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# Perspective – synthetic DEMs: a vital underpinning for the quantitative future of landform analysis?

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# Abstract

Physical processes, including anthropogenic feedbacks, sculpt planetary surfaces (e.g., Earth's). A fundamental tenet of Geomorphology is that the shapes created, when combined with other measurements, can be used to understand those processes. Artificial or synthetic Digital Elevation Models (DEMs) might be vital in progressing further with this endeavour. Morphological data, including metrics and mapping (manual and automated) are a key resource, but at present their quality is typically weakly constrained (e.g., by mapper inter-comparison). In addition to examining inaccuracies caused by noise, relatively rare examples illustrate how synthetic DEMs containing *a priori* known, idealised morphologies can be used perform "synthetic tests" to make strong "absolute" statements about landform detection and quantification; e.g., 84 % of valley heads in the real landscape are identified correctly. From our perspective, it is vital to verify such statistics as ultimately they link physics-driven models of processes to morphological observations, allowing quantitative hypotheses to be formulated and tested. Synthetic DEMs built by directly using governing equations that encapsulate

<sup>15</sup> tested. Synthetic DEMs built by directly using governing equations that encapsulate processes are another key part of forming this link. Thus, this note introduces synthetic tests and DEMs, then it outlines a typology of synthetic DEMs along with their benefits, challenges and future potential to provide constraints and insights. The aim is to discuss how we best proceed with uncertainty-aware landscape analysis to examine physical processes.

### 1 Introduction

Physical processes sculpt planetary surfaces such as the Earth's. A fundamental tenet of Geomorphology is that the form of the surface created, when combined with other data or modelling, can be used to understand those processes. Discrete "landforms" (cf. Evans, 2012) (e.g., craters, cirgues, drumlins, volcanoes) can be delimited with

<sup>25</sup> (cf. Evans, 2012) (e.g., craters, cirques, drumlins, volcanoes) can be delimited with a closed boundary and then isolated in order to quantify key characteristics such



as height *H* or slope of a flank (e.g., Hillier, 2008). Linear features (e.g., rivers) can also be measured. Equally, spatially continuous properties of Digital Elevation Models (DEMs) can be quantified (e.g., roughness, Wetness Index) (Beven and Kirkby, 1979; Grohmann et al., 2011; Eisank et al., 2014). Such morphology-derived observational data, including metrics from mapping that is both manual and automated, add to the

more qualitative assessments that may be drawn directly from geomorphological maps. Quantifying discrete landforms can give additional insights and provide constraints on models of physical processes. For example, discrete fluvial bedforms and their variability are quantified and used to predict extremes for engineering purposes (e.g., depth

- to place a pipeline) (van der Mark et al., 2008). Impact crater size-frequency distributions are used to estimate the age of the surface of the Moon and planetary bodies (e.g., Mars and Mercury) (e.g., Hartmann and Neukum, 2001; Ivanov, 2002). Similarly, size-frequency distributions of volcanoes have been used to examine how melt penetrates the tectonic plates (e.g., Wessel, 2001; Hillier and Watts, 2007). Aeolian dune formation can be constrained by their sizes (e.g., Duran, 2011; De et el., 2011).
- <sup>15</sup> formation can be constrained by their sizes (e.g., Duran, 2011; Bo et al., 2011). In sub-glacial geomorphology "flow-sets" of proximal bedforms thought to created by the same ice motion occur exponentially less often as their size increases (Fig. 1), which may indicate that the ice-sediment-water system beneath ice sheets is fundamentally random (Hillier et al., 2013).

