manifestation of system variables such as slope (as would be expected with Eq. 1). As a singular process, avulsion acts as a mechanism for channel “stabilisation” in aggrading systems, where sediment transport capacity is maintained through the creation or re-occupation of an alternate channel position (Ashmore, 1982; Field, 2001). Studies also focus upon the influence of supplied material, of which the calibre is important for the resulting trajectory of changes to hydraulics and morphology. An influx of fine sediment will increase sediment transport through increased exposure effects on coarser material (Wilcock et al., 2001; Wilcock and Crowe, 2003; Curran and Wilcock, 2005). On the other hand, coarse material will accumulate either through supply of un-entrainable material (Harvey, 2001) or the role of coarse grains as stabilising loci (Lisle et al., 1991). We could argue, therefore, that there exists a precedent for the role of large grains in controlling the behaviour of aggrading channels, derived from the deposition of those grains supplied to the channel (e.g. Moss, 1963; Dunkerley, 1990).

The applicability of using Eq. (2) to predict the changes in system slope is thus called into question when we consider the role of large grains in the stability of aggrading or degrading systems. We hypothesise that the presence of the large grains will result in different sediment mixture mobilities for aggrading channels, thus different channel morphodynamics and depositional slope, as in MacKenzie and Eaton (2017). In addition, we expect that this effect will not be maintained under discharge increases, as the D_{84} is suggested to strongly influence the thresholds of mobility within a mixture (MacKenzie et al., 2018). The goal of this paper, therefore, is to test whether or not large grains influence channel stability in aggrading systems, wherein many of the processes thought to produce stabilisation in degrading systems are suppressed. To that end, we present the results for two sets of four experiments paired by median grain size but differentiated by the shape of their distributions, for which Eqs. (1) and (2) would predict similar behaviour. In most studies, slope acts as a response to an existing deposit, e.g. degradation into a bed surface (Parker et al., 1982a). Here, sediment may freely aggrade or degrade and thus slope acts instead as an emergent indicator of the system state, thus allowing its form to fully represent the suite of processes acting upon it, a methodology reserved mostly for fan studies (e.g. Schumm et al., 1987; Clarke et al., 2010). The results described here show that the grain size distribution used affects the resulting behaviour of the deposit and its slope, and the differences between paired experiments are controlled by the experimental boundary conditions.

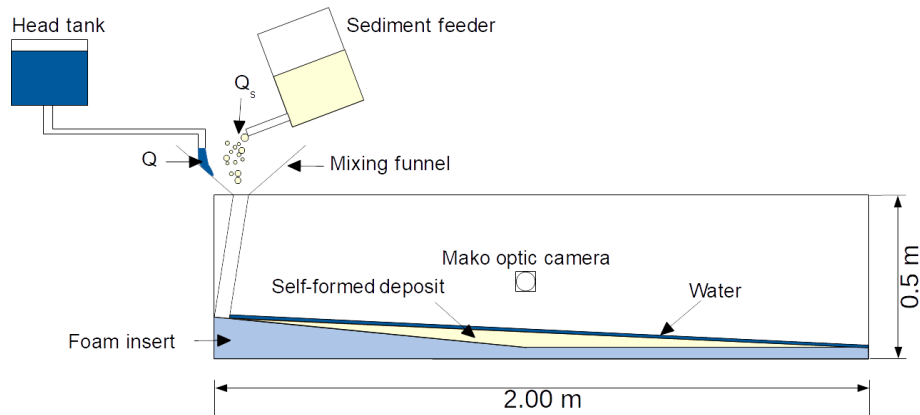


Figure 1. Simplified diagram of the experimental setup for the steep channel flume.

2 Methods

Eight experiments were run in the recently constructed steep mountain channel flume at the University of British Columbia. The flume is acrylic walled, 2 m long by 0.128 m, wide with a foam insert creating a transition from a steep (slope = 0.1 m m^{-1}) upper and flat (slope = 0 m m^{-1}) lower section (Fig. 1), upon which a fan deposit can develop. These deposits that form within the flume are analogous to a one-dimensional fan or to the channel bed of a steep river confined by bedrock walls. Design and methodological cues were taken from previous experiments concerning self-formed deposition (Guerit et al., 2014) and steep channel stability (Lisle et al., 1991).

During the runs reported here, feed and flow were held constant for the length of each experiment. These were conducted under one of four conditions: 100L, 100H, 200L, or 200H, where the number refers to the flow rate (in mL s^{-1}) and the letter to the feed rate (L for 1 g s^{-1} , H for 2 g s^{-1}). The experiments also have a relative sediment concentration compared to the 100L experiment, where a value of 1 represents both factors increasing (i.e. 100L and 200H), 0.5 is a halving of feed relative to flow (i.e. 200L), and 2 is a halving of flow relative to feed (i.e. 100H). This range of values allows us to consider five changes in relative sediment concentration mediated by changes to discharge or sediment feed rate. These are (1) no change in concentration but changes in the total flux magnitude (100L vs. 200H), (2) doubling concentration through increasing sediment feed (100L vs. 100H), (3) doubling concentration through decreasing discharge (200H vs. 100H), (4) halving concentration through increasing discharge (100L vs. 200L), and (5) halving concentration through sediment feed (200H vs. 200L). As in MacKenzie and Eaton (2017), sediment is scaled from gravel-bedded streams found in Alberta, Canada, and truncated at 0.25 mm at the lower end to remove unscalable laminar sub-layer effects for sediment finer than this size limit (Peakall et al., 1996).

These eight experiments primarily serve to distinguish between the behaviour of two grain size distributions across a range of run conditions. The two grain size distributions (GSDs) share nearly the same D_{50} ($\text{GSD}_{\text{broad}} = 2.03 \text{ mm}$, $\text{GSD}_{\text{narrow}} = 2.02 \text{ mm}$). The first grain size distribution ($\text{GSD}_{\text{broad}}$) comprises a log-normal distribution from 0.25 to 8 mm (Fig. 2). The second distribution ($\text{GSD}_{\text{narrow}}$) is only comprised of two size classes: 1.4 to 2.0 mm and 2.0 to 2.8 mm (Fig. 2). As a result, $\text{GSD}_{\text{broad}}$ has a substantially higher D_{84} and standard deviation (σ), as would be expected from its substantially coarser and finer tails.

At the beginning of the experiment, roughness elements were placed on the bed to ensure that the flow remained sub-critical during the initial deposit-building stages. Once the sediment feed and water supply were turned on, bed material deposited around the initial roughness elements, burying them and creating a freely adjustable self-formed deposit with a configuration dictated by the grain size distribution of the sediment supply. The data presented here are collected after the sediment has begun to exit the flume. That is, sediment has deposited along the length of the flume, sediment transport out of the flume has begun, and the sediment trap is collecting this output (see Fig. 3). By which time the channel has a self-adjusted roughness, and the influence of the roughness elements themselves is limited. Data collection ended when the supply of sediment was exhausted; thus, run time is proportional to the feed rate.

