

Comments to the Author:

Review of Wang et al.

This paper contains a clear comparison of the chi and S-A methods for extracting information such as the channel steepness and concavity index from river profiles. The paper is timely since these two methods are being used in parallel and a comparison of their strengths yet to be performed in such detail. I ask for revisions as I am not quite prepared for this to be published; I believe there are some elements that could be improved and will hopefully increase the impact of the paper. The original AE was unable to continue handling the paper, and thus I have looked at this paper after the first round of revisions, so this does constitute a second round of review that the authors were not expecting. Hopefully the authors find my comments constructive. I have spent some time making editorial comments in order to improve the readability of the manuscript. In addition, I still feel the authors have missed a few relevant papers, although they have done a good job of addressing the comments relating to landscape transience and the papers cited by one of the referees. Referee 1 had three main comments. Firstly, they felt changes in concavity might have been caused by transience and suggested an inversion of the uplift rates from the channel profiles. The authors have done this to show there is only minimal evidence for transience in the studied catchments, and in addition cite previous work that suggests a low degree of transience. In chi space, the best fit concavity index, based on collinearity, tends to lead to concave channels (e.g., figs 10, 12 and 14). If the channels were all incising into spatially homogenous bedrock, and the uplift rate was spatially homogenous, this would suggest a slowing of uplift. This is seen in the inversion results, but is subtle. It is not really clear how the inversion might deal with changing transport processes: the authors suggest the change in concavity is due to alluviation rather than changing uplift rates, and thus represents a change from detachment to transport limited conditions. Overall, I feel the first two comments from this referee are addressed but I do feel the methodology could be clearer. In my lined comments below I make specific suggestions about where more detail is needed.

Referee #2 had further methodological questions. The authors have answered some of the comments but again I feel there is more scope for making their methods clearer. Again, I will suggest changes in my lined comments below. My recommendation is that the paper be accepted subject to revisions. I think there are some interesting and timely results here, but the paper could use some further edits to help readers understand what the authors have done. Since I am not calling for additional analysis, I will say these required revisions are minor.

Lined comments:

P1 line 8: Delete “one” after “former”. Also what are “deviated concavities”? I don’t see a discussion of this in the paper. It seems the concavity indices identified by the S-A method are similar to the ones determined by the chi method, but with higher uncertainties. I would just delete the phrase “and deviated concavities” from this sentence.

Thanks for the comment. We have deleted “one” and “and deviated concavities” and revised the sentence in Line 7-9 P1.

P1. Line 9: “False knickpoints”: again, I don’t see much discussion of this in the text. How is one more likely to find a “false knickpoint” using chi analysis vs S-A analysis? S-A analysis, done with intensive smoothing, might only pick up the largest knickpoints, but this isn’t discussed in the text. The main focus of the text is that the S-A method is better at identifying changes in concavity than the chi method. So why not write that in the abstract instead?

Thanks for the comment. We have revised the sentence as “The former is better at identifying changes in concavity indices but produces stream power parameters with higher uncertainties than the integral approach. The latter is much better for calculating channel steepness.” in Line 7-9 P1.

10 P1. Line 11: Delete “manage to”.

Thanks for the comment. We have deleted “manage to” in Line 12 P1.

P1, line 13: Add a sentence explaining why serial correlation of residuals is important to eliminate.

15 Thanks for the comment. We have add a sentence “In addition, we run bi-variant linear regression statistic tests for the two methods to examine and eliminate serially correlated residuals because they may bias both the estimated value and precision of stream power parameters.” to explain the importance of eliminating serial correlation of residuals in Line 12-14 P1.

P2, line 10: This section is not as clear as it should be. There is a very important point that belongs here and that the authors imply but do not state explicitly. The concavity index can change. In the S-A approach, the plots are simply data reflecting topography and the concavity index can be extracted from regression. This regression is subject to the noise of S-A data and the details of profile smoothing, but it is a reflection of data. The chi transformation, on the other hand, contains an assumption about concavity. Thus if a chi profile is used one must use some discriminatory technique to separate areas of different concavity: such a method has not, to my knowledge, been suggested. There are a number of suggestions for determining concavity of a river network using chi analysis but none for determining spatially varying concavities. In S-A analysis the concavity can be extracted directly from a regression of the data. This point is extremely important! I believe this point is what the authors wanted to highlight in the paper so it needs to be stated very, very clearly. S-A analysis is very noisy compared to chi analysis, so this property, that S-A analysis is a more direct measure of concavity, is really the main reason to continue using S-A analysis. The authors would do well to emphasize this point.

30 Thanks for the comment. We have revised the text as “Concavity changes with different channel substrate properties, which can be reflected and extracted from the slope-area data directly. Then, one can discriminate channel properties according to variable concavity indices.” (Line 10-11 P2) and “Nevertheless, the χ transformation contains an assumption of single concavity, which is distinctly different from slope-area analysis. In fact, concavity can change. In places where there is spatially varying concavities (because channels may go from bedrock to alluvial), the integral approach may show a break in the χ -z plot. Methods of separating areas of different concavities from a χ -z plot have not been suggested. Despite a very

noisy method compared to the integral approach, slope-area analysis is a more direct measure of concavity, which is the main reason to continue using it.” (Line 24-28 P2).

5 P2, line 10: I do suggest rewriting this section, as outlined above, but “for its need to estimate slope” is awkward and needs to be rewritten.