Similar is true for linear features and spatially continuous measures. Channel geometry is measured to investigate the influences of tectonic or climatic landscape forcing (e.g., Brummer and Montgomery, 2003; Wohl, 2004), and channel networks identified to evaluate hydrological responses in floodplains (e.g., Cazorzi et al., 2013). Continuous measures such as curvature can arguably distinguish dominant geomorphic processes (e.g., diffusive vs. fluvial) (e.g., Tarolli and Dalla Fontana, 2009; Lashermes et al., 2007), and can be designed to detect the presence of anthropogenic features (e.g., agricultural terraces) (Sofia et al., 2014). They can also be used to estimate the probability of landsliding during rainstorms or for (semi-)automated geomorhological mapping (e.g., Tarolli and Tarboton, 2006; Milledge et al., 2009; Eisank et al., 2014).



Thus, such quantifications also have value for geomorphic understanding. Importantly, these examples illustrate how a robust, reproducible and quantitative approach can be used to develop our understanding of process.

Any enhanced use of landform observations, however, relies on us being able to trust what we have mapped or quantified. Specifically, the key question is; in terms of precision, accuracy and mapping completeness to what extent is it possible to trust the metrics derived from morphometric quantification of the landforms or surface recorded in the DEMs?

One way around this difficulty is to derive descriptive statistics that are as robust as possible to observational shortcomings (e.g., Hillier et al., 2013; Sofia et al., 2013; Tseng et al., 2015). Another solution is to assess the quality of the morphological mapping and quantification, perhaps either by an estimate of data completeness or quality (e.g., Hillier and Watts, 2007) or by traditional inter-comparisons between mappers (e.g., Podwysocki et al., 1975; Siegal, 1977; Smith and Clark, 2005) or techniques (e.g.,

- Sithole et al., 2004). The difficulty with robust statistics is that they will still be distorted if shortcomings are substantial (e.g., Hillier and Watts, 2004), and inter-comparisons can only ever yield relative levels of success and even complete agreement is inconclusive; all techniques, mappers, or techniques calibrated to mappers (e.g., Robb et al., 2015) may be systematically missing things (e.g., smaller features) (e.g., Eisank et al.,
- 20 2014; Hillier et al., 2014). Furthermore, it is simply not possible to calculate or estimate the magnitude of potential systematic biases within these approaches. An alternative is to verify each method or result against suitable features or properties known *a priori* within a suitably constructed test DEM. Thus designed landscapes, or "synthetic" DEMs, can give strong "absolute" answers (e.g., 84 % of valley heads in the real land-
- <sup>25</sup> scape are identified correctly), and may be vital in allowing us to proceed better with uncertainty-aware landscape analysis to examine physical processes.

Synthetic DEMs built by directly using postulated governing equations that encapsulate processes, or Landscape Evolution Models (LEMs) (e.g., Chase, 1992), are another key part of examining the form-process link. By altering their constants (e.g.,



rainfall, hillslope diffusivity) and mathematical construction they can give insights into the drivers and impacts of physical processes (e.g., Willgoose et al., 1991; Montgomery and Dietrich, 1994; Miyamoto and Sasaki, 1997). LEMs are, however, not yet the whole solution and to be securely compared to reality, equivalent landforms within both DEM types must still be robustly quantified, sometimes making calibration very difficult (De-Long et al., 2007).

This note introduces synthetic tests and DEMs, then it outlines a typology of synthetic DEMs along with their benefits, challenges and future potential to provide constraints and insights. Note that "virtual" and "artificial" are used interchangeably with "synthetic", as they are in the literature.

# 2 Synthetic tests and the potential uses of synthetic DEMs

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In fields such as geophysics it is standard to verify any method against its performance on some idealised or "synthetic" data. A well-documented example is the classic "synthetic checkerboard" test (e.g., Dziewonski et al., 1977, Saygin and Kennett, 2010) used in tomographic imaging of the Earth's interior. Broadly, there are four requisite stages for such a test based upon synthetic data (e.g., Nolet et al., 2007).

- 1. Construct a synthetic input including any features of interest (e.g., the morphology of a landform).
- 2. Create the synthetic data that resembles the observed data, for instance adding suitable noise.
- 3. Invert the synthetic data using the same numerical approach applied to the observed data.
- 4. Compare the inverted result with the synthetic input to see how well the assumed synthetic input (e.g., landform) is recovered.