The main source of data used in this study was collected using a side-looking camera to map the evolution of the channel's long profile. A Mako optic camera was positioned perpendicular to flume orientation, and it took photographs at 60 s intervals. The camera itself contains a routine to flatten these images and correct for radial lens distortion, resulting in a nearly perfect orthometric image. An image calibration routine translated pixel values to real-space coordinates, from which a linear regression was fitted to estimate the bulk sediment deposit gradient from the channel profile. Additionally, at 30 s intervals, oblique images of the bed were cap-

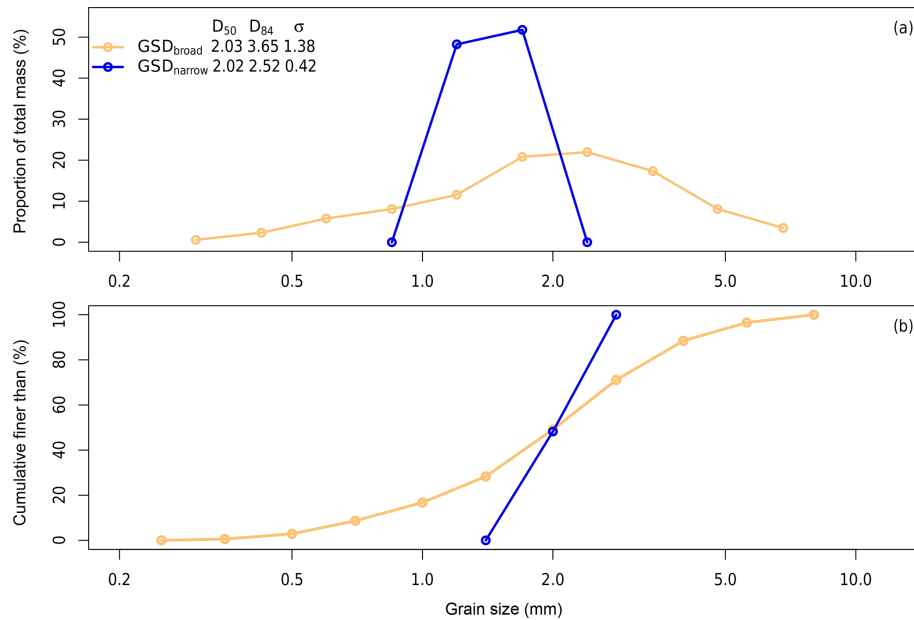


Figure 2. Grain size distributions for half-phi classes (a) individually and (b) cumulatively. Grain size metrics are shown in mm.

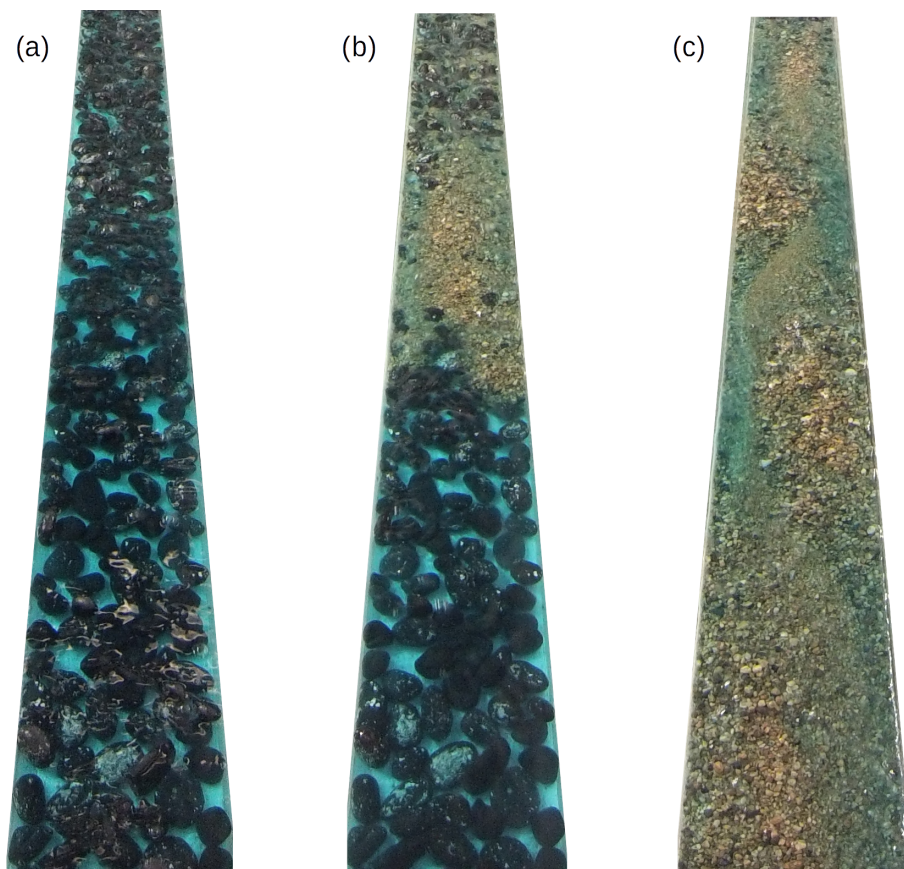


Figure 3. Example images of the black roughness elements used to force subcritical flow, and their submergence taken during (a) beginning of experiment with full emergence, (b) partial submergence and (c) onset of transport, almost complete burial and submergence, from experiment 200H using GSD_{broad}.

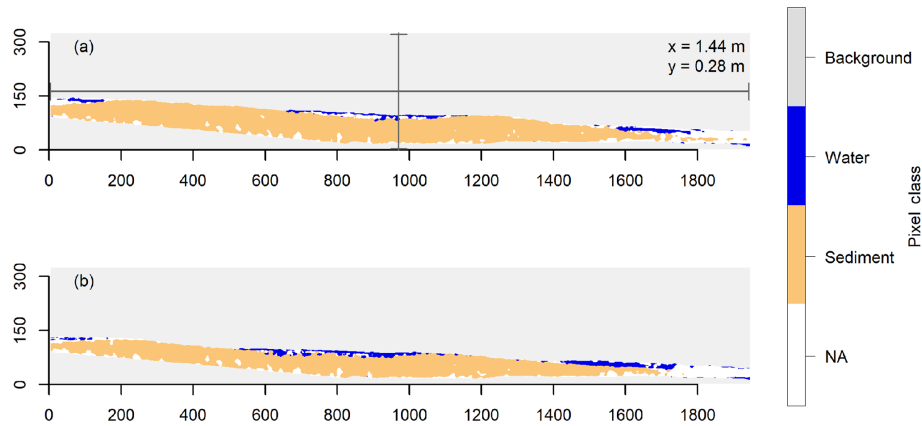


Figure 4. Output after image classification at the onset of output for experiment 100L using (a) $\text{GSD}_{\text{broad}}$ ($T = 326$ min) and (b) $\text{GSD}_{\text{narrow}}$ ($T = 149$ min). Axes are pixel values of the raster, and real distances are provided for scale.

tured by a GoPro oriented upstream. The images were compiled into videos and submitted with this paper to record the bed state evolution (see Video supplement). Note that in the online videos the name GSD_1 refers to $\text{GSD}_{\text{broad}}$, and the name GSD_2 refers to $\text{GSD}_{\text{narrow}}$.