Thanks for the comment. We have revised the text as outlined above (Line10-11 and Line24-28, P2). We have rewritten the sentence as “However, estimates of slope obtained by differentiating and resampling noisy elevation data are even noisier.” In Line 13-14 P2.

10 P2 line 12-13: Awkward sentence. Rewrite to: “In addition, the derived channel steepness suffers from high uncertainty due to...”. Also Perron and Royden need to be re-cited here.

Thanks for the comment. We have rewritten the sentence as “In addition, the derived channel steepness suffers from high uncertainty due to error propagation (Perron and Royden, 2013)” in Line 16 P2.

15 P2 lines 19-21: This section needs some rewriting. Say “Thus, the chi method provides...”. Then the reason the uncertainty will be underestimated should be explained. Finally the last sentence (“false concavities and knickpoints”) needs to be rewritten into my suggestions stated above: because chi analysis is based on the assumption of a single concavity, in places where there is spatially varying concavities (because channels may go from bedrock to alluvial) the chi method may show a break in the chi-elevation profile that is spurious.

20 Thanks for the comment. We have revised the text as “the χ transformation contains an assumption of single concavity, which is distinctly different from slope-area analysis. In fact, concavity can change. In places where there is spatially varying concavities (because channels may go from bedrock to alluvial), the integral approach may show a break in the χ -z plot. Methods of separating areas of different concavities from a χ -z plot have not been suggested. Despite a very noisy method compared to the integral approach, slope-area analysis is a more direct measure of concavity, which is the main reason to continue using it.” in Line 24-28 P2.

25 We have explained the reason the uncertainty will be underestimated as “In addition, the uncertainty in k_s will be underestimated because the transformed profile (χ -z plot) is a continuous curve, and therefore the residuals of the linear fit are serially correlated (Perron and Royden, 2013).” in Line 28-30 P2.

30 P3 Line 1: say “is debris flow dominated and therefore will not display the typical fluvial scaling in Equaiton (1)” and then cite the Stock and Dietrich 2003 paper:

Stock, J., and W. E. Dietrich (2003), Valley incision by debris flows: Evidence of a topographic signature, Water Resour. Res., 39(4), 1089, doi:10.1029/2001WR001057.

Thanks for the comment. We have revised the text as “is debris flow dominated and therefore will not display the typical fluvial scaling in Eq. (1) (Stock and Dietrich, 2003)” in Line 10 P3.

5 P3 Line 3: the sentence ending in “scaling” needs a citation. The Whipple and Tucker 1999 paper might be appropriate here, or perhaps the 1994 willgoose paper:

Willgoose, G. (1994), A physical explanation for an observed area-slope-elevation relationship for catchments with declining relief, *Water Resour. Res.*, 30(2), 151–159, doi:10.1029/93WR01810.

Thanks for the comment. We have cited the papers (Whipple and Tucker, 1999; Willgoose, 1994) in Line 12 P3.

10 P3, line 5. Replace “could get” with “derive”.

Thanks for the comment. We have replaced “could get” with “derive” in Line 15 P3.

P3, line 7: This sentence is unclear. How exactly is the channel subject to lower uncertainties? You can restate that the chi analysis of the channel can be derived from the bedrock section that is suggested by the varying concavities in S-A space.

15 Thanks for the comment. We have revised the text as “the χ -z analysis of the channel can be derived from the bedrock section that is suggested by the varying concavities in slope-area space” in Line16-17 P3.

P3, Line 9: Here the authors say that the coupled process provides a better way to perform stream profile analysis. As I mention earlier, this has not been well demonstrated because the different advantages of the two methods have not been sufficiently highlighted in previous sections. Modification of the text earlier in the paper should fix this problem.

20 Thanks for the comment. We have sufficiently highlighted different advantages of the two methods in previous sections (Line 9-30 P2).

Page 3, Line 9: While it may be true that “little has been done” on the statistics of S-A or the integral method, there are some papers that investigate this topic that are strangely not cited here. In fact there is a paper with the title “A statistical framework to quantify spatial variation in channel gradients using the integral method of channel profile analysis” which I am familiar with because I wrote it! The entire purpose of that paper was to explore statistical ways to constrain channel steepness and m/n. So I cannot understand why that paper is not even mentioned.

25 Mudd, S. M., M. Attal, D. T. Milodowski, S. W. D. Grieve, and D. A. Valters (2014), A statistical framework to quantify spatial variation in channel gradients using the integral method of channel profile analysis, *J. Geophys. Res. Earth Surf.*, 119(2), 2013JF002981, doi:10.1002/2013JF002981.

30 As a historical note, our original version of that paper included calculation of the D-W statistic, but we found it did not yield information that was better than other tests. However, if you use our code that was released along with the 2014 paper you

will see that it still spits out the Durbin-Watson statistics for all chi analysis (https://csdms.colorado.edu/wiki/Model:Chi_analysis_tools).

Thanks for the comment. We are sorry for missing the paper. We have added the paper as “Mudd et al (2014) proposed a statistical framework to quantify spatial variation in channel gradients and calculated Durbin-Watson statistics in their code (https://csdms.colorado.edu/wiki/Model:Chi_analysis_tools).” in Line 24-25 P3.

P3, line 14: What I think is missing from this section is a clear description of why these statistical tests are necessary. I only think a few sentences are necessary but an explanation of the benefit of these statistics would help keep the attention of the reader.