The difficulty always lies in generating a suitable, statistically representative synthetic; in the case of geomorphology the task is to create an "appropriate" synthetic landscape or DEM that is realistic enough in the aspects under investigation.

- DEMs containing a synthetic component have been employed in "synthetic tests" to s assess approaches used to estimate the fractal dimension of topography (Malinverno, 1989; Rodriguez-Iturbe and Rinaldo, 1997; Tate, 1998a, b), slope and aspect (Zhou, 2004), land surface parameters (LSPs) (e.g., Wechsler, 2006; Sofia et al., 2013), and the reliability of DEMs (e.g., Fischer, 1998; Oksanen, 2010). Additionally, they have been used to evaluate how well some features (e.g., river networks, terraces) are identified (Pelletier, 2013; Sofia et al., 2014) and others (e.g., submarine volcanoes and 10 drumlins) are isolated in 3-D (i.e., their volumes explicitly delimited) (Wessel, 1998; Hillier, 2008; Kim and Wessel, 2008; Hillier and Smith, 2014). Synthetics have also been used to assess algorithms quantifying landscape processes such as flow-routing (e.g., Pelletier, 2010) and to give a first insight into how effective the manual mapping of glacial bedforms is (Hillier et al., 2014). Often, by including randomness (e.g., 15 in locations or noise) in a Monte Carlo approach multiple realisations of a landscape (e.g., n = 10 or 1000) are used to understand uncertainty and variability and more tightly constrain results (e.g., Heuvenlink, 1998; Raaflaub and Collins, 2006; Wechsler, 2006). The large (e.g., > 50 %) and systematic trends and biases that studies so far have uncovered indicates that the uses of synthetic tests in geomorphology should be, 20 arguably, similar in extent and function to the current use of inferential statistics; namely they are a demonstration that the observation claimed actually exists or method actually works. Some potential applications of synthetic tests in geomorphology can be
- Assessing the impact of "noise" (e.g., Sofia et al., 2013; Zhou and Liu, 2002, 2008) that could be instrumental, anthropogenic (e.g., houses) or natural (e.g., vegetation).

categorised as:



- Verifying that a geomorphic signature is actually characteristic of a particular landform type of interest, rather than other morphologies in a study area (e.g., Conway et al., 2011; Sofia et al., 2014).
- Quantifying extraction of features (e.g., completeness, reliability) (e.g., Hillier et al., 2014; Eisank et al., 2014), where the key advantage is that synthetics give "absolute" measures of accuracy simply not possible with traditional mapper intercomparisons (e.g., 62% of ribbed moraine can be detected).

- Assessing filtering or other techniques used to manipulate a DEM (e.g., Hillier and Smith, 2014), whose choice would otherwise be subjective.
- Evaluating the sensitivity of algorithms quantifying geomorphic processes to modelling assumptions (e.g., DEM resolution) (e.g., Pelletier, 2010).

Ultimately, the geomorphological intention is to use synthetic DEMs to examine more clearly the expression of physical processes. Rigor added to geomorphological observations through testing with synthetic DEMs will, we believe, ultimately link physics-<sup>15</sup> driven models of processes to morphological observations, allowing quantitative hypotheses to be formulated and tested. This is illustrated in Fig. 2, and described below. For a landform that it is not yet possible to create numerically from first mathematical principles, the challenge is to securely relate measured morphology and its variability within geographical areas to the driving process (e.g., tectonic uplift rate). The exam-<sup>20</sup> ple shown is that of relating drumlin sizes for each flow-set to characteristics of flow within an ice sheet (e.g., flow velocity) representative of the area of the flow-set. Statistical models can be formulated to link observations to numerical ice-sheet models