Sediment output data were also recorded through the use of a sediment trap emptied at 15 min intervals. The material was captured, dried, and then weighed, giving us mean transport rates for the preceding period and allowing us to calculate relative sediment storage efficiency as the difference between output and input. That is, a relative storage efficiency of 100 % means that all sediment that is input is stored during a time step (Table 3). Additionally, the mean transport rate is the value used in Eq. (3) in order to calculate η values reported later.

2.1 Slope derivation

In order to derive a water surface slope from the profile images, a simple supervised image classification process was applied to each frame to automate the process. First, a random forest model (“randomForest”) was used to assign one of seven sub-classes to RGB pixel values built from a smoothed training image (Liaw and Wiener, 2002). Random forest models utilise decision trees, which minimise some factor, that are built on different, random samples of the training observations and then average the results of each of these decision trees to make predictions from that dataset (Breiman, 2001). Averaging the results of the myriad regressions built in the model thus improves its predictive strength, and random forest models have been employed during supervised classification of remotely sensed images (see Belgiu and Drăguț, 2016). The sub-classes are sediment, clear water, water with sediment behind it (pool), water surface, background, background with shadow, and the roughness elements. These sub-classes were then grouped into four umbrella classes as sediment, water, background, and roughness

elements, with the latter treated as “NA” values and then smoothed using a 7×7 mode pixel filter to reduce noise (Fig. 4). The training image was chosen such that each of these sub-classes was present and then a model built between the red, green, and blue pixel values of each class was applied to every other image in the dataset. The slope values are the water surface slopes defined as the boundary between background class pixels and the highest of either water or sediment class pixels, until the downstream-most extent of sediment. As sediment may infill between the roughness elements, but not contiguously deposit up to that point, a manual mask was applied to the height of the roughness elements to prevent the erroneous reporting of slope values. Example slope profiles show the typical calculation of the regression at the beginning, middle, and end of runs (Fig. 5).

3 Results

There is a substantial difference between the distribution of slopes for $\text{GSD}_{\text{broad}}$ and $\text{GSD}_{\text{narrow}}$ under 100L conditions; $\text{GSD}_{\text{broad}}$ organised to a mean 42.7 % higher than $\text{GSD}_{\text{narrow}}$ (Fig. 6). Similarly, for twice the relative sediment concentration (i.e. 100H), a clear separation exists between the distributions of slopes formed by $\text{GSD}_{\text{broad}}$ and $\text{GSD}_{\text{narrow}}$, albeit with a lower difference between the two; the mean slope of $\text{GSD}_{\text{broad}}$ is 22.1 % higher. In contrast, at higher discharges but the same relative sediment concentration (200H) the slopes for both sediment feed rates are distributed about a lower mean ($\text{GSD}_{\text{broad}}$: 0.0492 m m^{-1} , $\text{GSD}_{\text{narrow}}$: 0.0452 m m^{-1}), and substantial overlap occurs between the lower bound of $\text{GSD}_{\text{broad}}$ and the upper bound of $\text{GSD}_{\text{narrow}}$. The mean slope value decreases for both grain mixtures at lower feed rates and higher discharge (200L), although it decreases more sharply for $\text{GSD}_{\text{broad}}$ (0.0497 m m^{-1}) than $\text{GSD}_{\text{narrow}}$ (0.0428 m m^{-1}), and it occupies a similar distribution as that of 200H. Mean slopes are given in Table 1, and

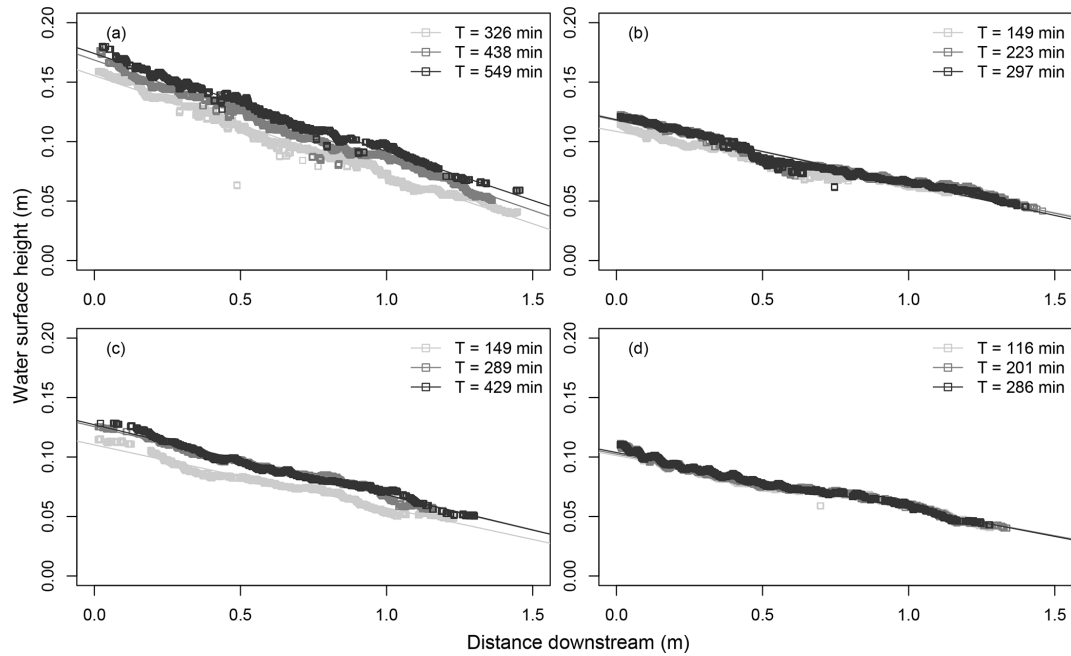


Figure 5. Example water surface profiles, and regressions used to derive slope, for experiments (a) $\text{GSD}_{\text{broad}} 100\text{L}$, (b) $\text{GSD}_{\text{broad}} 200\text{H}$, (c) $\text{GSD}_{\text{narrow}} 100\text{L}$, and (d) $\text{GSD}_{\text{narrow}} 200\text{H}$. Times given in legend correlate to the onset of output, approximately halfway through the experiment, and the end of the experiment.

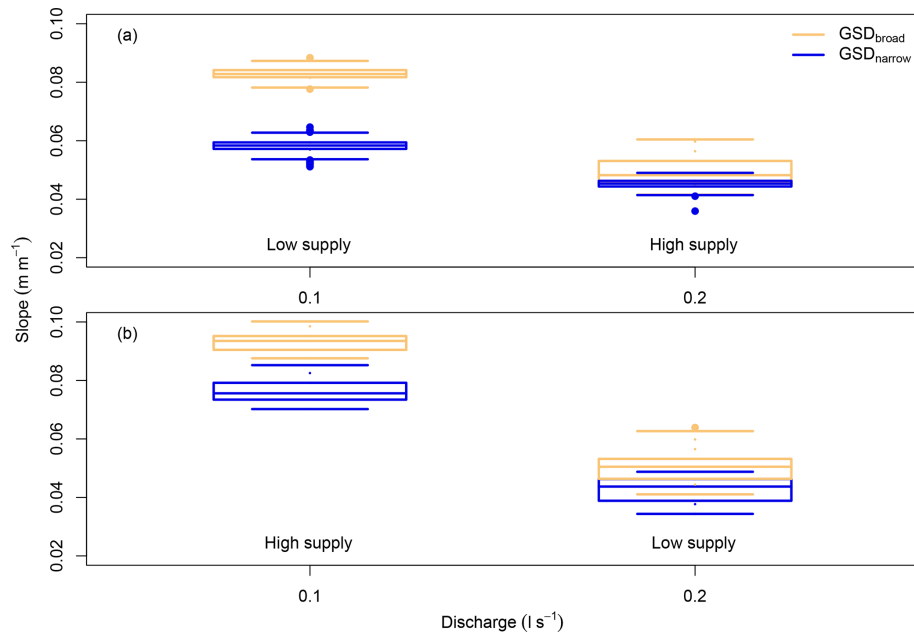


Figure 6. Distribution of slope values from the onset of transport onwards. Plots separate experiments by relative sediment concentrations of (a) 1 and (b) not 1 (i.e. 0.5 or 2). Text indicates sediment feed rate (low supply = 1 g s^{-1} , high supply = 2 g s^{-1}).

differences resulting from changes between run conditions for the same grain size distribution are shown in Table 2.

