

**Predicting the roughness length of turbulent flows over landscapes**

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# Predicting the roughness length of turbulent flows over landscapes with multi-scale microtopography

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Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



## Abstract

The fully rough form of the law of the wall is commonly used to quantify velocity profiles and associated bed shear stresses in fluvial, aeolian, and coastal environments. A key parameter in this law is the roughness length,  $z_0$ . Here we propose a predictive formula for  $z_0$  that uses the amplitude and slope of each wavelength of microtopography within a discrete-Fourier-transform-based approach. Computational fluid dynamics (CFD) modeling is used to quantify the effective  $z_0$  value of sinusoidal microtopography as a function of the amplitude and slope. The effective  $z_0$  value of landscapes with multi-scale roughness is then given by the sum of contributions from each Fourier mode of the microtopography. Predictions of the equation are tested against  $z_0$  values measured in  $\sim 10^5$  wind velocity profiles from southwestern US playa surfaces. Our equation is capable of predicting  $z_0$  values to 50 % accuracy, on average, across a four order-of-magnitude range.

## 1 Introduction

### 1.1 Problem statement

The velocity profiles of turbulent boundary-layer flows are often quantified using the fully rough form of the law of the wall:

$$u(z) = \frac{u_*}{\kappa} \ln \left( \frac{z}{z_0} \right), \quad (1)$$

where  $u(z)$  is the wind velocity (averaged over some time interval) at a height  $z$  above the bed,  $u_*$  is the shear velocity,  $\kappa$  is the von Kármán constant (0.41), and  $z_0$  is an effective roughness length that includes the effects of grain-scale roughness and microtopography (e.g. Bauer et al., 1992; Dong et al., 2001). Velocity profiles measured in the field are commonly fit to Eq. (1) to estimate  $u_*$  and/or  $\tau_b$  for input into empirical

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### Predicting the roughness length of turbulent flows over landscapes

J. D. Pelletier  
and J. P. Field

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



## Predicting the roughness length of turbulent flows over landscapes

J. D. Pelletier  
and J. P. Field

sediment transport models (often after a decomposition of the bed shear stress into skin and form drag components) (e.g. Gomez and Church, 1989; Nakato, 1990). Fits of wind-velocity profiles to Eq. (1) also provide measurements of  $z_0$ . Given a value for  $z_0$ , a time series of  $u_*$  and/or  $\tau_b$  can be calculated from Eq. (1) using measurements of velocity from just a single height above the ground. This approach is widely used because flow velocity data are often limited to a single height. Equation (1) only applies to  $z \geq z_0$ , and may be further limited in its accuracy within the roughness sublayer, i.e. the range of heights above the ground comparable to the height of the largest roughness elements. Values of  $z_0$  depend on microtopography/land cover (quantifying this dependence in unvegetated landscapes is a key goal of this paper) and are typically in the range of  $10^{-2}$ – $10^1$  mm for wind flow over arid regions (Prigent et al., 2005).

Most existing methods for estimating  $z_0$  using metrics of surface roughness or microtopography rely on the concept of a dominant roughness element, the size and density of which the user must specify a priori (e.g. Lettau, 1969; Arya, 1975; Smith and McLean, 1977; Jacobs, 1989; Raupach, 1991, 1994; Kean and Smith, 2006a). Procedures are available for estimating  $z_0$  in landscapes with multi-scale roughness, but they often rely on idealizations such as treating the microtopography as a sequence of Gaussian bumps (e.g. Kean and Smith, 2006b). Nearly all natural landscapes have microtopographic variability over a wide range of spatial scales. Identifying the dominant scale objectively and uniquely can be difficult. For example, the top plot in Fig. 1 shows a hypothetical case of a landscape composed of two superposed sine waves. The effective roughness length of a landscape is related to the presence/absence or extent of flow separation, and flow separation is primarily controlled by the derivatives of topography (slope and curvature) rather than the amplitude of the bedforms/roughness elements (Simpson, 1989; Lamballais et al., 2010). As such, roughness elements of smaller amplitude but steeper slopes may exert greater control on  $z_0$  values compared with roughness elements that are larger in amplitude but gentler in slope. Given a landscape with multi-scale roughness in which each scale has distinct amplitudes

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion





## Predicting the roughness length of turbulent flows over landscapes

J. D. Pelletier  
and J. P. Field

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



concluded that “the spacing of morphological elements is far less powerful in explaining variations in  $z_0$  than metrics based on surface roughness height.” In this paper we build upon the results of Nield et al. (2014) to show that  $z_0$  can be most accurately predicted using a combination of the amplitudes and slopes of microtopographic variations measured at multiple scales using Fourier analysis.

The presence of multi-scale roughness in nearly all landscapes complicates attempts to quantify effective  $z_0$  values for input into regional and global atmospheric and Earth-system models. In such models, topographic variations are resolved at scales larger than a single grid cell (10–100 km at present, but steadily decreasing through time as computational power increases) but the aerodynamic effects of topographic variations on wind velocity profiles at smaller scales are not resolved in these models and must be represented by an effective  $z_0$  value (sometimes in combination with an additional parameter, the displacement height, which shifts the location of maximum shear stress to a location close to the top of the roughness sublayer (Jackson, 1981)). Topographic variations at spatial scales below 10–100 km are typically on the order of tens to hundreds of meters. Currently available maps of  $z_0$  values do not incorporate the aerodynamic effects of topography at such scales. For example, Prigent et al. (2005) developed a global map of  $z_0$  in deserts by correlating radar-derived measurements of decimeter-scale roughness with  $z_0$  values inferred from wind velocity profiles. This approach assumes that the dominant roughness elements that control the effective  $z_0$  value over scales of 10–100 km occur at the decimeter scale captured by radar. It is possible that, in some landscapes, the roughness that controls  $z_0$  occurs at scales that are larger or smaller than those measured by radar. Therefore, a procedure is needed that predicts  $z_0$  values using data for topographic variations over a wide range of scales, including but not limited to decimeter scales. This study aims to fill that gap.

### 1.2 Study sites

We collected wind-velocity profiles and high-resolution topographic data using terrestrial laser scanning (TLS) from ten playa sites in the southwestern US (Fig. 2) during

## Predicting the roughness length of turbulent flows over landscapes

J. D. Pelletier  
and J. P. Field

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



the spring of 2015. These sites were selected based on the range of microtopographic roughness they exhibit (Table 1). Roughness can be quantified in multiple ways, but  $H_{\text{RMSE}}$ , the root-mean-squared deviation of elevation values measured at a sampling interval of 0.01 m, provides one appropriate metric (Nield et al., 2014). The ten sites range in  $H_{\text{RMSE}}$  from approximately 0.55 to 36 mm (see Sect. 2.1).