- or their outputs, but robustly determined observational metrics will be needed for such an inversion; i.e., synthetic tests are needed. If arguably realistic forms can be gen-
- erated directly by a physics-based model (e.g., Dunlop et al., 2008; Refince et al., 2012; Brown, 2015) creating a synthetic DEM, the link is more direct and the middle box may be omitted; the effects of various constants (e.g., rainfall), conditions and processes in the physical models on observables can be viewed and compared to reality



by the simple expedient of turning them off or amplifying them. Comparisons have been qualitative (e.g., Kaufman, 2001), but can provide more powerful insights if they apply consistent mapping or quantification procedures (e.g., Willgoose et al., 1994). Thus, creating a form-process link will still depend critically upon understanding any errors

or biases in landform morphometrics (e.g., in size-frequency distributions) for both the measured and generated landscapes; the appropriate metrics are better understood for some landforms than others, and it is only possible to assess their efficacy with tests involving synthetic DEMs. Furthermore, realistic models are likely to contain stochastic elements (e.g., Tucker et al., 2001), thus a statistical understanding may help to identity more effectively appropriate parameterizations for observations (e.g., Weibull) than

testing a variety of established distributions (e.g., van der Mark, 2008).

A final use of synthetic DEMs is examining "what if" engineering scenarios as they affect behaviours such as hydrological processes (e.g., Tarolli et al., 2015). This may be somewhat tangential, but imposing a proposed artificial geometry onto a measured

<sup>15</sup> DEM as a way of testing an artificial geometry to be created on the part of the Earth's surface is clearly a legitimate pursuit.

### 3 Synthetic DEMs

Synthetic DEMs are only useful if they can be constructed, and to be of most use their construction must be from or clearly identify "components" (e.g., a landforms layer). In

- <sup>20</sup> contrast to viewing a landscape as plan-view regions, height in DEMs can be described at any location (*x*, *y*) as the sum of *n* "components" (Eq. 1) (e.g., Wren, 1973; Wessel, 1998; Hillier and Smith, 2008), namely  $H_{\text{DEM}} = H_1 + H_2 + \dots + H_n$ . Conceptually, these components lie on top of each other, like geological strata, and extend across the entire DEM although they may have zero thickness for few or many parts of it.
- <sup>25</sup> For landform analysis the first component would typically be "noise" (e.g., DEM error, or surface "clutter" such as trees), the small-scale height variations not genetically related to the landform. A second component would be the landforms themselves, per-

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haps overlying a third component of larger-scale trends (e.g., 10 km wide smoothly undulating hills). However, in the limit, only one component is actually required, and how the components are constructed will vary depending upon the purpose of the synthetic DEM. Furthermore, the synthetic DEM might mix idealised, created components with real ones. Typically randomness is involved in the creation of statistical synthetics, and multiple realisations of landscapes may be created. The broad approaches to constructing synthetic DEMs are outlined in the typology below.

# 3.1 Simple and statistical

Perhaps the simplest synthetic DEMs are those constructed by using basic geometries
as building blocks such as cones, Gaussian functions, and planes or other surfaces defined by simple equations (e.g., Hodgson, 1995; Wessel, 1997; Jones, 1998; Kim and Wessel, 1998; Hillier, 2008; Pelletier, 2010; Qin et al., 2012); admittedly, some functions may be less simple (e.g., Pelletier, 2013). Typically, generalized shapes (e.g., 2-D Gaussian, rotated parabola) are formulated based upon visual or statistical fitting
of the functions to measured morphologies (e.g., Conway et al., 2011; Hillier and Smith, 2012; Pelletier, 2013) (Fig. 3).

These synthetics do not contain the complexity in the observed landscape, or necessarily have realistic statistical properties, but they have the advantages of being simple to construct and understand, and noise can be entirely omitted or modified with certainty in order to investigate data errors. They contain the key morphologies under investigation are perfectly sufficient for some tests; e.g., are approximately conical submarine volcanoes of variable size effectively isolated even when upon a slope? (Fig. 4). Statistically generated "noise" can be added to simple synthetic DEMs to assess the degradation caused (e.g., Zhou, 2004; Jordan and Watts, 2005), but for results to be

<sup>25</sup> meaningful its statistical distribution (e.g., Gaussian, uniform), length-scale of correlation, and any non-stationarity must be correct (e.g., Fischer, 1998; Sofia et al., 2013).