Sediment output rates show a decrease in the proportion of sediment storage in response to increases in discharge (Table 3). For both grain size distributions, more

material is stored at lower discharges, resulting in steeper-sloped deposits. Doubling the feed rate results in both systems retaining a higher proportion of sediment within the system at 100 mL s^{-1} , although this effect is more prominent in $\text{GSD}_{\text{broad}}$: 59.3 % to 91.5 % and 27.1 % to 33.6 % for

Table 1. Mean slope values and standard deviations, for the eight experiments reported here.

	GSD _{broad}			GSD _{narrow}		
	Mean	SD	<i>n</i>	Mean	SD	<i>n</i>
100L	8.29×10^{-2}	1.96×10^{-3}	224	5.81×10^{-2}	2.21×10^{-3}	281
100H	9.30×10^{-2}	2.99×10^{-3}	101	7.68×10^{-2}	3.93×10^{-3}	175
200L	4.98×10^{-2}	4.28×10^{-3}	437	4.28×10^{-2}	3.89×10^{-3}	449
200H	4.92×10^{-2}	4.36×10^{-3}	256	4.52×10^{-2}	1.57×10^{-3}	243

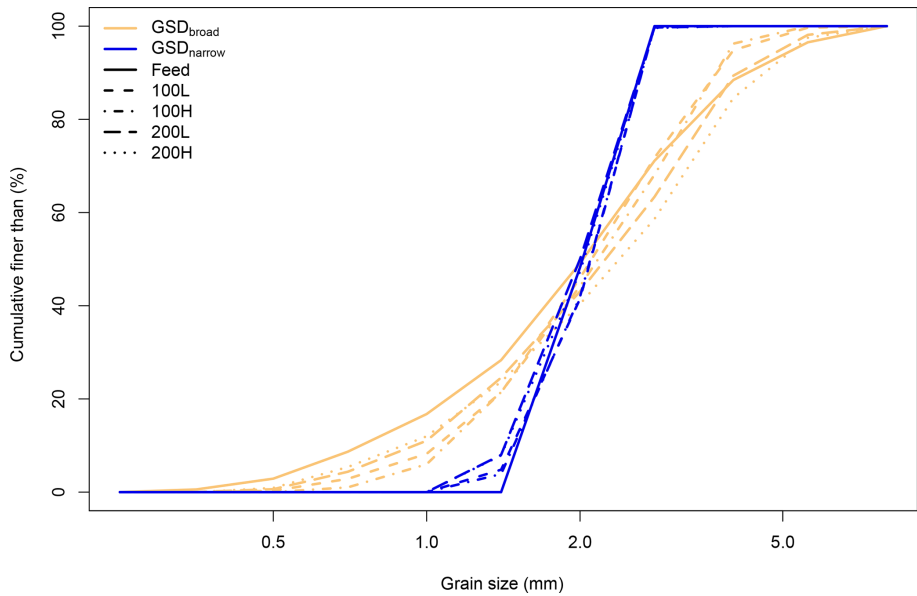


Figure 7. Size distributions of material output across the length of each experiment. Original grain size distributions are also provided.

Table 2. Changes in mean slope for the column name experiment, given relative to the row name experiment, for GSD_{broad} and GSD_{narrow} respectively. Values are given in %.

	100L	100H	200L	200H
100L	–	12.2/32.1	–40.0/–26.4	–40.6/–22.2
100H	–10.9/–24.3	–	–47.1/–41.1	–46.5/–44.3
200L	66.7/35.9	86.9/79.6	–	–1.03/5.77
200H	68.4/28.5	88.9/69.8	1.05/–5.46	–

GSD_{broad} and GSD_{narrow}, respectively. However, when discharge is increased, regardless of feed rate, the two systems behave more similarly both with respect to feed rate and with each other. Here, 16.3 % and 18.3 % of material is stored for GSD_{broad} under low and high feeds, respectively, and only 9.4 % and 8.6 % for GSD_{narrow}. At higher discharges and higher sediment supply rates, the onset of transport occurs earlier regardless of grain size distribution (Table 4). In addition, output starts later using GSD_{broad} for all experiments barring 200H, where transport begins at almost the same time.

Table 3. Output of sediment during each experiment, from the time sediment output occurred. The proportion of sediment output is relative to the volume input over the same time span.

	Mean output rate (g s ^{−1})		Proportion stored of input (%)	
	GSD _{broad}	GSD _{narrow}	GSD _{broad}	GSD _{narrow}
100L	0.41	0.73	59.3	27.1
100H	0.19	1.34	91.5	33.6
200L	0.84	0.91	16.3	9.4
200H	1.64	1.84	18.3	8.6

Table 4. Timing of the onset of transport, given in minutes from the start of the experiment.

	GSD _{broad}	GSD _{narrow}
100L	326	149
100H	149	116
200L	103	87
200H	42	44

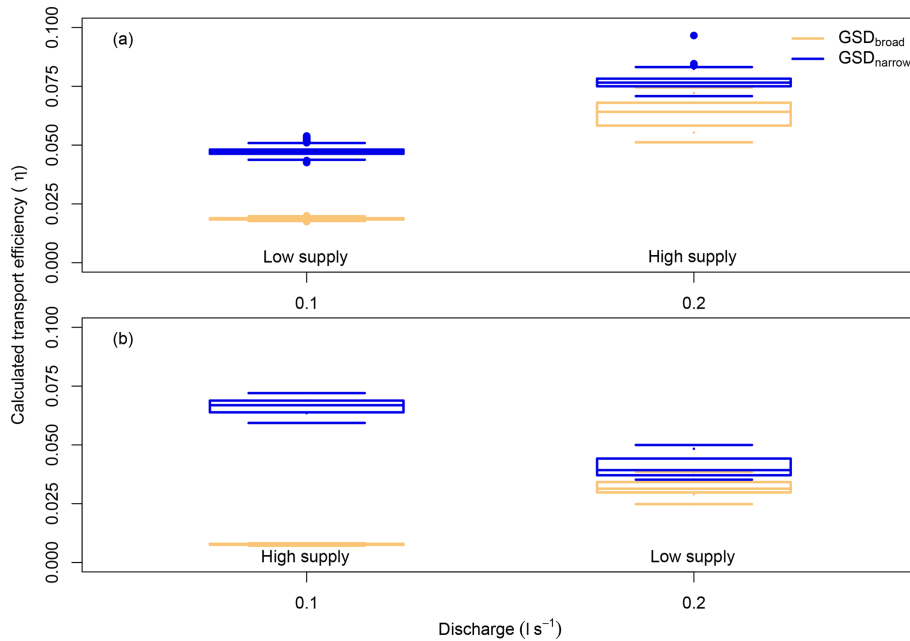


Figure 8. Distribution of transport efficiencies, calculated using Eq. (3). Plots separate experiments by relative sediment concentrations of (a) 1 and (b) not 1 (i.e. 0.5 or 2). Text indicates sediment feed rate (low supply = 1 g s^{-1} , high supply = 2 g s^{-1}).