Each study site was an area of at least 30 m × 30 m with relatively uniform roughness, as judged visually and by analysis of the TLS data. The minimum fetch required for an equilibrium boundary layer flow is typically assumed to be 1000 times the height of the dominant roughness elements (Counihan, 1971). Based on this criterion, 30 m was adequate fetch for seven of the ten sites, i.e. all except for the three Death Valley sites, where roughness elements were up to 300 mm, hence the area of homogeneous roughness was verified to a distance of only ~ 100 times the height of the dominant roughness elements. However, the required fetch must also depend on the maximum height above the ground where velocities are measured to compute a  $z_0$  value locally, since any roughness transition triggers an internal boundary layer that grows indefinitely in height with increasing distance downwind of the transition. Using the Elliot (1958) formula for the height of the internal boundary layer downwind of a roughness transition, the minimum fetch required for a log-law profile between 0 and 3 m above the ground over a landscape with  $z_0 \approx 30$  mm (the value measured at the Death Valley rough site) is 31.8 m. According to this alternative criterion, 30 m may be adequate for an equilibrium boundary layer flow to be established to a height of 3 m despite the limited fetch-to-roughness height ratio at the Death Valley sites.

The playa surfaces at our study sites were predominantly crusted and ranged from flat, recently formed crust to well-formed polygons with deflated and broken crust ridges. All of the sites were completely devoid of vegetation. Sand blows episodically across some portions of the playas we studied but we chose study areas in which we observed no sediment transport during fast winds. We considered only landscapes without vegetation and loose, erodible sand because such cases must be understood first before the additional complications of flexible roughness elements and saltation-

**Predicting the roughness length of turbulent flows over landscapes**J. D. Pelletier  
and J. P. Field

induced roughness can be tackled. That said, we anticipate that concepts from this paper may be relevant to quantifying  $z_0$  over vegetated landscapes also.

Our goal is to understand the controls on boundary layer flows over rough terrain generally, not playa surfaces specifically or exclusively. As such, we use playa surfaces as “model” landscapes. Playas are useful for this purpose because they are macroscopically flat but exhibit a wide range of microtopographic roughness at small scales. The relative flatness of playas at scales larger than  $\sim 1$  m makes it possible to characterize their boundary layer flows using relatively short anemometer towers. Of course, playas are also of special interest to aeolian geomorphologists because they can be major dust sources when sand from playa margins is transported across the playa surface, disturbing crusted surfaces and liberating large volumes of silt- and clay-rich sediments.

The questions addressed in this paper could, in principle, be addressed using wind tunnel experiments. Wind tunnels certainly have the advantage of user control over wind velocities. However, Sherman and Farrell (2008) documented that  $z_0$  values in wind tunnels are, on average, approximately an order of magnitude lower than those measured in the field for otherwise similar conditions (e.g. grain size). One interpretation of the Sherman and Farrell (2008) results is that the confined nature of wind tunnel flows and/or their limited fetch can limit the development of boundary layers in equilibrium with bed roughness. For this reason, we focused on measuring wind flow over natural surfaces with homogeneous roughness characteristics over distances of at least 30 m surrounding our measurement locations.

**2 Methods****2.1 Terrestrial laser scanning and analyses of playa surface microtopography**

A Leica C10 terrestrial laser scanner was used to acquire point clouds of the central 10 m  $\times$  10 m ground surface upwind of the anemometers at each of the 10 study sites.

Title Page	
Abstract	Introduction
Conclusions	References
Tables	Figures
⏪	⏩
◀	▶
Back	Close
Full Screen / Esc	
Printer-friendly Version	
Interactive Discussion	



## Predicting the roughness length of turbulent flows over landscapes

J. D. Pelletier  
and J. P. Field

The areas surrounding each 10 m × 10 m area were also surveyed to check for approximate homogeneity in the roughness metrics out to areas of 30 m × 30 m, but the central 10 m × 10 m areas were the focus of the subsequent data analysis. Each area was scanned from four stations surrounding the 10 m × 10 m area and merged into a single point cloud using a Leica disk target system. Registration errors were a maximum of 2 mm in all cases. The Leica C10 has an inherent surface-model accuracy of 2 mm, but this value decreases as the number of overlapping scans increases (Hodge, 2010), resulting in a value of approximately 1 mm in the case of four overlapping scans. The scanner was mounted on a 3.5 m tripod to maximize the angle of incidence (low angles of incidence elongate the “shadows” or occlusions behind microtopographic highs (Brown and Hugenholtz, 2013)). All of the returns within each 1 cm<sup>2</sup> domain were averaged to create a Digital Elevation Model (DEM) with point spacing of 0.01 m. Voids were filled using natural-neighbor interpolation. Voids requiring interpolation were limited to < 1% of the area at the smoothest five sites (Lordsburg and Willcox Playas), between 1 and 3% at the two Soda Lake sites, and between 10 and 20% at the three Death Valley sites.

In addition to the calculation of basic topographic metrics such as  $H_{RMSE}$  and  $S_{av}$  (the latter being the average slope computed at 0.01 m scales) (Table 1), we also computed the average amplitude spectrum of all 1-D topographic transects at each study site. The amplitude spectrum is equal to two times the absolute value of the complex discrete Fourier transform (DFT). The average amplitude spectrum refers to the fact that the one thousand amplitude spectra of each 1-D transect computed along the east-west direction were averaged to obtain a single average spectrum for each study site. We used the DFT implemented in the IDL programming language. The DFT coefficients were also used as input to a filter that uses the amplitude and slope of each Fourier mode to compute its contribution to the  $z_0$  value. We created “mirror” images of each transect before application of the DFT. This approach has been shown to work as well or better than windowing for minimizing truncation error (i.e. incomplete sampling) in

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion





data sets characterized by the broadband/multi-scale variability characteristic of many environmental data series (Smigelski, 2013).

## 2.2 Measurement and analyses of wind profiles

Wind speeds were measured at 1 s intervals and at 7 heights above the surface (0.01, 0.035, 0.076, 0.16, 0.52, 1.22, and 2.80 m) using four Inspeed Vortex rotating cup anemometers and four AccuSense hotwire anemometers (F900 series) (the latter calibrated to work over the 0.15–10  $\text{ms}^{-1}$  range of wind velocities) (Fig. 3). The hotwire sensors were secured to an L-shaped steel frame and placed above the surface such that the small opening in the sensor head was oriented as perpendicular to the wind direction as possible (Fig. 3). The 10  $\text{ms}^{-1}$  range of the hotwire sensors was not a limiting factor because all of the hot-wire sensors were located close to the ground, i.e. within 0.16 m from the surface, where velocities were lower than 10  $\text{ms}^{-1}$  during our deployments. We collected data at each of the ten sites for ten to thirty hours spanning multiple days, times of day, and a wide range of wind velocities.

The lowest cup and the highest hotwire anemometers were positioned at the same height (0.16 m) above the surface to standardize measurements between the two types of wind sensors. When positioned at the same height, the hotwire sensors measured wind speeds (based on the factory calibration) that were approximately 10 % lower than the values obtained from the cup anemometers. We used the ratio of the wind velocities measured by the bottom cup anemometer to the wind velocities measured by the top hotwire sensor to standardize the hotwire measurements to the cup anemometer measurements in real time. This scaling-factor approach also serves a second purpose, which is to minimize the effects of wind-direction variability on the velocities measured by the hotwire sensors. The cup sensors measure wind speeds effectively from nearly any direction, but the hotwire sensors are required to be oriented within 20° perpendicular to the wind for greatest accuracy. The hotwires were manually repositioned following large and sustained changes in wind direction, but short-duration changes may have resulted in oblique incidence angles with a bias towards lower velocities. Contin-

## Predicting the roughness length of turbulent flows over landscapes

J. D. Pelletier  
and J. P. Field

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

⏪

⏩

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



ually rescaling the velocities measured by the highest hotwire sensor to the lowest cup sensor mitigated this potential problem.