10 Thanks for the comment. We have explained why these statistical tests are necessary in Line 20-27 P3. The text is as below:
The coupled process does provide a better way to perform stream profile analysis. Indeed, both the slope-area analysis and integral approach are bi-variant linear regression methods. Statistically, some tests must be done to meet two critical conditions, i.e. the residuals are independent and homoscedastic (Cantrell, 2008; Kirchner, 2001). Perron and Royden (2013) noticed that the precision in steepness derived from the integral approach would be overestimated due to auto-correlated
15 residuals. Mudd et al (2014) proposed a statistical framework to quantify spatial variation in channel gradients and calculated Durbin-Watson statistics in their code (https://csdms.colorado.edu/wiki/Model:Chi_analysis_tools). In this contribution, we find that auto-correlation of residuals can bias the regression coefficient, channel steepness (see details in Sect. 3). Therefore, not only theoretically but in practice, statistical tests are necessary for both the two methods.

20 P.3, line 16: The authors need to state if these tests are performed on the entire profile or only for the sections identified as bedrock using the S-A analysis.

Thanks for the comment. These tests are performed on the sections identified as bedrock using the slope-area analysis. (Line 29-30 P3)

25 P4, line 11: Again, an additional sentence or two is needed here to explain why these statistics are needed and useful.

Thanks for the comment. We have explained it in Line 20-27 P3.

P4, line 17: The Harkins et al is an excellent paper, but they do not present any evidence that chi and S-A methods produce the same results. To my knowledge, the first paper to actually compare the methods was the paper by Scherler et al (2014),
30 which should be cited here:

Scherler, D., B. Bookhagen, and M. R. Strecker (2014), Tectonic control on ^{10}Be -derived erosion rates in the Garhwal Himalaya, India, *J. Geophys. Res. Earth Surf.*, 119(2), 2013JF002955, doi:10.1002/2013JF002955.

Thanks for the comment. We have cited the paper in Line 6 P5.

P4, line 19: How was the dividing point determined? Was it done by eye or some other method? This needs to be explained. There are a number of ways to do this rigorously. I've done it with multiple segments in the Mudd et al. 2014 JGR-ES paper and we also used a 2 segment method for 1st order channels to find the area of the process transition in this paper:

- 5 Clubb, F. J., S. M. Mudd, D. T. Milodowski, M. D. Hurst, and L. J. Slater (2014), Objective extraction of channel heads from high-resolution topographic data, *Water Resour. Res.*, 50(5), 4283–4304, doi:10.1002/2013WR015167.

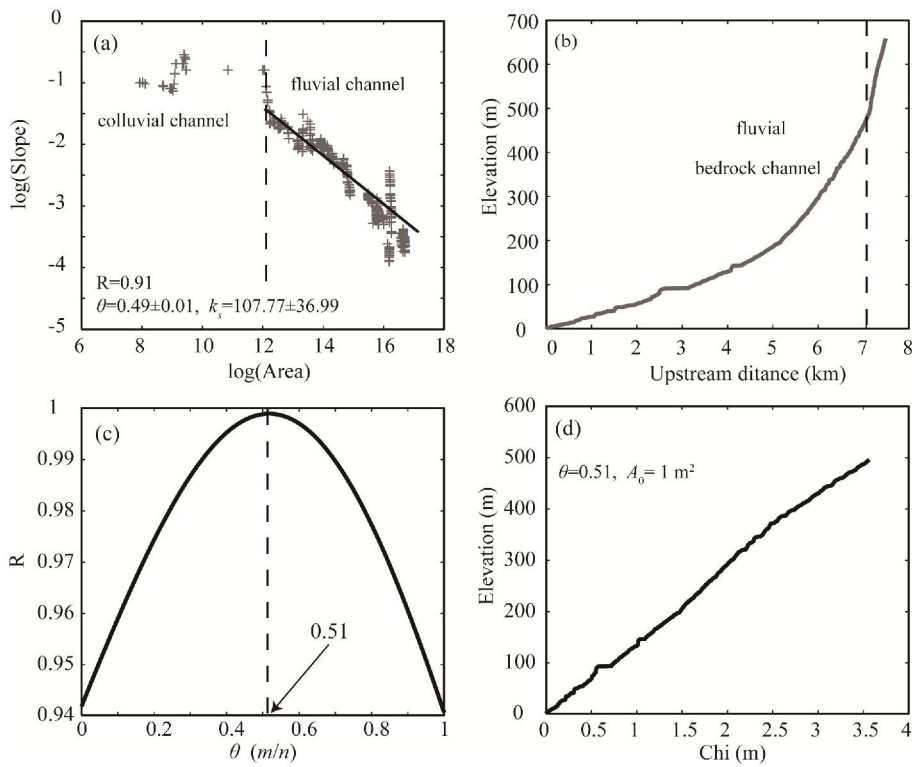
Thanks for the comment. We have explained it in Line 7-11 P5. The text is as below:

- 10 The area of process transition along a river profile can be determined by some rigorous methods. For example, Mudd et al (2014) worked on it with multiple segments and Clubb et al (2014) used a two-segment method for 1st order channels to find the area of process transition. Nevertheless, Fig. 3a shows a very simple log-transformed slope-area plot, from which the colluvial (nearly constant $\log(\text{slope}) \sim -1$) and fluvial (decreasing channel gradient) sections can be discriminated just by eye.

- 15 P4, line 23: The difference in the results between this paper and the Perron and Royden paper is curious. If you use the 10m DEM that they used do you get the same result they did? I note that a previous review has asked for such an analysis and it has not been performed. I now see that higher resolution data has been downloaded and analysed so it seems not too much work to report the results with higher resolution data.