Table 5. Grain size statistics of output material, averaged over the total output mass and given in millimetres (mm).

	GSD _{broad}			GSD _{narrow}		
	D_{50}	D_{84}	σ	D_{50}	D_{84}	σ
Bulk	2.03	3.65	1.38	2.02	2.52	0.42
100L	2.11	3.38	1.03	2.10	2.55	0.45
100H	2.17	3.42	1.00	2.10	2.55	0.44
200L	2.24	3.72	1.24	2.00	2.52	0.48
200H	2.39	3.94	1.39	2.03	2.53	0.48

The distributions of the output material show a variable agreement between the input load and the output material (Fig. 7 and Table 5). For GSD_{broad} the D_{50} of the output is coarser at all discharges, whereas the D_{84} is finer at 0.1 L s^{-1} and coarser at 0.2 L s^{-1} . The output mixture also only equals the feed σ at high feed rate and discharge. In contrast, GSD_{narrow} has a slightly higher output D_{50} at low discharge and finer at high discharge, with an almost constant D_{84} . In addition, the σ is always higher than the feed rate. This, caused by the addition of a fine tail, is an artefact of the rotary feeder used in these experiments: the action of the rotating feeder pipe crushed a small amount of sediment as it was input into the flume. Overall, however, there is strong agreement between the feed and output grain mixtures.

Three key observations can be made regarding the distribution of transport efficiencies (Fig. 8). First, the distribution

of calculated transport efficiencies of GSD_{broad} are consistently lower than those of GSD_{narrow} (Table 6), following from the differences in slope reported above. For example, the mean transport efficiency of GSD_{narrow} is 154 % greater than GSD_{broad} for experiment 100L. Second, increasing water discharge, for a given feed rate, increases the efficiency of both grain size distributions except for GSD_{narrow} under low feed, where a decrease is observed (Table 7); efficiency for GSD_{broad} is 17.2 % higher under 100L than 100H. Third, increasing feed rate, for a given discharge, increases the efficiency of both grain size distributions except for GSD_{broad} with low discharge, where a decrease is observed (Table 7).

The mean slope values were also used to calculate the reference shear stress (τ_r) necessary to entrain the D_{84} using the approach of Wilcock and Crowe (2003):

$$\frac{\tau_{ri}}{\tau_{rs50}} = \left(\frac{D_i}{D_{50}} \right)^b, \quad (4)$$

where τ_{rs50} is the reference stress for the median surface grain size (D_{50}), and b is an exponent of value 0.67 when i is larger than the mean surface grain size. Equation (4) produces a shear stress that is 48.1 % greater for entrainment of the D_{84} than the entrainment of the median in GSD_{broad} and a shear stress that is 15.5 % greater for GSD_{narrow}. This value is static for each mixture, solely based on the grains comprising the mixture and not on deposit characteristics, slope, or bed state. We also calculated the mixture mobility transition point (τ_m^*) from Recking (2013), which is adapted from Recking (2010), using

Table 6. Mean transport efficiencies and their standard deviation with the number of observations (n) of the experiments.

	GSD _{broad}			GSD _{narrow}		
	Mean	SD	n	Mean	SD	n
100L	1.87×10^{-2}	4.42×10^{-4}	224	4.75×10^{-2}	2.21×10^{-3}	281
100H	3.21×10^{-2}	2.81×10^{-3}	101	4.05×10^{-2}	3.82×10^{-3}	175
200L	7.71×10^{-3}	2.48×10^{-4}	437	6.60×10^{-2}	3.29×10^{-3}	449
200H	6.33×10^{-2}	5.50×10^{-3}	256	7.68×10^{-2}	2.80×10^{-3}	243

Table 7. Changes in mean transport efficiency for the column name experiment, given relative to the row name experiment, for GSD_{broad} and GSD_{narrow} respectively. Values are given in percent (%).

	100L	100H	200L	200H
100L	–	–58.7/39.1	71.9/–14.7	239/61.9
100H	142/–28.1	–	316/–38.6	721/16.4
200L	–41.8/17.2	–76.0/63.0	–	97.3/89.8
200H	–70.5/–38.2	–87.8/–14.1	–49.3/–47.3	–

Table 8. Mixture mobility transition points calculated using Eq. (5), taken from Recking (2013).

	GSD _{broad}	GSD _{narrow}
100L	0.414	0.318
100H	0.479	0.417
200L	0.228	0.240
200H	0.225	0.264

$$\tau_m^* = (5S + 0.06) \left(\frac{D_{84}}{D_{50}} \right)^{4.4\sqrt{S}-1.5}, \quad (5)$$

where S is energy slope, and the transition point represents the Shields stress where partial mobility transitions to full mobility (Table 8). GSD_{broad} has substantially higher values for both low and high feeds (0.414 and 0.479, respectively) than GSD_{narrow} at low discharge (0.318 and 0.417), but they decrease at higher discharges (0.228 and 0.225) and approximate those of GSD_{narrow} (0.240 and 0.264), albeit slightly lower in value. That is, both mixtures exhibit similar transitions between partial and full mobility under the higher discharges, but GSD_{narrow} remains substantially lower at lower discharges.

In addition, the experiments also demonstrate differences in the morphologies, particularly centred around the form and behaviour of bars in the flume. The full suite of evidence is available in the supplemental videos submitted with this paper, but key frames are also included here. The bars formed using GSD_{broad} seem to form from the coarser end of material and exhibit greater curvature, whilst those of GSD_{narrow} form bars that deflect flow to a lesser extent, which are tex-

turally indistinguishable from the bulk mix. At lower discharges, both grain size distributions exhibit higher numbers of bars with lower wavelengths, with GSD_{broad} typically organising to shorter wavelengths than GSD_{narrow} (Fig. 9a and c). At higher discharges, the number of bars decreases for both mixtures and their wavelengths increase to compensate, with GSD_{broad} continuing to exhibit a shorter wavelength (Fig. 9b and d). We also observed the occurrence of erosional events that we will refer to as “thalweg sweeps”, presented as a series of frames in Fig. 10 and also observable in the supplemental videos. During these events, the thalweg laterally erodes through the adjacent bar and then either remains on the new side or migrates back to its original position. These bar sweeps do occur in both grain mixtures; however, they are relatively limited in their frequency and magnitude in GSD_{broad} and are a more defining feature of the morphodynamics of GSD_{narrow}.