Scaled values from the bottom three (0.01, 0.035, and 0.076 m) hotwire sensors were combined with the four cup anemometers to calculate shear velocities,  $u_*$ , and aerodynamic roughness lengths,  $z_0$ , based on the average velocities measured in each 12 s interval via least-squares fitting of the wind velocities to the natural logarithm of the distance above the ground. The shear velocity is equal to the slope of  $u$  vs.  $\ln z$  divided by  $\kappa$ . The roughness length is equal to the exponential of the following: minus the intercept divided by the slope. The 12 s interval was chosen based on the results of Nimakas et al. (2003), who found that time intervals greater than 10 s resulted in the most accurate results, while those obtained from smaller averaging intervals were less reliable. Values of  $z_0$  can be influenced by deviations from neutral stability. A common way to address this issue is to remove profiles from the analysis in which the velocity at a given height is below some threshold value (e.g. Nield et al., 2014). In this study we repeated our analysis using only those profiles with a wind velocity of at least  $3 \text{ m s}^{-1}$  at a height of 0.16 m. The mean and standard deviations of  $z_0$  were nearly identical to those obtained using all of the data, likely reflecting the fact that we targeted time periods of fast winds for measurement.

During the data collection, the hotwire sensors were moved to approximately 25–50 random locations within each site. We moved the hotwire sensors to numerous locations within each site because wind velocities measured close to the ground are sensitive to the microtopography of the specific spot above which they are measured, i.e. the  $z_0$  value measured on the stoss side of a microtopographic high tends to be smaller than the  $z_0$  value measured on the lee due to the convergence/divergence of flow lines. Since our goal was to characterize the average or representative  $z_0$  value over each surface, it is appropriate to move the hotwire sensors around the surface to ensure that the results are not specific to one location but instead represent a statistical “sample” of the flow above the surface at multiple locations. This approach is also consistent with how the CFD model output was analyzed (see Sect. 2.3).

**Predicting the roughness length of turbulent flows over landscapes**

J. D. Pelletier  
and J. P. Field

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



## Predicting the roughness length of turbulent flows over landscapes

J. D. Pelletier  
and J. P. Field

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Velocity profiles can deviate from Eq. (1) close to the ground over rough terrain. As such, it is important to identify which sensors, if any, are located within the roughness sublayer prior to computing  $u_*$  and  $z_0$  values by fitting wind velocity data to Eq. (1). To do this, we plotted the average of all wind velocity measurements at each site as a function of  $\ln z$ . The results (described in Sect. 3.2) show that the lowest two (hotwire) sensors (located 0.10 and 0.035 m above the ground) at the three Death Valley sites and the rough Soda Lake site deviated noticeably from Eq. (1). The fact that these sensors were within the roughness sublayer is consistent with the fact that the height of the largest roughness elements at these sites is greater than or comparable to 0.035 m (the height of the second lowest sensor). Data from the lowest sensor at the next four smoothest sites (i.e. smooth Soda Lake, the two Willcox Playa sites, and the rough Lordsburg Playa site) also deviate noticeably from Eq. (1). Data from these sensors were not used in the calculation of  $u_*$  and  $z_0$  at those sites. In addition, we verified in all cases that the removal of these sensors deemed to be within the roughness sublayer improved the mean correlation coefficients,  $R^2$ , at each site. Only profiles with  $R^2$  values greater than 0.95 were retained.

### 2.3 Computational fluid dynamics

CFD modeling was used to quantify the effects of the amplitude and slope of sinusoidal microtopography on  $z_0$ . We used the 2013 version of the PHOENICS CFD model (Ludwig, 2011) to estimate the time-averaged wind velocities associated with neutrally stratified turbulent flow over sinusoidal topography with a range of amplitudes and slopes. PHOENICS uses a finite-volume scheme to solve simultaneously for the time-averaged pressure and flow velocity. PHOENICS solves the flow equations using the iterative SIMPLEST algorithm of Spalding (1980), which is a variant of the SIMPLE algorithm of Patankar and Spalding (1972). The solution was considered converged when the state variables changed by less than 0.001 % from one iteration to the next. We used the renormalization group variant of the  $k-\varepsilon$  closure scheme first proposed





$z_0$  value, fully taking into account microtopographic variations across a wide range of scales.

Within the implementation of the DFT in the IDL programming language, the amplitude of each Fourier mode is equal to 2 times the amplitude of the complex Fourier coefficient, i.e.  $a_n = 2|f_n|$ , and the maximum slope is given by  $S_n = 2\pi k a$ , where  $k$  is the natural wavenumber. As such, the generalization of Eq. (3) to multiscale topography as quantified using the DFT is

$$z_0 = z_{0g} + \sum_{n=1}^N z_{0n} \text{ where } z_{0n} = \frac{2c_4|f_n|}{1 + (c_2/|4\pi k f_n|)^{c_3}}. \quad (4)$$

where  $c_4$  is a unitless coefficient analogous to  $c_1$  but with a potentially different value, and  $k$  is the natural wavenumber defined as the inverse of the wavelength. We verified that Eq. (4) returns the same value of  $z_0$  as predicted by Eq. (3) for the case of a sinusoidal bed if  $c_4 = c_1$ . We also verified that the  $z_0$  values predicted by Eq. (4) were independent of the total number of data points and the sampling interval of the input data (provided that the dominant scales of roughness were represented and resolved). The best-fit value of  $c_4$  was obtained by a trial and error minimization of the least-squared difference between the predictions of Eq. (4) and the mean  $z_0$  values measured at the ten sites.

## 3 Results

### 3.1 TLS surveying

Figure 4 presents color maps of the topography of the roughest and smoothest sites at each playa. Table 1 presents summary statistics for the ten sites, including the topographic metrics  $H_{\text{RMSE}}$  and  $S_{\text{av}}$ .

Figure 5 plots the average amplitude spectrum of all 1-D topographic transects for each site. These spectra demonstrate that significant topographic variability exists at

## Predicting the roughness length of turbulent flows over landscapes

J. D. Pelletier  
and J. P. Field

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion











## Predicting the roughness length of turbulent flows over landscapes

J. D. Pelletier  
and J. P. Field

et al. (2014). For example, using Eq. (5) with  $H_{\text{RMSE}}$  values in the range of predicts  $z_0$  values in the range of 6–54 m, i.e. values larger than any value ever measured. Playa surfaces rarely, if ever, have  $H_{\text{RMSE}}$  values of 1–3 m, but many other landscapes (e.g. alluvial fans) do. Since the goal of this work is to use playas as model landscapes for understanding the multi-scale controls on  $z_0$  above landscapes in general (not playas specifically), it is necessary for any empirical equation to predict reasonable results for a broad range of landscape types and a range of spatial scales beyond the specific range considered in the model calibration. Second,  $H_{\text{RMSE}}$  values are problematic to use as the sole or dominant variable for predicting  $z_0$  values because they contain no information about terrain slope. A topographic transect with a point spacing of 0.01 m can be “stretched” to obtain any slope value, with importance consequences for flow separation and  $z_0$  values.