- 20 Thanks for the comment. We use the 10m DEM for stream Cooskie and get two kinds of concavity values: 0.49 (slope-area analysis), and 0.51 (the integral approach) (see the figure as is shown below). These results are similar to Fig. 3 in our contribution (1Arc SRTM DEM is used) but different with Perron and Royden (2013). That's because we choose a tributary that is different to Perron.

There are many tributaries in the catchment Cooskie. The length of the tributary used by Perron is ~2.5 km (Fig. 1a in Perron and Royden (2013)), while that we used is longer than 7 km (Fig. 3b in our paper, or Fig b as is shown below). The stream used in our work is mapped in Fig. 1. Nevertheless, we do not know which tributary (in Cooskie catchment) was used in Perron and Royden (2013) because they did not show a map of the tributary they used.



5 Stream profile analysis of Cooskie. Elevation data are from 1/3 arc-second USGS DEM. (a) Log-transformed slope-area plot. The slope was derived from the smoothed (horizontal distance of 100m) and re-sampled (elevation interval of 10m) elevation data. (b) The full river profile (without any smoothing or re-sampling) of Cooskie. (c) The correlation coefficients, R , as a function of θ for least-squares regression based on Eq. (5). The maximum value of R , which corresponds to the best linear fit, occurs at $\theta=0.51$ (dotted line and black arrow). (d) χ -z plot of the bedrock channel profile, transformed according to Eq. (3) with $\theta=0.51$, $A_{cr}=0.1 \text{ km}^2$, and $A_0=1 \text{ m}^2$.

P4. Line 24: Delete “with each other”. Then later in the sentence you can say the “there are large uncertainties in channel steepness of approximately 40%. Also I think there should be a sentence saying how the uncertainty is computed.

10 Thanks for the comment. We have deleted “with each other”. The uncertainties are calculated by dividing the estimated value by error (see details in Line 17-18 P5). For example, the steepness value is $k_s=79.16\pm 29.35$. Then, the uncertainty is $(29.35/79.16) \sim 40\%$.

P4, line 30: This is an important result and I feel it should be stated in the abstract.

15 Thanks for the comment. We have stated in the abstract (Line 9 P1).

P5, line 3, 4: Again, how was this transition point identified? The method needs to be stated.

Thanks for the comment. We determine the transition point where channel concavity changes (from the log S-A plot). We have stated it in Line 7-11 and 26-26 P5.

P5, lines 13-15: These sentences could be clearer. Please rewrite.

- 5 Thanks for the comment. We have rewritten the sentences as “However, no knickpoint occurs on stream Juan because the river has been controlled by uniform rock uplift and under steady state (Snyder et al., 2000; see Sect. 4.2 for discussion). Thus, a χ -z plot generated by a single concavity will lead to misestimates in stream power parameters. We should recognize changes in concavities from slope-area space.” in Line 4-7 P6.

- 10 P5, lines 20-24: Again, there is a need for some text explaining why the D-W statistic and t statistics are useful. What are the implications of these tests?

Thanks for the comment. We have explained why the two statistic tests are useful. The texts are as below:

- (Line 16-22 P6) The uncertainties in steepness indices (revised by Durbin-Watson test) are about 2.4% - 9.9% (Fig. 8), which are much higher than those without statistical test (lower than 1%, Fig. 6). In addition to uncertainty estimate, auto-correlated residuals can also bias the regression coefficient, steepness. The channel steepness values of streams Fourmile, Kinsey and Hardy are 57.01, 103.90 and 58.78 $\text{m}^{0.9}$ (Fig. 6). While revised by Durbin-Watson test, these values are 36.33, 82.16 and 76.65 $\text{m}^{0.9}$, respectively (Fig. 8). Then, steepness varies about 25.6% - 58.3% (dividing the difference of the two kinds of steepness indices by the values revised by Durbin-Watson test). Due to such influence of auto-correlated residuals on both the estimated value and precision of steepness, Durbin-Watson test is necessary when applying the integral approach.
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- 20 (Line 25-26 P6) Despite no heteroscedasticity found in our study area, we suggest that Spearman rank correlation coefficient test should also be done because the test is a part of linear regression (statistically).

- p.6, line 3: Here is another chance for the authors to highlight why the S-A approach is useful even though they have shown that it gives highly uncertain channel steepness values. They need to reiterate here that S-A data makes no assumptions about m/n and therefore is more sensitive than chi analysis in detecting spatially varying concavities.
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Thanks for the comment. We have revised the text as “Even though it gives highly uncertain channel steepness values, slope-area plot makes no assumptions about θ and therefore is more sensitive than χ analysis in detecting spatially varying concavities.” in Line 2-3 P7.

- 30 P6, line 8-9: Awkward sentence. Rewrite.

Thanks for the comment. We have revised the text as “Perron and Royden (2013) considered that the uncertainty in channel concavity derived from a linear regression of the log-transformed slope–area plot described how precisely one can measure the slope of the plot, not how precisely the parameter is known for a given landscape.” in Line 9-11 P7.

P6, line 13: In the Mudd et al., 2014 paper we included an extensive discussion of selecting m/n based on the main stem vs the collinearity and I feel that paper should be cited here.

Thanks for the comment. We have cited the paper in Line 14 P7.

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P6, line 15: I suggest writing θ_{co} is the concavity from the collinearity test, and θ_{mR} is the concavity derived from averaging. Also, there should be some more detail as to how θ_{mR} is calculated: what, exactly, is being averaged?