Whole landscapes can be generated statistically using fractals (e.g., Mandelbrot, 1983) or multi-fractals (Fig. 5a) (e.g., Gilbert, 1989; Schertzer and Lovejoy, 1989; Weis-



sel, 1994; Cheng, 1996), and these can be useful if the construction matches closely the element of reality being considered (e.g., uncorrelated, fractal in Swain and Kirby, 2003). Even multi-fractal landscapes, however, may not be an adequate representation without considering properties such as anisotropy (e.g., Gagon, 2006) and character<sup>5</sup> istic scales (e.g., Perron, 2008) if they are important in a particular circumstance. A limitation of these purely statistically generated, or statistically altered, DEMs for landform

analysis is that they do not explicitly contain spatially distinct, isolated features (i.e., landforms are not labelled as such during generation).

# 3.2 Landscape evolution models

- DEMs resembling real landscapes can also be created by the application of mathematical characterisations of physical processes in numerical models typically known as "Landscape Evolution Models" (LEMs) (Fig. 5b) (e.g., Chase, 1992; Braun and Sambridge, 1997). These now incorporate numerous processes (e.g., Tucker, 2010; Refice et al., 2012); for example, bedrock landslides (e.g., Densmore, 1998), flex-
- <sup>15</sup> ure of the lithosphere (e.g., Lane et al., 2008), and erosion by ice flow within valleys (e.g., Harbour, 1992; Brocklehurst and Wipple, 2004; Amundson and Iverson, 2006; Tomkin, 2009), including when this is thermo-mechanically coupled to ice sheets (e.g., Jamieson et al., 2008). Models of the evolution of single classes of feature (e.g., bedforms) and simpler 2-D configurations (i.e., *x-z* profiles) fall within this class of model
- (cf. Dunlop et al., 2008; Zhang et al., 2010; Brown et al., 2014). Simple geometries or measured landscapes may be used as an input (e.g., DeLong et al., 2007; Refice et al., 2012; Baartman et al., 2015; Hancock et al., 2015).

These models appear to be a perfect solution, however, there are some difficulties. The first difficulty is that it is not as yet possible to generate some landforms such as drumlins from first principles (e.g., Hindmarsh, 1998; Schoof, 2007), and it is not computationally practical to include certain processes, such as impact crater formation in the MARSSIM model (Howard, 2007); the simulation of rivers illustrates an area where there is progress, but also much to do (cf. Coulthard et al., 2013; Brown et al.,



2014). In general, a "perfect" unified model is still some way off. The second difficulty is that these models do not currently associate processes with a type of landform. For instance, a bedrock failure process is a bedrock failure process, not a bedrock failure process explicitly making a V-shaped valley. Equally, sediment is not tagged as making

- <sup>5</sup> a floodplain. So, the number and location of defined features are not known *a priori*. This can be seen as a strength of the models, but means that creating a secure link from process to landforms as observed in reality requires a step in which consistent mapping or quantification procedures are applied to both measured and simulated DEMs. This is not easy (e.g., DeLong, 2007). The lack of *a priori* features may also be
- the reason that, although LEMs have great potential to create DEMs for synthetic tests of landform mapping or extraction methodologies, we are not aware of this being done. Like simple or statistical synthetic DEMs, synthetics created by a LEM have the advantage of being free from errors associated with DEM measurement (e.g., instrumental, processing).

### 15 3.3 Complex geometrical

A possible class of synthetic DEM is one that uses simple or statistical building blocks, but constructed in a more complex fashion. For instance, multiple idealised shapes can be given additional observed attributes (e.g., spatial clustering, size-frequency realism) (e.g., Howard, 2007; Hillier and Smith, 2012), but such DEMs have so far contained other elements of realism as well, perhaps making them better described as hybrids.