Figure 8b plots the relationship between mean  $z_0$  and  $S_{\text{av}}$ , the mean slope computed between adjacent points at the 0.01 m scale, for the ten study sites. This figure documents a systematic nonlinear relationship between  $z_0$  and  $S_{\text{av}}$ , suggesting that the nonlinearity between  $z_0$  and  $H_{\text{RMSE}}$  in Eq. (5) may reflect a dependence of  $z_0$  on  $S_{\text{av}}$  in addition to a dependence of  $z_0$  on  $H_{\text{RMSE}}$ . This hypothesis is consistent with Fig. 8c, which demonstrates that  $H_{\text{RMSE}}$  values are highly correlated with  $S_{\text{av}}$  values, i.e. that, in the playa surfaces we studied, playas with larger microtopographic amplitudes are systematically steeper. We would not expect such a correlation between amplitude and steepness to apply to all landform types because, as microtopography transitions into mesotopography and  $H_{\text{RMSE}}$  increase from 0.1 to 1 and higher, slope gradients do not continually steepen without bound. If our goal is to understand the controls on  $z_0$  values in landscapes generally, the data in Fig. 8 suggests that it is necessary to quantify the separate controls of amplitude and slope on  $z_0$  values. This was the purpose of the CFD modeling described in the next section.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



### 3.3 Computational fluid dynamics

Figure 9 presents color maps that illustrate the output of the CFD model for an example case ( $a = 0.05$  m and  $S = 0.79$  m/m). Figure 9a, which shows a color map of the turbulent kinetic energy, illustrates the growth of the internal boundary layer with increasing distance from the upwind boundary of the domain as the input velocity profile interacts with and adjusts to the presence of the microtopography. Figure 9b and c zooms in on the flow and illustrate the zones of flow separation that occur in this example. These figures also illustrate the terrain-following and logarithmically spaced nature of the computational grid in the vertical direction.

Figure 10 plots the  $z_0$  values computed from an analysis of the CFD-predicted wind profiles over sinusoidal topography for two different values of the sine-wave amplitude ( $a = 0.05$  and  $0.1$  m) and for a range of values of the maximum slope  $S$  from approximately 0.001 to 2.0. For maximum slope values less than approximately 0.004, the  $z_0$  value is equal to  $z_{0g}$ , as we would expect (the topography is effectively flat). As the slope of the microtopography increases, the wind field is increasingly perturbed by the roughness of the terrain. Eventually, flow separation is triggered and flow recirculation zones are created in the wakes of each bedform, further increasing  $z_0$  values. For very steep slopes, i.e.  $S \sim 0.4-1$ ,  $z_0$  values still increase with increasing slope but at a slower rate than for gentler slopes since the flow is already separated and additional steepening has only a modest effect on the spatial extent of flow separation and  $z_0$  values. The nonlinear dependence of  $z_0$  on  $S$  is well fit by a sigmoidal relationship of the form given by Eq. (3). Best-fit values are  $c_1 = 0.1$ ,  $c_2 = 0.4$ , and  $c_3 = 2.0$ .

### 3.4 Fourier analysis of topography and a multi-scale approach to quantifying $z_0$

Using a minimization of the squared difference between the mean measured values of  $z_0$  and the values predicted by Eq. (4) for all study sites, we found the optimal value of  $c_4$  to be 1.5. Figure 11 plots  $z_{0n}$  values computed by Eq. (4) as a function of the

## Predicting the roughness length of turbulent flows over landscapes

J. D. Pelletier  
and J. P. Field

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion





## Predicting the roughness length of turbulent flows over landscapes

J. D. Pelletier  
and J. P. Field

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



and the associated lee-side flow separation. Similarly, the value of  $c_2$  represents the maximum slope of the microtopography in which an increase in slope leads to a non-linear increase in  $z_0$  values. Above this slope value,  $z_0$  values increase more modestly with increasing slope because flow separation already occurs over a significant portion  
5 over the surface.

The approach of this paper is limited in that it applies the superposition principle to a problem for which it cannot apply precisely (superposition applies only to linear systems). The limited applicability of the superposition principle to this problem may be one reason why the value of the value of  $c_4$  is larger than  $c_1$ . If superposition were to apply  
10 exactly, we would expect Eq. (4) to be an exact Fourier-based implementation of Eq. (3) with the same values of the coefficients. Instead, we found that the best-fit value of  $c_4$  is approximately fifteen times larger than  $c_1$ . The high correlation coefficient between the model and data (obtained with just one free parameter) suggests that our approach is reasonable, but the difference between the values of  $c_1$  (the mono-scale case) and  $c_4$  (the multi-scale case) points to the limited applicability of the superposition principle in  
15 this case. Despite this limitation, we believe that our approach is a reasonable first step towards quantifying the multi-scale controls on  $z_0$  values until a more comprehensive and fully nonlinear approach is found.

We developed and tested a new empirical formula for the roughness length,  $z_0$ , of  
20 the fully rough form of the law of the wall that uses the amplitude and slope of microtopographic variations across multiple scales within a discrete-Fourier-transform-based approach. A sigmoidal relationship between  $z_0$  and the amplitude and slope of sinusoidal topography developed from CFD model results was used to quantify the effects of each scale of microtopography on  $z_0$ . The model was developed and tested using  
25 approximately sixty thousand  $z_0$  values from the southwestern US obtained over 2.5 orders of magnitude in distance above the bed. The proposed method is capable of predicting  $z_0$  values to 50 % accuracy, on average, across a four order-of-magnitude range. This approach adds to our understanding of and ability to predict the characteristics of turbulent boundary flows over landscapes with multi-scale roughness.

## Data availability

DEMS of each of the study sites (relative elevation in m) and mean wind velocities (in  $\text{m s}^{-1}$ ) measured at seven heights above the ground at 12 s intervals are available as Supplementary files.

5 **The Supplement related to this article is available online at doi:10.5194/15-1107-2015-supplement.**

*Acknowledgements.* This study was funded by award #W911NF-15-1-0002 of the Army Research Office. We thank the staff of Death Valley National Park for permission to conduct a portion of the work inside the park.

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## Predicting the roughness length of turbulent flows over landscapes

J. D. Pelletier  
and J. P. Field

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



## Predicting the roughness length of turbulent flows over landscapes

J. D. Pelletier  
and J. P. Field

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



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30

## Predicting the roughness length of turbulent flows over landscapes

J. D. Pelletier  
and J. P. Field

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



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## Predicting the roughness length of turbulent flows over landscapes

J. D. Pelletier  
and J. P. Field

**Table 1.** Study site locations and attributes.

Name	Latitude (° N)	Longitude (° W)	# profiles	$H_{\text{RMSE}}$ (mm)	$S_{\text{av}}$	mean $z_0$ (mm)	predicted $z_0$ (mm)
Death V. rough	36.34449	116.86338	8036	34	0.144	23	34
Death V. interm.	36.34466	116.86321	10 922	36	0.142	16	26
Death V. smooth	36.34485	116.86307	9457	26	0.122	6.3	10
Soda Lake rough	35.15845	116.10413	10 838	14	0.159	7.64	4.1
Soda Lake smooth	35.15852	116.10352	7134	11	0.154	4.6	2.8
Willcox rough	32.16882	109.88889	6404	6.6	0.056	0.26	0.22
Willcox smooth	32.14869	109.90317	2403	4.8	0.076	0.16	0.14
Lordsburg rough	32.28137	108.88378	1883	1.3	0.032	0.047	0.020
Lordsburg interm.	32.28105	108.88400	2569	0.72	0.017	0.002	0.0026
Lordsburg smooth	32.28097	108.88459	203	0.55	0.017	0.002	0.0025