Thanks for the comment. We have revised the text as “ θ_{co} (derived from the collinearity test) and θ_{mR} (from averaging the concavity values of all the streams within a catchment)” in line 17-18 P7.

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P6, line 30: It needs to be stated here if these results are based on all of the profile data or just the data that has been determined to be bedrock using S-A analysis.

Thanks for the comment. We have stated that these results are “for all of the profile data” in Line 1 P8.

15 Page 8, line 6: Replace “various” with “variable”. Do you mean “calculate”? This sentence doesn’t make sense, please check.

Thanks for the comment. We have revised the text as “We utilized variable erodibility ($K=U/k_{sn}$) values to calculate rock uplift rates.” in Line 8 P9.

20 P.8 Line 22: Add sentence explaining why this is the case.

Thanks for the comment. We have explained it as “Roberts et al (2012) noticed that the slope-area methodology might produce unstable results because small amounts of randomly distributed noise added to river profile will cause significant change in channel gradient.” in Line 24-25 P9.

25 P. 8 line 33: Unclear what is meant by “composited”. Rerword.

Thanks for the comment. We have revised the text as “slope-area data from all the streams within the same zone were composited.” in Line 2 P10.

30 P.9 line 10: This is an interesting result, but brings me back to the question of why your estimated concavity of the bedrock sections is so different from that estimated by Perron and Royden (2013); see comment on p4, line 23.

Thanks for the comment. We have explained it as “We do not deny that utilizing different datasets may cause some difference in parameter estimate for an individual catchment. For example, when using the integral approach, the resulting channel concavity of stream Cooskie is 0.45 (in Sect. 3) (1 arc-second SRTM DEM) but 0.36 in Perron and Royden (2013)

(1/3 arc-second USGS DEM). However, for averaging results (as done in Sect. 4.3), uncertainty in elevation data may not cause distinct differences in parameter estimates in this study area (e.g. θ and k_{sn})." in Line 12-16 P10.

P. 9, line 19: Say "The knickpoint is located at an elevation of..."

- 5 Thanks for the comment. We have revised the text as "The knickpoint is located at an elevation of ~280 m" in Line 25 P10.

P.9, line 24: replace "it" before "suggests" with "these steepness indices suggest".

Thanks for the comment. We have revised the text as "these steepness indices suggest that other variables" in Line 30 P10.

- 10 P.9, line 32: I don't feel the sentences starting with "thus" is supported. Why would you trust the S_A analysis more than the chi analysis when you have already shown that estimates of k_{sn} from S-A analysis are highly uncertain. I believe your results show that when the S-A analysis differs from the chi analysis it should be the chi analysis that should be trusted due to its lower uncertainties. Either explain or delete this sentence.

Thanks for the comment. We have deleted it.

- 15 We want to show that a river may be in disequilibrium condition despite a linear relationship in the χ -z plot. We have added sentences in Line 9-14 P11. The text is as below:

Both the slope-area data (Fig. 17b) and the χ -z plot based on a θ value derived from collinearity test (Fig. 18c) detect the unsteady signal (a knickpoint located at an elevation of ~280 m) on the trunk stream of the Mattole river, despite the best linearity for the integral approach (Fig. 17e). Then, we can find that a river may be in disequilibrium condition in spite of a

- 20 linear relationship in the χ -z plot. In some cases, uplift can be inserted along rivers, which makes values of χ difficult to interpret (Czarnota et al., 2014; Paul et al., 2014; Pritchard et al., 2009; Roberts and White, 2010; Roberts et al., 2012; Wilson et al., 2014).

P. 10 line 22: Does "Amanda" have a surname?

- 25 Thanks for the comment. We have added her surname as "Amanda McDowell" in Line 30 P11.

Coupling slope-area analysis, integral approach and statistic tests to steady state bedrock river profile analysis

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Abstract. Slope-area analysis and the integral approach both have been widely used in stream profile analysis. **The former is better at identifying changes in concavity indices but produces stream power parameters with higher uncertainties than the integral approach. The latter is much better for calculating channel steepness.** Limited work has been done to couple the advantages of the two methods and to remedy such drawbacks. Here we show the merit of the log-transformed slope-area plot to **determine changes in concavities and then to** identify colluvial, bedrock and alluvial channels along river profiles. Via the integral approach, **we obtain** bedrock channel concavity and steepness with high precision. In addition, we run bi-variant linear regression statistic tests for the two methods to examine and eliminate **serially correlated residuals because they may bias both the estimated value and precision of stream power parameters.** We finally suggest that, the coupled process, integrating the advantages of both slope-area analysis and the integral approach, can be a more robust and capable method for bedrock river profile analysis.

1 Introduction

In an evolving landscape, information about tectonics, climatic change, and lithology can be recorded by the bedrock river profiles (Fox et al., 2014, 2015; Goren et al., 2014; Harkins et al., 2007; Royden and Perron, 2013; Snyder et al., 2000). How to retrieve such details has long been a focus in both geologic and geomorphologic researches (Flint, 1974; Wobus et al., 2006; Rudge et al., 2015). Most of these studies are based on a well known power-law relationship between local channel gradient and drainage area (Flint, 1974; Hack, 1973; Howard and Kerby, 1983):

$$\frac{dz}{dx} = k_s A^{-\theta} \quad (1)$$

$$k_s = (U/K)^{1/n} \quad (2)$$

$$\theta = m/n \quad (3)$$

where z is elevation, x is horizontal upstream distance, U is bedrock uplift rate, K is an erodibility coefficient, A is drainage area, and m and n are constants. Parameters θ and k_s are referred to as concavity and steepness indices, respectively. The power-law scaling holds only for drainage areas above a critical threshold, A_{cr} , which is the transition from divergent to