### 3.4 Hybrid

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A "hybrid" class of synthetic DEM contains, for reasons of practicality, elements of the other classes. Typically, a morphology whose key properties cannot currently be readily simulated is either retained (e.g., most or all of a measured DEM), or an idealised but observationally constrained component is added (e.g., terraces (Sofia et al., 2014)), or



both. The spectrum of what is possible is illustrated by the, relatively rare, studies using hybrid synthetic DEMs in geomorphology.

A first example of a hybrid synthetic DEM is impact crater formation in the MARSSIM model (Howard, 2007). This evolution model does not dynamically model crater for-5 mation. Instead, randomly located craters are assigned shapes from a catalogue of measurements of individual fresh craters on Mars and given sizes from a power-law distribution. This introduces certain assumptions, such as the fresh craters being representative, but avoids complexity. A second example, deals with the quantification of glacial bedforms, illustrated with drumlins (Hillier and Smith, 2012, 2014; Hillier et al., 2014). It is the association of the bedforms with underlying trends (i.e., "hills") and 10 complex and spatially structured "noise" (e.g., trees, roads, houses) that makes the quantification difficult; they are not yet possible to simulate. The approach taken was therefore to circumvent this issue entirely by leaving the hills and noise as they were,

- and moving the drumlins such that they were randomly positioned with respect to these problems for identification (Fig. 6). Orientations and spatial density distribution (i.e., 15 number per km<sup>2</sup>) were preserved, as were the geometries (i.e., height-width-length triplets) of the 173 drumlins shuffled around. In these synthetics, the number and location of defined features are known a priori such that sizes and locations of mapped discrete landforms can be compared to synthetic ones directly. Similarly, but by assum-
- ing the highest-guality measured LiDAR DEMs were perfect, even if this is debatable, it 20 is possible to circumvent the need to generate statistically realistic landscapes when investigating DEM errors (Raaflaub and Collins, 2006; Sofia et al., 2013). Anthropogenic elements (e.g., open-cast mines, terraces) visually determined to be reasonable can also be added (e.g., Baartman et al., 2015), for instance to a 2-D multi-fractal statistical
- landscape (Sofia et al., 2104; Chen et al., 2015). 25

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# 4 Discussion

By providing an *a priori* known answer to test against synthetic DEMs, or DEMs containing a synthetic component, have some clear and powerful advantages in geomorphological analyses. They can be used to test errors, systematic or random biases, and
<sup>5</sup> unpick potential sources of misinterpretation. Furthermore, they give *absolute* answers (e.g., 47% of all actual drumlins *H* > 3 m are mapped) to questions about accuracy that are simply not obtainable by other means, and are often considered "objective". Through this they provide a route to answering key questions about geomorphic processes (e.g., Fig. 2). There are, however, complexities surrounding these statements,
<sup>10</sup> which are less commonly recognised. There are issues of objectivity, realism, circularity and the cost in time and effort of constructing synthetics.

Whilst the conclusions reached through the use of synthetics may be simplistically thought of as objective, it is more accurate to say that they are quantitative, reproducible, and are likely to be significantly less subjective. Without perfect, all-purpose

synthetics an element of subjectivity will remain in the choices made when designing the test DEM. Hillier and Smith (2012) illustrate some choices and a logical justification for them. Manually selecting data to test against (e.g., Sithole, 2004; Hillier and Watts, 2004) is faster in some circumstances, if more subjective. Reproducibility makes testing using synthetic DEMs superior to subjective visual verification, even if synthetic tests later indicate the visual estimate was a reasonable solution (Hillier and Smith, 2012, 2014). Pre-existing synthetic DEMs, however, are entirely objective means for

inter-comparison for future studies (e.g., Eisank et al., 2014).