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

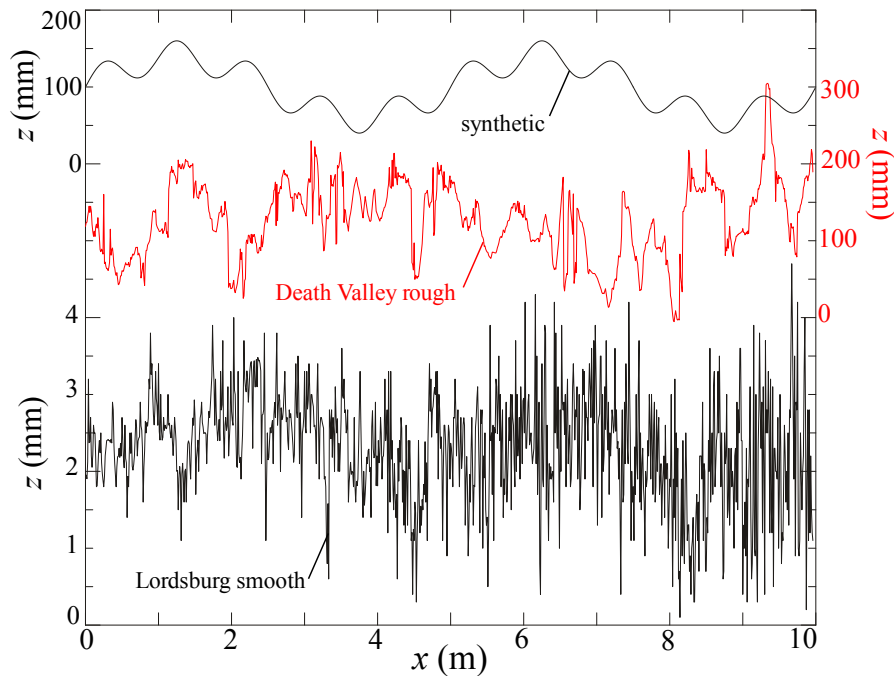
Interactive Discussion





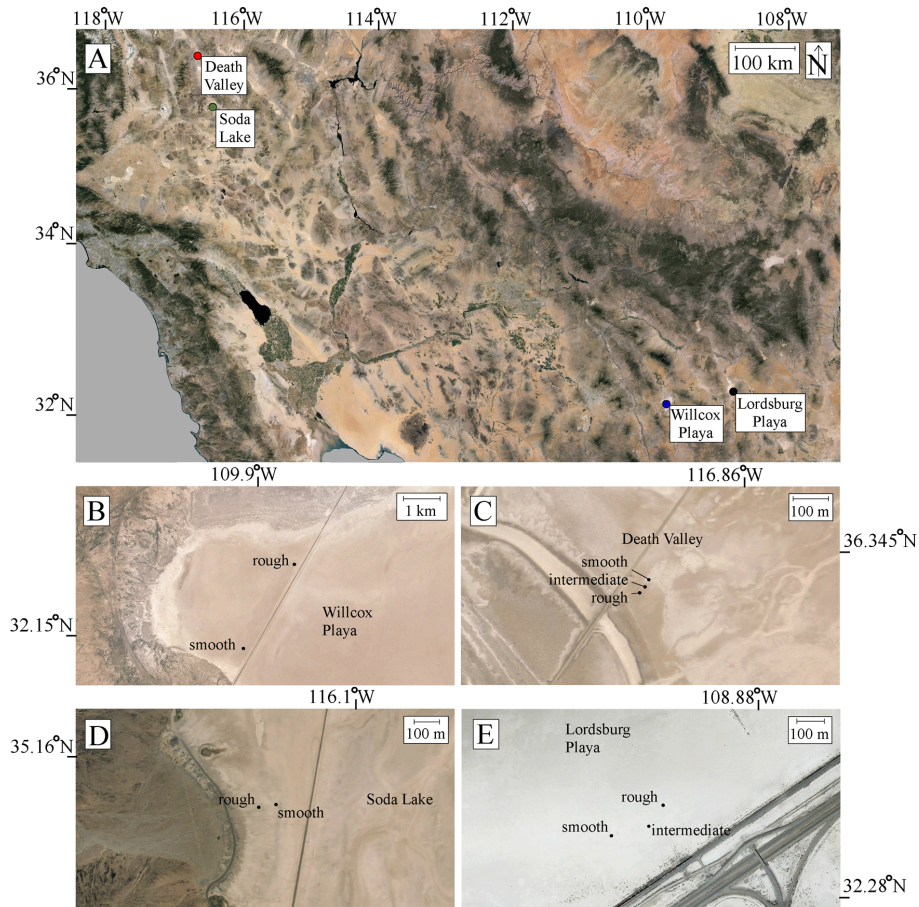
## Predicting the roughness length of turbulent flows over landscapes

J. D. Pelletier  
and J. P. Field



**Figure 1.** Plots of synthetic (top) and real (middle and bottom) topographic transects illustrating the multi-scale nature of topography using natural playa surfaces as examples.

[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[◀](#)[▶](#)[◀](#)[▶](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)



**Figure 2.** Aerial images of the study sites.

## Predicting the roughness length of turbulent flows over landscapes

J. D. Pelletier  
and J. P. Field

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

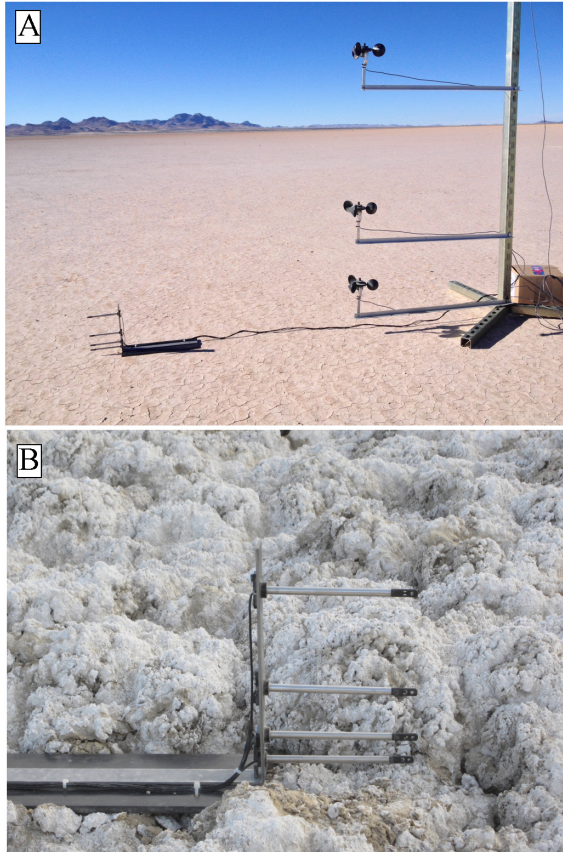
Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



**Figure 3.** Photographs of the equipment used for measuring wind profiles. **(a)** Mast holding 4 hot-wire anemometers (left) and four cup anemometers (right, note that only the lowest 3 are visible) at the Animas intermediate study site. **(b)** Close-up photograph of the hot-wire sensors at the Soda Lake smooth site. For scale, note that the top hot-wire sensor is located 0.16 m above the surface in both photographs.