4 Discussion

The results of these experiments clearly demonstrate that the range of grain sizes present in the bed material and load exerts first-order control over self-formed deposition, and it is therefore inappropriate to simply use the median surface grain size in order to characterise the system under all conditions. The extent of this influence, however, varies with the boundary conditions under which the experiments are conducted. At lower discharges, differences between the two grain size distributions can be attributed to the relative difficulty of the channel to mobilise the larger grains, thus it is the volume of supplied material that influences the efficiency of transport. At higher discharges, the difference in behaviour between the two mixtures decreases as the mobility differences also decrease.

4.1 Differential mobility

The difference in mobility varying alongside discharge is shown by our primary response variable, slope. Slope acts as an indicator of the system’s ability to transport the material supplied to it, as mediated by the energy supplied to it (Mackin, 1948; Lane, 1955; Church, 2006; Eaton and Church, 2011). If we were to predict behaviour of the systems from the Lane and Church relations (Eqs. 1 and 2), we

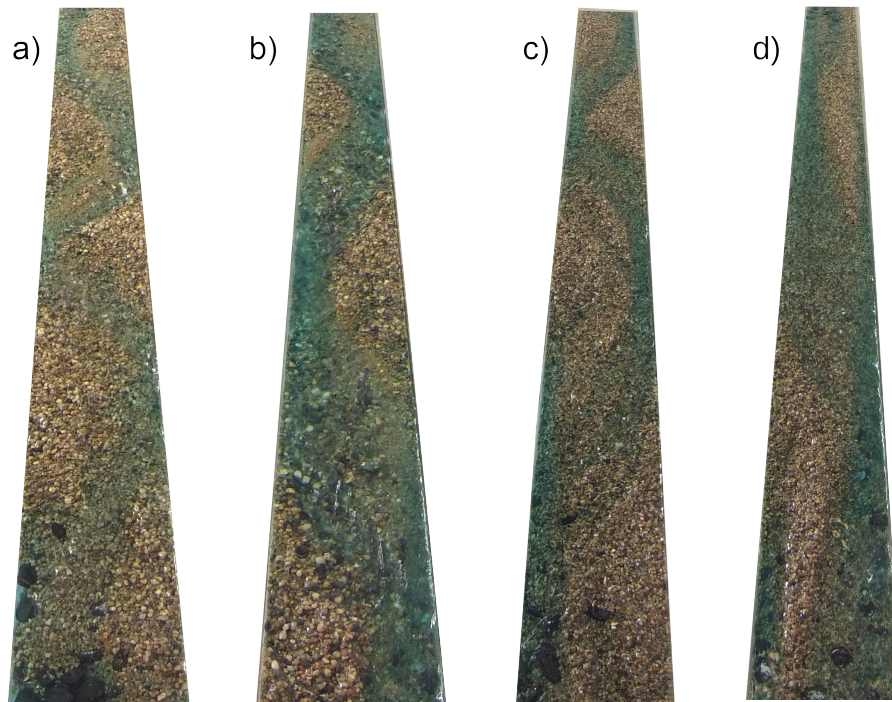


Figure 9. Example images of bed state taken from GSD_{broad} at low (a) and high (b) discharge, and GSD_{narrow} at low (c) and high (d) discharge.

would assume that both grain size distributions would behave in the same manner. Additionally, those experiments of the same relative sediment concentration (100L and 200H) would have the same values of slope. Further, where sediment concentration was increased or decreased, we would expect commensurate increases or decreases in slope, respectively. However, one set of systems (i.e. those of the broadly graded GSD_{broad}) consistently organise to higher slopes and lower transport efficiencies than those for the more narrowly graded (i.e. GSD_{narrow}) systems for each experimental condition. As all systems were continuously accumulating, static sediment surface armouring (e.g. Sutherland, 1987; Parker and Sutherland, 1990; Gomez, 1994) could not occur due to the suppression of selective transport and subsequent equivalence between the bed surface and sediment feed grain size distributions. Instead, here the bed surface resembled the bed states that Iseya and Ikeda (1987) and Lisle et al. (1991) observed, in which the mixture is laterally organised. Bennett and Bridge (1995) also observed a lack of bed texture adjustments under aggrading settings, when the accumulation is induced either by flume slope or feed rate changes. Therefore, we believe that the observed differences in slope cannot be attributed to differing degrees of surface armouring across the bed surface.

A potentially critical explanation for this disparity is that equal mobility does not apply to all of the bed sediment all of the time. For example, Andrews (1983) found equal mobility applied only to sediment finer than about the bed surface D_{84}

in their field study, and nearly all of the data on bed mobility published by Haschenburger and Wilcock (2003) showed similar relative stability of the largest grains at even the highest shear stresses. Mixtures do approach equalised mobility under higher entraining stresses, although larger grains are still entrained less frequently and travel less distance (Church and Hassan, 1992). We believe that this suggests that the size of the largest sediment in the bed may determine the deposition threshold for a mixture, at least for those situations in which competence controls sediment deposition, not sediment transport capacity. The implication of which is that the gradient of self-formed alluvial deposits is likely to be related to the mobility of the largest sediment in transport not the median grain size, as evidenced in bimodal fan experiments (Reitz and Jerolmack, 2012; Delorme et al., 2017).

According to the conventions established by Lane (1955) and Church (2006), both of our grain size distributions had the same sediment calibre, so why did they not equilibrate at the same slope and achieve the same transport efficiency? The average size of the sediment feed calibre is almost identical for both GSD_{broad} and GSD_{narrow} . While we can explain the failure of Eq. (1) as stemming from its original intention to be used as a qualitative guide for thinking about channel grade, Eq. (2) is based on the existing semi-empirical representations of bed sediment entrainment, so the discrepancy between Eq. (2) and the results in Fig. 8 points to a more fundamental problem. Under these conditions, both mixtures do not exhibit the same mixture mobility because of the distri-