A thorny question regarding synthetics is: how realistic is realistic enough? At one limit, it is notable that even extreme simplifications such as conical volcanoes can give

significant and useful first-order insights (e.g., Kim and Wessel, 2008; Tarolli et al., 2015). At the other limit, synthetic DEMs are not used as their applicability to real datasets is questioned (e.g., Robb et al., 2015). Lacking a perfect set of properties, however, should not be taken to invalidate tests using a synthetic DEM; in statistics for



instance, Student's t test underpinned by its idealized Gaussian distribution is widely used although observations are rarely perfectly Normal. A challenge then is to determine a generalised objective framework or workflow to assess the sufficiency of the realism of synthetic DEMs, but in its absence what can be done? Deficiencies can be

- visually identified. For instance, if spatial resolution is raised as an issue, it can either be matched to the observed data, or varied for a sensitivity test. If a particular statistical property is key, and perhaps how it varies across size-scales, it can be measured to ensure it is realistic in the synthetic. So, if a clearly stated set of properties argued to be most relevant to any given research task are faithfully reproduced in synthetics,
- we believe they will provide useful insights. Ultimately, however, practitioners within a peer-group must decide what is convincing, performing additional tests if necessary. For example, Hillier and Smith (2012) did not locally align neighbouring drumlins with each other, but participants the GMapping workshop (Hillier et al., 2014) felt that this was critical. Modified DEMs with this property included were therefore provided, altherearch is the englishing work is a second to be a second to
- though in the end this proved to be a minor effect. Similarly, highlighting that what must be captured well in a synthetic DEM may critically vary between studies, is that the impact of life (e.g., buildings, earthworks, trees, eco-geomorphic work by worms) may either be inconvenient "noise" (e.g., Hillier and Smith, 2012) or the morphology of interest (e.g., Dietrich and Perron, 2006).
- A more subtle potential issue is circularity. It is important to avoid basing aspects of a synthetic DEM on an assumption, and then using it to support the assumption. This is easily avoided in simple synthetic DEMs but a synthetic DEM based on a landscape evolution model, for instance, should not be later justified because a search algorithm trained on it finds only similar features in a real landscape; the algorithm might just be
- <sup>25</sup> missing things in the real landscape that differ from what it has been trained to detect. A similar issue was faced by Hillier and Smith (2012), but demonstrably avoided as the filter later found to be optimal was not the one initially assumed (Hillier and Smith, 2014).



So, subjectivity is reduced, even synthetic tests using basic DEMs can give some insight, and circularity can be avoided. On balance we argue that, if designed appropriately and used with appropriate care, tests using synthetic DEMs are worth the cost in time as they can be used to access results and insights of real significance and power. Exactly the same can be said for the application of statistical techniques, and so it seems reasonable to advocate the use of synthetic tests with similar strength.

By making observations more robust synthetic tests using synthetic DEMs containing *a priori* known landforms have the potential to strengthen the insights that can be gained through synthetic DEMs generated using physics-based numerical models,

- i.e. Landscape evolution models. LEMs can provide useful insights, but they are not the entire solution; firstly, they cannot model all processes yet, and secondly they are insufficient without synthetic tests to secure the observational part of the linkage between measured and generated DEMs. It is also worth noting that landscape evolution models are not the only route to creating a from-process link since the statistical work-
- around described also provides a quantitative means of establishing a form-process link even without a LEM. Thus, there are a number of valid types and specific uses of synthetic DEMs, but in combination we believe that they form a vital underpinning for the quantitative future of landform analysis.

#### 5 Conclusions

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- <sup>20</sup> From this discussion on the uses of synthetic digital landscapes (i.e., DEMs), or synthetic elements within them, the following overarching points can be drawn:
  - Synthetic DEMs can help to link physics-based models of processes to morphological observations, allowing quantitative hypotheses to be formulated and tested; importantly, this is not only through the use of landscape evolution models.