## Predicting the roughness length of turbulent flows over landscapes

J. D. Pelletier  
and J. P. Field

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

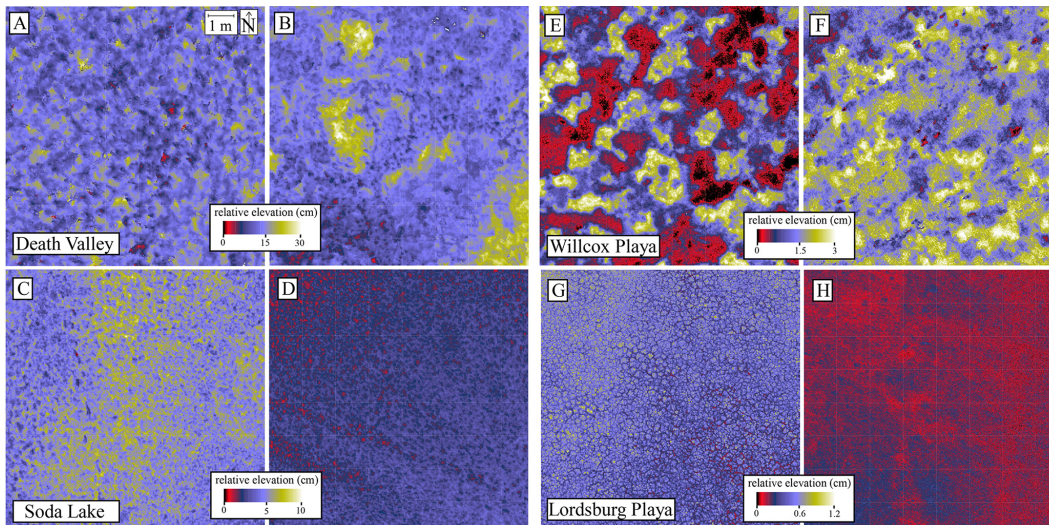
Printer-friendly Version

Interactive Discussion



## Predicting the roughness length of turbulent flows over landscapes

J. D. Pelletier  
and J. P. Field



**Figure 4.** Color maps of TLS-derived DEMs of eight of the ten study sites. **(a)** Death Valley rough, **(b)** Death Valley smooth, **(c)** Soda Lake rough, **(d)** Soda Lake smooth, **(e)** Willcox rough, **(f)** Willcox smooth, **(g)** Lordsburg rough, **(h)** Lordsburg smooth. Please note the differing color scales between **(a, b)**, **(c, d)**, **(e, f)**, and **(g, h)**.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

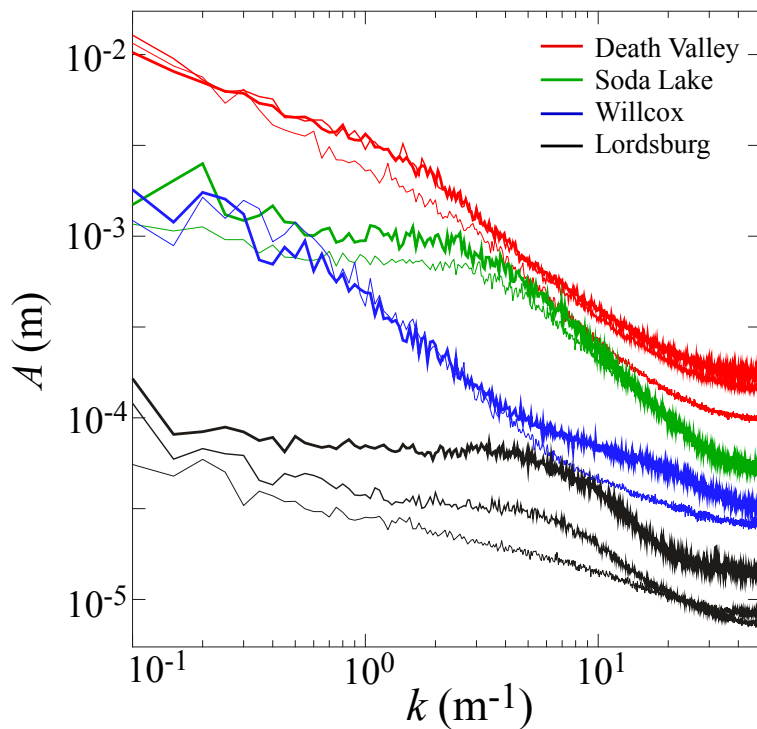
Full Screen / Esc

Printer-friendly Version

Interactive Discussion







**Figure 5.** Plots of the average amplitude spectrum,  $A$ , of 1-D transects of the microtopography of each site as a function of the natural wavenumber,  $k$ . The colors red, green, blue, and black are used to represent the Death Valley, Soda Lake, Willcox, and Lordsburg sites, respectively. Thicker curves represent rougher sites within each playa.