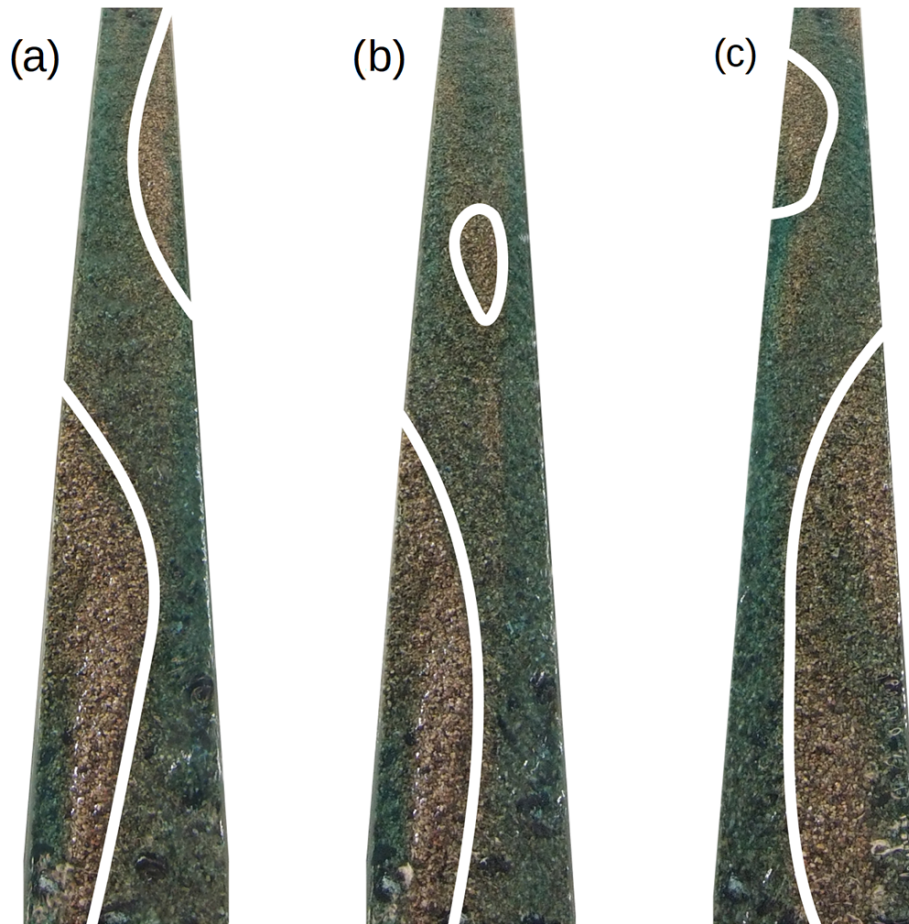


Figure 10. Three frames taken from the beginning, middle and end of a thalweg sweep event from the left side of the flume to the right and resulting in a switching of the thalweg position, in experiment 200H using GSD_{narrow}. These frames correspond to approximately 28 to 30 s of the accompanying video.

bution's relationship with the threshold of motion; both mixtures are not equally mobile irrespective of discharge. Simply put, these results clearly indicate that D_{50} is a poor choice for the characteristic grain size, at least when considering the processes forming (i.e. aggrading) alluvial deposits at lower discharges (i.e. the majority of the time), rather than those eroding them or under equilibrium conditions. The use of these equations confirms that the D_{50} is only appropriate under equal mobility conditions. Our preliminary analysis suggests that some representation of the coarse tail is probably more appropriate (such as the D_{84} , which is commonly used in flow resistance equations (e.g. Lenzi et al., 2006; Ferguson, 2007; Recking et al., 2008)), under the partial mobility conditions shown during some of these experiments.

At a basic level, the observed difference in slopes is associated with the differential ability of two experimental systems to transport sediment, which in turn is related to the relative thresholds of motion of the largest grains. Curran and Wilcock (2005) observed a gravel–sand mixture organising to lower slopes in response to increased proportions of

sand, implying that the higher sand presence decreased the critical shear stress necessary to transport coarser material, a common feature in bed organisation studies (e.g. Iseya and Ikeda, 1987). When the bed is organised as such, the variance of force exerted upon the grain and thus the likelihood of entrainment increases (Schmeeckle et al., 2007), hence the lower deposit slope and higher mobility. Here we infer that the inverse is in operation, with the presence of coarser grains decreasing the overall transport rate by increasing the entraining stresses of the mixture in a similar manner to their behaviour in degrading settings (Church et al., 1998; MacKenzie and Eaton, 2017), antithetical to the influence of sand. That is, the presence of coarse grains acts in a manner similar to those in kinematic waves and traction clogs in slowing the overall bed load motion (Leopold and Wolman, 1957; Moss, 1963; Langbein and Leopold, 1966; Ashmore, 1991).

Based solely on the differences in reference stress values (Eq. 4), we would expect a fixed difference in slopes between the two grain mixtures. However, our observations of the dif-

ferential system state responses (i.e. slope) show that the degree of this difference changes with discharge. Our calculations of the transitional Shields stress, from Recking (2013), indicates that this value changes alongside discharge, as a product of slope. The differences in slope at low discharge and similarities at high discharge indicate the importance of the absolute mobility of the bed material, and the coarser fraction, in conjunction with its relative mobility. That is, if the material is subjected to a larger fluid force (i.e. higher discharge), it performs the same role as removing those grains which cause the immobility, and hence a convergence in behaviour.

The threshold calculation used in Eq. (5) invokes the partial and full mobility conditions under differing flow strengths by Wilcock and McArde (1993). Although we cannot calculate a shear stress, given the lack of water depths, it is a useful indicator of the state of the system at a more generic scale, regardless of the actual values of τ_m^* . This separation between transport regimes at low and high discharges is also similar to the observation of the three phase transport models of Ashworth and Ferguson (1989) and Warburton (1992), where full mobility is achieved above a threshold discharge following the cessation of a given influence. However, the increased transport rates are not generated through the destruction of previously organised structures (e.g. Laronne and Carson, 1976; Cudden and Hoey, 2003; Recking et al., 2009). Instead the difference is sourced from an increase in the maximum grain size entrainable by the flow, and the likelihood of that grain's entrainment. The fact that we see a broadly graded mixture (GSD_{broad}) acting in a manner similar to one that is narrowly graded (GSD_{narrow}) at higher discharges suggests that Eq. (2) is applicable when there is equal sediment mobility as the characteristic grain size approaches the median.

We also observed two further phenomena that may contribute to the observed output distributions. First, the finest material would often be found at the base of the flume during preparation for the next run, having filtered through the coarser matrix; a phenomenon limited to GSD_{broad} . The hiding of this finer material through vertical sorting explains the observed differences in the fine tail (Fig. 7) as well as the constant coarser D_{50} for GSD_{broad} . Second, there was a degree of coarse material deposition at the mouth of the feeder. However, as shown by the similarities of the output and input D_{84} (Table 5), this only affected GSD_{broad} at the low discharges, presumably when these grains were not mobile throughout the mixture, regardless of their deposition upstream. Therefore, we believe the mobility differences are systematic between the two distributions.

4.2 Bedform and dynamics

The differences in morphodynamics extend beyond reach-average 1-D parameters like depositional slope and transport efficiency. Our observations of the bed dynamics have high-

Table 9. Flume dimensions and run conditions for Lisle et al. (1991) and the two 100L experiments included here.

	Lisle et al. (1991)	GSD_{broad}	GSD_{narrow}
Length (m)	7.5	2	2
Width (m)	0.3	0.128	0.128
Slope ($m\ m^{-1}$)	0.03	0.083	0.058
Grain size range (mm)	0.35–8	0.25–8.0	1.4–2.8
D_{50} (mm)	1.4	2.03	2.02
Flow rate ($mL\ s^{-1}$)	582	100	100
Feed rate ($g\ s^{-1}$)	8.4	1	1
Run time (min)	560	549	429

lighted the important role that surficial organisation plays in controlling channel morphology and influencing sediment transport rates. Surface organisation is a frequent response of channels to increased sediment supply in order to maintain some sediment coherency (Lisle and Hilton, 1992; Kasai et al., 2004; Pryor et al., 2011). The alternate bar morphodynamics we observed during some runs have been previously observed (Table 9), arising from unequal stresses across the bed (Lanzoni, 2000). Under a similar grain size distribution to GSD_{broad} , Lisle et al. (1991) observed the formation of stationary (non-migrating) lateral bars with the bed surface separated into congested and smooth zones, influencing transport paths.