- By establishing "absolute" answers tests using synthetic DEMs containing a priori known landforms are a powerful tool with which to test and add rigor to geomorphological observations, and arguably should become as standard as statistical tests in geomorphology or synthetic test data in other arenas (e.g., Geophysics).
- A "perfect" synthetic DEM faithfully representing all aspects of an environment is likely impractical or impossible to create at present, but is not necessary.
  - Synthetic DEMs for tests may be easy and simple to construct, yet still provide valuable insights.
  - Synthetic tests using DEMs should be tailored to each research question, and their appropriateness to the key aspects of each inquiry (e.g., resolution, biases, and sensitivities) set out clearly and logically.

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**Figure 1.** Semi-logarithmic frequency plot of the lengths, *L*, of UK drumlins adapted from Hillier et al. (2013). Black dots are data digitised from Fig. 8 of Clark et al. (2009), with a bin width of  $\sim$  50 m. Red line is the exponential trend. Crosses indicate zero counts, placed at a nominal value of 1. Aspects of the curve are speculatively associated with processes, glacial or related to erosion and DEM construction.





**Figure 2.** Linking models and data, i.e., process to form. Where it is not yet possible to confidently generate realistic landforms from first principles statistical models, perhaps formalising conceptual ones, can be created to link geomorphological observations; an example of this are the continuing efforts to link drumlins to physical properties in numerical ice sheet models (cf. Hillier et al., 2013). If arguably realistic forms can be generated directly by the physical model (e.g., Dunlop et al., 2008; Brown et al., 2014), the link is more direct and the middle box might be omitted.





**Figure 3. (a)** HiRISE image of Zumba crater on Mars coloured according to elevation; HiRISE image DT2EA\_002118\_1510\_003608\_1510\_A01 and DEM DTEEC\_002118\_1510\_003608\_1510\_A01, credit NASA/JPL/UofA. (b) Radial elevation profile; blue shading illustrates the data distribution, black dots are averages within 50 m distance bins, and the red line is a parabolic fit to those points. (c) A synthetic crater created by rotating the parabolic equation, overlain by uncorrelated Gaussian noise and displayed as in (a).





**Figure 4. (a)** A simple 2-D (i.e., distance-height profile) synthetic seamount (grey shading) (Hillier, 2008), which following Kim and Wessel (2008) is conical with a radius of 3 km and summit height of 3 km above the surrounding seafloor. The thin black line is the synthetic topography, and the thick black line the filter's output. **(b)** A more demanding test of two, variably sized seamounts upon a sloping surface.





**Figure 5.** Comparison of simulated DEMs in (a) and (b) with LiDAR measurement of a real landscape in the South of Italy in (c). (a) Fractional Brownian motion (Mandelbrot, 1983); initial roughness of the surface = 0.2, initial elevation of the surface = 0.0, and change of roughness over change of terrain = 0.005. (b) A landscape model (Refice et al., 2012) that evolves through time a southward-dipping initial topography containing small-scale randomness, with all 4 boundaries closed except lower right corner. Simulated time is ~ 30 kyr and the run parameters are: tectonic uplift  $u_f = 1 \text{ mmyr}^{-1}$ ; diffusivity constant  $k_d = 0.2 \text{ m}^2 \text{ yr}^{-1}$ ; with channelling parameters of  $K_c = 10^{-4} \text{ m}^{(1-2 \text{ m})} \text{ yr}^{-1}$ , m = 0.5, and n = 1. Centroid in (c) is 14°37′59.46″ E, 40°43′25.80″ N.





**Figure 6.** Idealised distance-height profiles to illustrate the process used by Hillier and Smith (2012) to create synthetic DEMs. There are three "components". Drumlins, that are shaded dark grey, rise above a regional trend indicated by a dotted line. These are overprinted by "clutter" or "noise" shown in light grey. (a) In the process the upper and lower surfaces of the drumlin (X) are estimated to define it, and its height is subtracted from the measured DEM. (b) Two Gaussian shaped drumlins (Y and Z) are then inserted by adding their height to create the synthetic DEM.