## Predicting the roughness length of turbulent flows over landscapes

J. D. Pelletier  
and J. P. Field

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

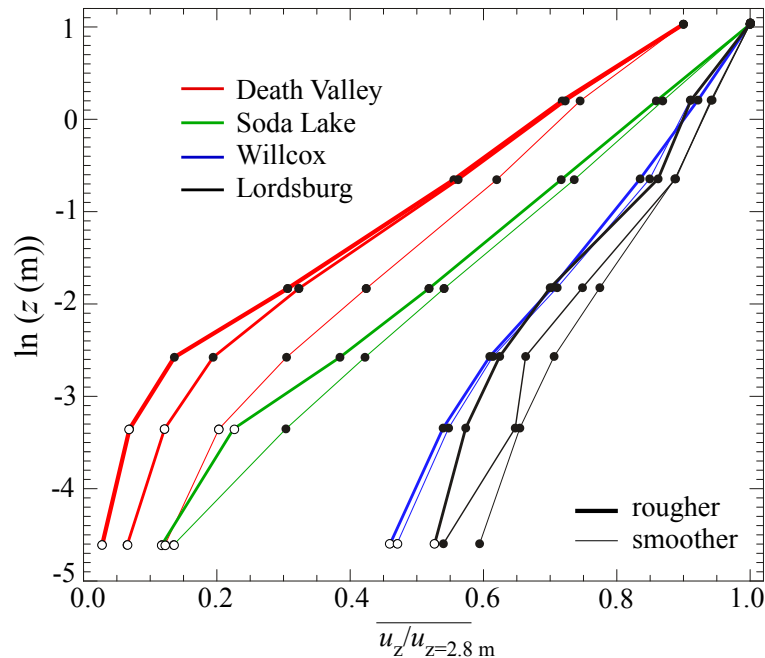
Printer-friendly Version

Interactive Discussion



## Predicting the roughness length of turbulent flows over landscapes

J. D. Pelletier  
and J. P. Field

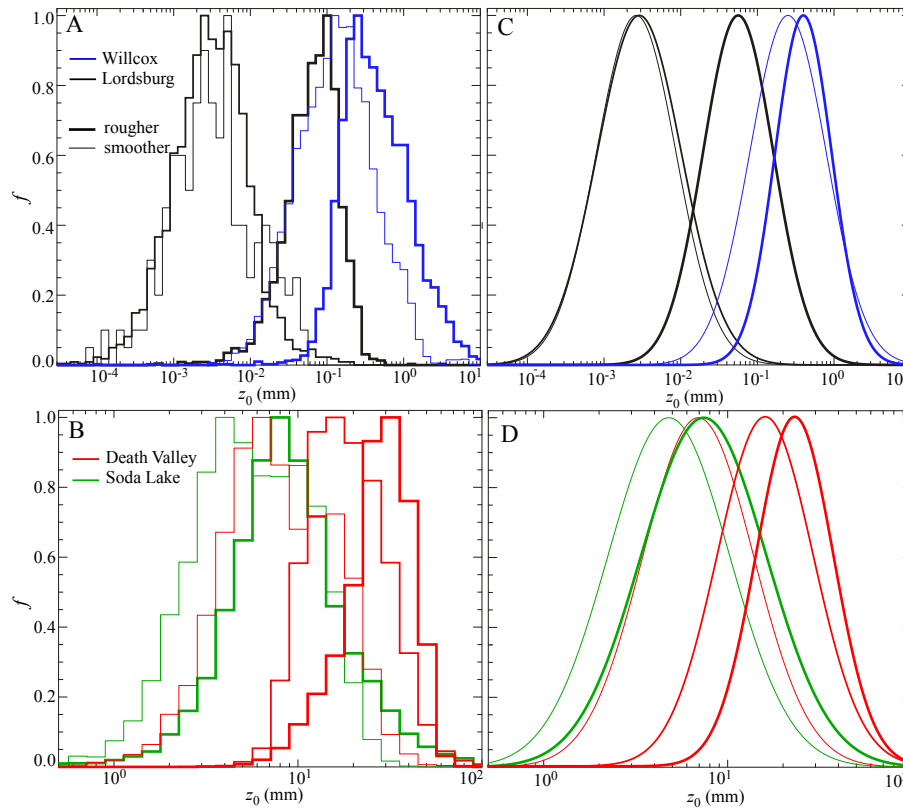


**Figure 6.** Plots of mean wind velocity (normalized by the velocity measured at the highest sensor, located 2.8 m above the ground) ( $x$  axis) as a function of the natural logarithm of height above the ground ( $y$  axis). The colors red, green, blue, and black are used to represent the Death Valley, Soda Lake, Willcox, and Lordsburg sites, respectively. Within each playa, thicker lines are used to represent the rougher sites. Open circles indicate stations located within the roughness sublayer. These sensors were not used to calculate  $z_0$ .

[Title Page](#)
[Abstract](#)
[Introduction](#)
[Conclusions](#)
[References](#)
[Tables](#)
[Figures](#)
[◀](#)
[▶](#)
[◀](#)
[▶](#)
[Back](#)
[Close](#)
[Full Screen / Esc](#)
[Printer-friendly Version](#)
[Interactive Discussion](#)

## Predicting the roughness length of turbulent flows over landscapes

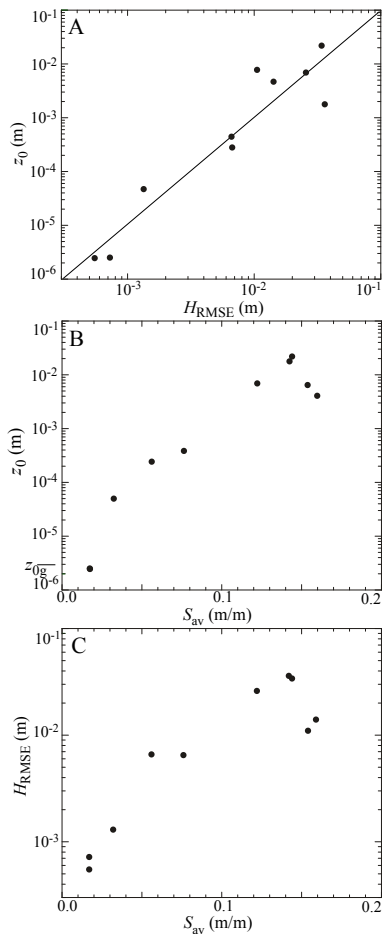
J. D. Pelletier  
and J. P. Field



**Figure 7.** (a, b) Normalized histograms of  $z_0$  values measured at each site and (c, d) probability distributions for each site, assuming  $z_0$  values are log-normally distributed.

## Predicting the roughness length of turbulent flows over landscapes

J. D. Pelletier  
and J. P. Field



**Figure 8.** Plots of mean  $z_0$  at each site vs. **(a)**  $H_{RMSE}$  and **(b)**  $S_{av}$ . **(c)** Plot of  $H_{RMSE}$  vs.  $S_{av}$ .

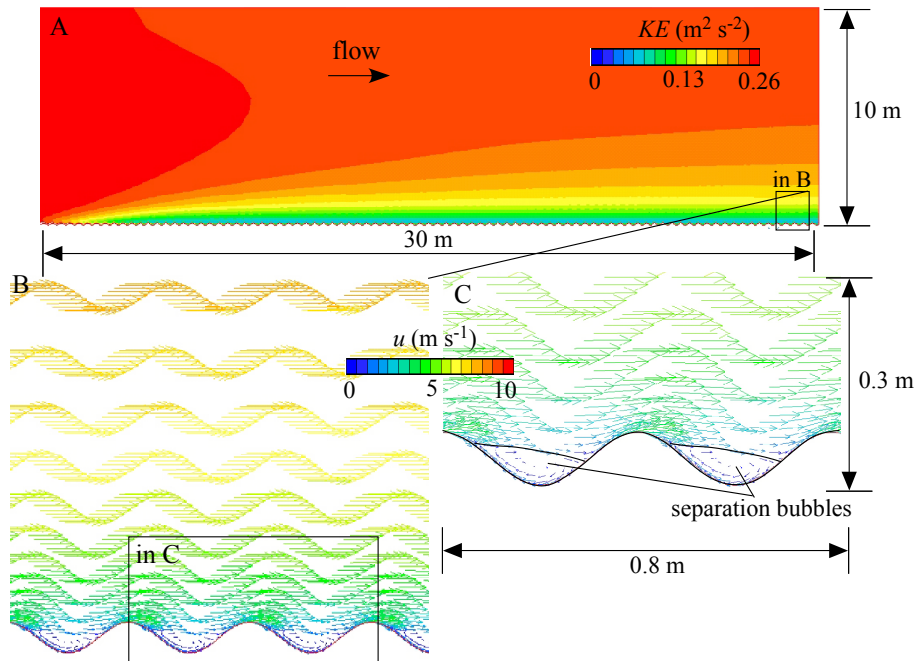
Title Page	
Abstract	Introduction
Conclusions	References
Tables	Figures
◀	▶
◀	▶
Back	Close
Full Screen / Esc	
Printer-friendly Version	
Interactive Discussion	