convergent topography or from debris-flow to fluvial processes (Montgomery and Foufoula-Georgiou, 1993; Tarboton et al., 1989; Wobus et al., 2006). A growing number of studies have quantitatively related steepness to rock uplift (Hu et al., 2010; Kirby and Whipple, 2012; Kirby et al., 2003, 2007; Tarboton et al., 1989). Assuming a steady state river profile under constant rock uplift rates and erodibility in time and space, two forms of solutions to Eq. (1) are derived:

$$5 \quad \log\left(\frac{U}{K}\right)^{1/n} + \left(-\frac{m}{n}\right)\log A = \log\left(\frac{dz}{dx}\right) \quad (4)$$

$$z = z_b + \left(\frac{U}{KA_0^m}\right)^{1/n}\chi \quad (5)$$

$$\chi = \int_0^x \left(\frac{A_0}{A(x')}\right)^{m/n} dx' \quad (6)$$

where z_b is the channel elevation at $x=0$ (river outlet). This is a boundary condition to Eq. (1). A_0 is an area-scale factor.

The slope-area analysis, as shown in Eq. (4), yields concavity and steepness indices by a linear fit to the log-transformed slope-area plot. Concavity changes with different channel substrate properties, which can be reflected and extracted from the slope-area data directly. Then, one can discriminate channel properties according to variable concavity indices. For example, available studies indicate that the colluvial, bedrock and alluvial channels can be directly identified from the log-transformed slope-area plot (Kirby et al., 2007; Snyder et al., 2000, 2003; Wobus et al., 2006). However, estimates of slope obtained by differentiating and resampling noisy elevation data are even noisier (Perron and Royden, 2013). Then, considerable scatter will be typically caused in slope-area plots, making it challenging to identify a power-law trend with adequate certainty (Perron and Royden, 2013). In addition, the derived channel steepness suffers from high uncertainty due to error propagation (Perron and Royden, 2013; see Sect. 3 for details).

The integral approach, based on an integration of Eq. (1), was proposed by Royden et al (2000) to alleviate such problems by avoiding calculating channel slope. As shown in Eqs. (5) and (6), the transformed variable χ can be determined directly from drainage area data by simple numerical integration. Based on a proper concavity, the steady state river profile can be converted into a straight line. Slope of the line is steepness (we assume $A_0=1 \text{ m}^2$ throughout the paper). As the best fit value of θ is not known a priori, we can compute χ - z plots for a range of θ values and test for linearity (Perron and Royden, 2013). Thus, the integral method provides an independent constraint on both θ and k_s (Perron and Royden, 2013). Nevertheless, the χ transformation contains an assumption of a single concavity, which is distinctly different from slope-area analysis. In fact, concavity can change. In places where there is spatially varying concavities (because channels may go from bedrock to alluvial), the integral approach may show a break in the χ - z plot. Methods of separating areas of different concavities from a χ - z plot have not been suggested. Despite a very noisy method compared to the integral approach, slope-area analysis is a more direct measure of concavity, which is the main reason to continue using it. In addition, the uncertainty in k_s will be underestimated because the transformed profile (χ - z plot) is a continuous curve, and therefore the residuals of the linear fit are serially correlated (Perron and Royden, 2013).

Based on the analysis above, coupling the advantages of the two methods can make up for their individual drawbacks and provide a better way to constrain stream power parameters. We also run bivariate linear regression statistic tests for the two methods to evaluate if the residuals of linear fit are homoscedastic and serially correlated. In this paper, we take streams, located in the Mendocino Triple Junction (MTJ) region of northern California (Fig.1), for example, to illustrate the process.

5 2 Methods

2.1 Coupling slope-area analysis and the integral approach

A natural river usually consists of different channel substrates, for example, colluvial, bedrock and alluvial channels. In spite of their complex formation processes, we can identify them from a log-transformed slope-area plot (Fig. 1) (Snyder et al., 2000). The colluvial channel, characterized by steep channel slope ($>20^\circ$) and limited drainage area ($<A_{cr}$) (Wobus et al., 2006), is debris flow dominated and therefore will not display the typical fluvial scaling in Eq. (1) (Stock and Dietrich, 2003). Both bedrock (detachment-limited) and alluvial (transport-limited) channels show descending gradient with increasing drainage areas, which often exhibit a power-law scaling (Whipple and Tucker, 1999; Willgoose, 1994). However, the alluvial channel is often characterized by much gentler gradient and a higher concavity (Kirby et al., 2007; Snyder et al., 2000; Whipple and Tucker, 2002), which can be distinguished in the log-transformed plot (Fig. 1).

15 Via the integral approach (Perron and Royden, 2013), we derive concavities of bedrock channels. Based on a reference concavity index (Hu et al., 2010; Kirby et al., 2003, 2007; Perron and Royden et al., 2013; Snyder et al., 2000; Wobus et al., 2006), the χ -z analysis of the channel can be derived from the bedrock section that is suggested by the varying concavities in slope-area space.