Bedforms can influence sediment transport efficiency through the dissipation of energy and increased channel stability (Cherkauer, 1973; Hey, 1988; Prancevic and Lamb, 2015), and the bar characteristics are strongly linked to the maximum size of sediment in the bed material here. In GSD_{broad} , bars were more persistent in time and space than in GSD_{narrow} due to the importance of large grains as stabilising features for bars. In the case of GSD_{broad} the largest grains clearly deposited first, creating a locus of deposition around which the bar head formed, allowing additional sediment to accumulate in its wake (Leopold and Wolman, 1957; Ashmore, 1991; Ferguson, 1993). The bars formed during GSD_{narrow} were comprised of virtually the same size sediment, which can be entrained over a narrow range of shear stresses. As a result, the whole bar may be entrained at a similar shear stress, making these features more transient, and reducing their overall effect on bed stability as their relative impermanence means that the flow can freely move through them (Figs. 9 and 10). It is important to note that the stabilisation of the large grains in our experiment GSD_{broad} was not the result of jamming, as described by Church (2006). The size of our flume was such that the ratio of the flume width to D_{84} was greater than 6, the jamming ratio proposed by Zimmermann et al. (2010), and it is thus solely the result of deposition.

The formation of lateral bars allows for the transport of bed load through the contraction of the channel width increasing unit stream power as flow is concentrated (Lisle, 1987). This organisation of the bed surface into zones of

transport and deposition thus maximises the efficiency of the channel (Iseya and Ikeda, 1987; Ferguson et al., 1989) and enables the previously limited transmittance of sediment and the growth of the depositional lobe. The wavelengths of the bar forms we observed in higher sediment output experiments are longer than those of high sediment storage. Experiments by Pyrce and Ashmore (2003a, 2005), and a meta-analysis by Pyrce and Ashmore (2003b), demonstrated that the wavelength of bar spacing is a function of the transport lengths of bed load particles at channel-forming flows; therefore, the material is more mobile in higher wavelength reaches. Transport length is the distance between entrainment (τ_{ce}) and distraintment (τ_{cd}); therefore, it is dependent on when the grain is deposited. Ancey et al. (2002) observed a type of hysteretic difference between these two thresholds, where the specific flow rate (and thus stress) necessary to induce deposition is lower than the entraining flow. Given the differences in entraining threshold between the mixtures, assuming that it is controlled by the coarse tail, it follows that the distraintment threshold for GSD_{broad} will be higher than for GSD_{narrow} , such that a smaller decrease is needed to trigger deposition. Therefore, the systems can be characterised by the difference in behaviour of the coarse grains comprising the bar head loci (Pyrce and Ashmore, 2005). For the more equally mobile GSD_{narrow} , this is manifested in a decreased likelihood of deposition of these grains, triggering longer path lengths and greater bar wavelengths in the system. In other words, the likelihood of entrainment ($P[\tau > \tau_{ce}]$) is greater in GSD_{narrow} , setting a lower overall deposit slope, whereas the likelihood of distraintment ($P[\tau < \tau_{cd}]$) is higher in GSD_{broad} , decreasing transport length. This difference is reduced as discharge increases because the likelihood of entrainment increases, and distraintment decreases, for both mixtures but more strongly for GSD_{broad} , hence the similarity between τ_m^* values at higher discharges.

Were we to pinpoint the actual characteristic grain size of the material, we might expect the slopes to actually organise to the same values. For example, if we were to pair these distributions instead by a coarser grain (e.g. the D_{84}), we might have observed more similar self-organised slopes. However, this view still assumes the same inherent grain class mobility across discharges, which is the theoretical basis behind Church (2006), merely shifted in favour of the larger grains contributing more relative stability. That is, each mixture still has different distributions of transport likelihoods; does the characteristic grain size actually represent enough of the bed processes that the overall system behaves in the same manner? If the lateral bars were composed of coarser material, with the same narrow gradation as GSD_{narrow} , the depositional slope and wider morphodynamics may be similar (i.e. general organisation), but the finer scale processes (i.e. sediment transport and meander wavelength) would not be. However, it might be the case that similar characteristic grain sizes are just an artefact of the experimental design, rendered irrelevant when boundary conditions are expanded to differ-

ent ranges. Additionally, mobility differences can be more strongly controlled through channel widening and planform adjustments than allowed within this flume; thus, the importance of grain class thresholds are reduced as there are more options for resistance to be generated (Eaton and Church, 2004). Thus, the discussion of any one characteristic size is only useful within a given comparison, and it does not necessarily indicate a behaviour fundamental to self-formed channels but is merely the smallest partially mobile grain class (Wilcock, 1993).

We can therefore consider the systems generated by GSD_{narrow} as less stable on three accounts. Firstly, they developed at lower slopes and, as a result, were able to prograde more quickly due to reduced deposit volume. Secondly, the grains were more equally mobile due to a lower maximum threshold stress (i.e. smaller coarse fraction). Thirdly, the degree of surficial organisation was lower and bedforms were less persistent. The combination of these factors results in a system that does not need to concentrate flow in order to exceed threshold stress, despite the flow's lower slope and stream power, indicating its ability to transport sediment more efficiently than in experiments using GSD_{broad} .

5 Conclusions

The eight experiments presented here demonstrate a difference in the self-adjusted slope and morphodynamics of aggrading systems derived from the difference of their grain size distributions and mediated by the relative sediment concentration. According to the prevailing theory that the median grain size is predictive of channel behaviour, the systems described within this paper should have exhibited similar slopes and patterns of morphodynamics under the same boundary conditions. Instead, the deposit formed from the more widely graded distribution (GSD_{broad}) developed to a higher slope, with lower transport efficiency, and demonstrated a greater degree of surface organisation. We argue that this is the result of the large grains present in this mixture that exceed the competence of the flow, and they require channel narrowing in order to mobilise. Where these grains are absent (i.e. the narrowly graded GSD_{narrow}) the channel fails to organise to its most stable state (i.e. lateral bars with narrow thalweg) as regularly because of the more equally mobile sediment and bars. This difference decreases as discharge is increased (i.e. entraining stresses). Thus channel stability is linked not to the mobility of the median grain size, but to the mobility of the largest grains (e.g. D_{84}). We therefore conclude that the difference in behaviour between these systems is driven by a competence limitation of the larger grains. These findings indicate that models that include sediment transport and conceptualise stability, such as regime models, need to consider the characteristic grain size as a coarser fraction than the median in order to more realistically replicate behaviour in aggrading systems.

Code and data availability. Both the code and data used to create Figs. 2 and 4–8 are available online (<https://doi.org/10.5281/zenodo.3626231>; Booker, 2020).

Video supplement. Videos of the bed morphodynamics are available online; GSD_1 corresponds to GSD_{broad} : Q100L (<https://doi.org/10.5446/41771>), Q200H (<https://doi.org/10.5446/41772>), Q100H (<https://doi.org/10.5446/41773>), Q200L (<https://doi.org/10.5446/41774>). GSD_2 corresponds to GSD_{narrow} : Q100L (<https://doi.org/10.5446/41775>), Q200H (<https://doi.org/10.5446/41776>), Q100H (<https://doi.org/10.5446/41778>), Q200L (<https://doi.org/10.5446/41777>).

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