## Predicting the roughness length of turbulent flows over landscapes

J. D. Pelletier  
and J. P. Field

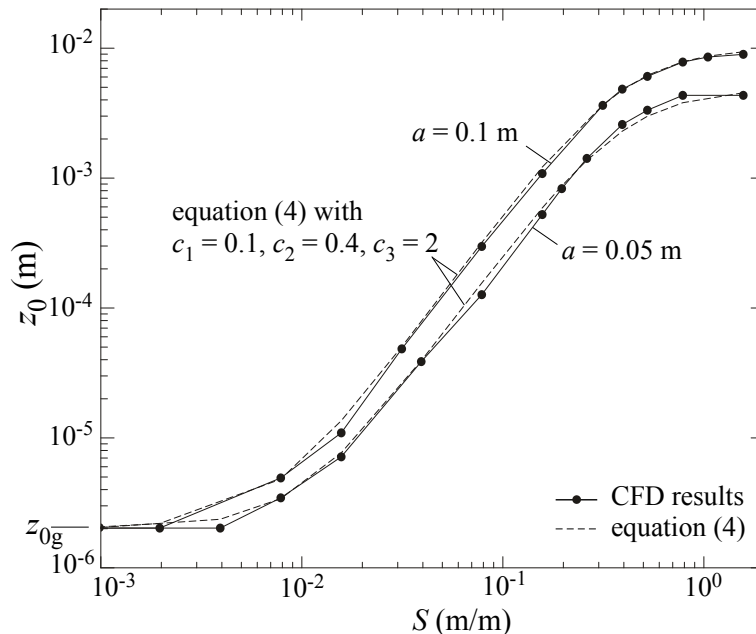


**Figure 9.** Illustrations of the output of the PHEONICS CFD model for the example case (with amplitude  $a = 0.05$  m and maximum slope  $S = 0.79$  m/m) of flow over a sinusoidal bed. **(a)** Color map of turbulent kinetic energy, KE. This map illustrates the growth of the internal boundary layer triggered by the effective roughness change as the input velocity profile (characterized by a grain-scale roughness  $z_{0g}$ ) interacts with and adjusts to the microtopography. The color vector maps in **(b)** and **(c)** illustrate the zones of flow recirculation that occur in the lee side of each bedform.

[Title Page](#)
[Abstract](#)
[Introduction](#)
[Conclusions](#)
[References](#)
[Tables](#)
[Figures](#)
[◀](#)
[▶](#)
[◀](#)
[▶](#)
[Back](#)
[Close](#)
[Full Screen / Esc](#)
[Printer-friendly Version](#)
[Interactive Discussion](#)

## Predicting the roughness length of turbulent flows over landscapes

J. D. Pelletier  
and J. P. Field



**Figure 10.** Plot of the  $z_0$  value predicted by the PHOENICS CFD model for flow over sinusoidal terrain with two values of the amplitude,  $a$ , and a wide range of values of the maximum slope values,  $S$ . Also shown are predictions of Eq. (3) for the best-fit parameter values.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

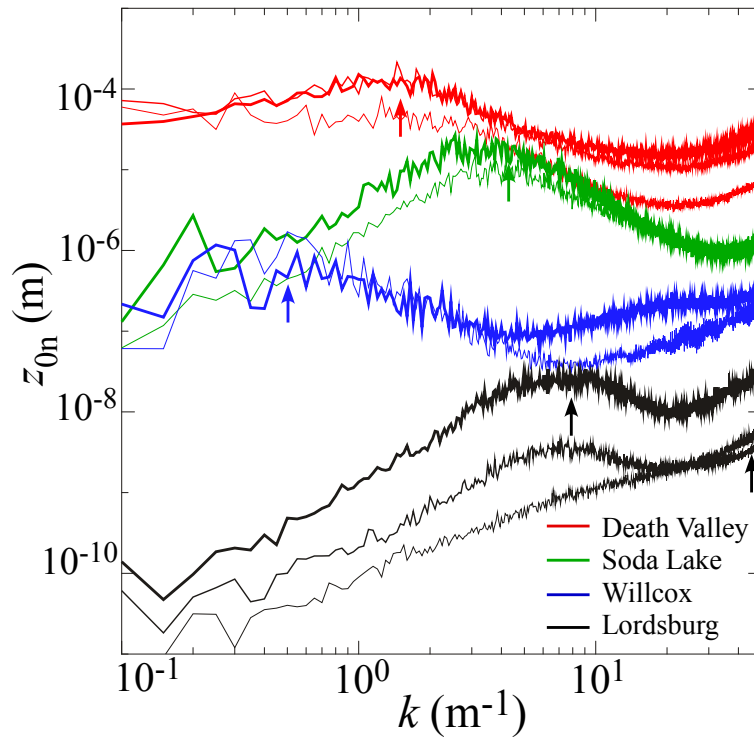
Printer-friendly Version

Interactive Discussion



## Predicting the roughness length of turbulent flows over landscapes

J. D. Pelletier  
and J. P. Field



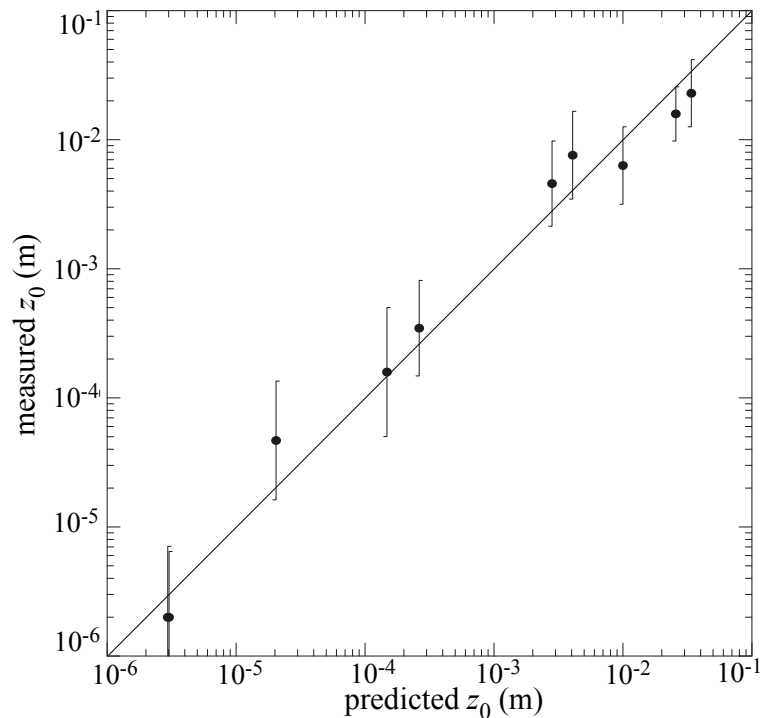
**Figure 11.** Plots of the contribution of each Fourier mode to the effective roughness length,  $z_{0n}$ , as a function of  $k$ . Arrows point to the range of wavenumbers that contribute most to  $z_0$ .

[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[◀](#)[▶](#)[◀](#)[▶](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

---

**Predicting the roughness length of turbulent flows over landscapes**J. D. Pelletier  
and J. P. Field

---



**Figure 12.** Plot of mean measured  $z_0$  values vs. predicted values (from Eq. 4) for the ten study sites. Error bars denote  $1\sigma$  variations in the measured  $z_0$  values.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