2.2 Statistic tests

20 The coupled process does provide a better way to perform stream profile analysis. Indeed, both the slope-area analysis and integral approach are bi-variant linear regression methods. Statistically, some tests must be done to meet two critical conditions, i.e. the residuals are independent and homoscedastic (Cantrell, 2008; Kirchner, 2001). Perron and Royden (2013) noticed that the precision in steepness derived from the integral approach would be overestimated due to auto-correlated residuals. Mudd et al (2014) proposed a statistical framework to quantify spatial variation in channel gradients and calculated Durbin-Watson statistics in their code (https://csdms.colorado.edu/wiki/Model:Chi_analysis_tools). In this contribution, we find that auto-correlation of residuals may bias the regression coefficient, channel steepness (see details in Sect. 3). Therefore, not only theoretically but in practice, statistical tests are necessary for both the two methods. Here, we introduce Durbin-Watson test (Durbin and Watson, 1950) and Spearman rank correlation coefficient test (Choi, 1977; Fieller et al., 1957; York, 1968) to examine if the residuals are independent and homoscedastic. These tests are performed on the sections identified as bedrock using the slope-area analysis.

30

2.2.1 Durbin-Watson test

We took the integral approach for an example and rewrote Eq. (5) into another form:

$$z_i = z_b + k_s \chi_i + e_i \quad (i = 1, 2 \dots p) \quad (7)$$

In the formula, p is the number of elevation data points, and e represents residuals. We determined the Durbin-Watson (DW) statistics in the following steps:

1) We first calculated the self-correlation coefficient of residuals via Eq. (8):

$$r = \frac{\sum_{i=2}^p e_i e_{i-1}}{\sqrt{\sum_{i=2}^p e_i^2} \sqrt{\sum_{i=2}^p e_{i-1}^2}}, \quad (8)$$

2) Then, the DW statistic was derived as: $DW=2 \times (1-r)$. Since $-1 \leq r \leq 1$, DW falls in the range of 0-4.

3) We then examined if the residuals were auto-correlated according to Table 1.

10 To eliminate the self-correlation, new variables were generated as Eq. (9):

$$z'_i = z_i - r z_{i-1}, \quad \chi'_i = \chi_i - r \chi_{i-1} \quad (i = 1, 2 \dots p), \quad (9)$$

Slope of a linear fit to revised relative elevation, z' , and χ' data are channel steepness.

2.2.2 Spearman rank correlation coefficient test

To evaluate if the variance of residuals is a constant, we utilized Spearman rank correlation coefficient test (Choi, 1977; York, 1968):

1) Via a linear regression of χ - z plots, we derived the absolute values of residuals $|e|$;

2) We sorted the χ values in descending order and recorded the ranks d_{i-1} . Then the χ values were sorted again according to $|e|$ and the new ranks were recorded as d_{i-2} ;

3) The Spearman rank correlation coefficient, rs , and the t-statistics, t , were calculated via Eqs. (10) and (11):

$$20 \quad rs = 1 - \frac{6}{p(p^2-1)} \sum_{i=1}^p (d_{i-1} - d_{i-2})^2 \quad (10)$$

$$t = \frac{\sqrt{p-2}}{\sqrt{1-rs^2}} rs \quad (i = 1, 2 \dots p) \quad (11)$$

4) When the t value is lower than a threshold, $t_{\alpha/2}(p-2)$, the variance of residuals is a constant. In our example, with $p > 30$ and significance level $\alpha = 0.05$, the threshold value is larger than 2.58.

3 Case study: Mendocino Triple Junction (MTJ) region

Based on 1 arc-second SRTM DEM (digital elevation model), we extracted 15 streams in Mendocino Triple Junction (MTJ) region (Fig. 2). Here we first took streams Cooskie and Juan, for example, to illustrate the advantages and disadvantages of slope-area analysis and the integral approach, as well as to explain the reason of coupling the two methods.

5 Channel concavity and steepness indices can be derived from either slope-area analysis or the integral approach. For the same river profile, both methods should yield identical results (Scherler et al., 2014). We divided the profile of Cooskie stream into colluvial and bedrock channels from the log-transformed slope-area plot (Fig. 3a). The area of process transition along a river profile can be determined by some rigorous methods. For example, Mudd et al (2014) worked on it with multiple segments and Clubb et al (2014) used a two-segment method for 1st order channels to find the area of process transition. Nevertheless, Fig. 3a shows a very simple log-transformed slope-area plot, from which the colluvial (nearly constant $\log(\text{slope}) \sim -1$) and fluvial (decreasing channel gradient) sections can be discriminated just by eye. The elevation and area of the dividing point are ~ 500 m (Fig. 3b) and 0.1 km^2 (critical area, A_{cr}). The concavity of bedrock channel is $\sim 0.47 \pm 0.05$. We also computed the correlation coefficients between bedrock channel elevation and χ values based on a range of θ values. The best linear fit corresponds to $\theta = 0.45$. Both of them are similar to the result (0.43 ± 0.12) of Snyder et al (2000), but slightly higher than the result (0.36) of Perron and Royden (2013), which may be attributed to the difference in DEM resolution or choosing different critical areas.

Although the concavities derived from the two methods are in agreement, uncertainties (dividing the estimated value by error) in channel steepness differ a lot. The uncertainty from slope-area analysis is $\sim 40\%$ ($k_s = 79.16 \pm 29.35$) (Fig. 3a), but the integral approach gives only $\sim 0.5\%$ ($k_s = 62.81 \pm 0.39$) (Fig. 3d). In addition to smoothing and re-sampling of elevation data, we attribute such large uncertainty to error propagation. The natural logarithmic value of steepness from slope-area analysis is 4.37 ± 0.37 , which results in a k_s value of 79.16 ± 29.35 . This indicates that the steepness indices will have large uncertainties even for high linear correlation of the log-transformed slope-area plot. Hence, the integral approach is much better for calculating channel steepness.

Concavity indices usually vary along river channels where different substrates outcrop (e.g. alluvium, and bedrock). For example, along the Juan River, we identified colluvial ($\log(\text{slope}) \sim -1$, drainage area $< 0.16 \text{ km}^2$, elevation > 700 m), bedrock (decreasing channel gradient) and alluvial (channel slope decreases in a much higher concavity, drainage area $> 8.89 \text{ km}^2$, elevation < 150 m) channels from the log-transformed slope-area plot for their variable concavities (Figs. 4a and b). As shown in Fig. 4a, these channels are characterized by different concavities, consistent with estimates from Snyder et al (2000). According to the concavity of the bedrock portion of the river ($\theta = 0.52$, derived from the integral approach, Fig. 4c), the bedrock channel profile is converted into a straight line (Fig. 4d).

Nevertheless, for the integral approach, it is difficult to recognize bedrock and alluvial channels along a river profile. When computing χ -z plots ($A_{cr} = 0.16 \text{ km}^2$, for the whole fluvial channel including both bedrock and alluvial portions) based on a series of concavity values, the best fit θ is 0.72 (Fig. 4e). As shown by the transformed profile (Fig. 4f), a knickpoint (at

elevation of ~400 m) occurs on the channel. Below the knickpoint, the alluvial and bedrock portions share the same slope ($k_s=3354\pm 20 \text{ m}^{1.44}$) despite the different channel substrates. Above the knickpoint, the k_s value is $1667\pm 15 \text{ m}^{1.44}$. Variations in the slope of χ - z plot may be treated as spatially or temporarily variant rock uplift rates (Goren et al., 2014; Perron and Royden, 2013; Royden and Perron, 2013). However, **no knickpoint occurs on stream Juan because the river has been controlled by uniform rock uplift and under steady state (Snyder et al., 2000; see Sect. 4.2 for discussion). Thus, a χ - z plot generated by a single concavity may lead to misestimates in stream power parameters. We should recognize changes in concavities from slope-area space.**

According to the log-transformed slope-area plots, we identified bedrock channels of the 15 streams. Concavity indices were then calculated via both slope-area analysis and the integral approach. As shown in Fig. 5, both methods yielded similar concavities. Based on a mean θ value of 0.45 ± 0.10 (1σ), we computed χ - z plots and normalized steepness indices (k_{sn}) with uncertainty estimates (Fig. 6). **The uncertainties in steepness indices (no statistical test) are nearly lower than 1.0% (Fig. 6).**

We run statistic tests (Durbin-Watson test and Spearman rank correlation coefficient test) for the integral approach and slope-area analysis. For the integral approach, all the DW statistics are lower than D_L (Fig. 7a), indicating serially correlated residuals. Then, we revised the elevation and χ data according to Eq. (9) (Fig. 8). The DW statistics of revised χ - z plots are all between D_U and $4-D_U$ (Fig. 7a), indicating independent residuals. The results of linear fit are shown in Fig. 8. **The uncertainties in steepness indices (revised by Durbin-Watson test) are about 2.4% - 9.9% (Fig. 8), which are much higher than those without statistical test (lower than 1%, Fig. 6). In addition to uncertainty estimate, auto-correlated residuals can also bias the regression coefficient, steepness. The channel steepness values of streams Fourmile, Kinsey and Hardy are 57.01, 103.90 and 58.78 $\text{m}^{0.9}$ (Fig. 6). While revised by Durbin-Watson test, these values are 36.33, 82.16 and 76.65 $\text{m}^{0.9}$, respectively (Fig. 8). Then, steepness varies about 25.6% - 58.3% (dividing the difference of the two kinds of steepness indices by the values revised by Durbin-Watson test). Due to the influence of auto-correlated residuals on both the estimated value and precision of steepness, Durbin-Watson test is necessary when applying the integral approach. For slope-area analysis, the DW statistics are all between D_U and $4-D_U$ (Fig. 7b), showing no auto-correlation.**

We also calculated t-statistics for both slope-area analysis and the integral approach (Figs. 7a and b). All the results are less than 2, indicating homoscedastic residuals. **Despite no heteroscedasticity found in our study area, we suggest that Spearman rank correlation coefficient test should also be done because the test is a part of linear regression (statistically).**

In addition to statistic tests, another way proposed by Perron and Royden (2013) to estimate uncertainty in steepness is to make multiple independent calculations of different river profiles. From Fig. 6, the mean k_{sn} of high uplift zone ($U=4 \text{ mm/yr}$) is 104.40 ± 14.06 , and that of low uplift zone ($U=0.5 \text{ mm/yr}$) is 71.25 ± 10.08 . The standard errors of the mean k_{sn} among profiles are considerably larger than that for individual streams. However, for multiple profiles under similar geological and/or climatic settings, this approach should provide more meaningful estimates of uncertainty.

4 Discussion

Even though it gives highly uncertain channel steepness values, slope-area plot makes no assumptions about θ and therefore is more sensitive than χ analysis in detecting spatially varying concavities. Slope-area analysis, thus, is useful to identify difference in substrates along a river (e.g. bedrock, alluvium), which can be used as regression limits to apply the integral method. The integral approach yields better-constrained values of θ and k_{sn} . Combining them and statistic tests, this coupled approach thus provides more reliable results while applied to perform stream profile analysis. In the following sections, we will discuss the parameter uncertainty and steady assumption to better illustrate this method.

4.1 Uncertainty of channel concavity

Perron and Royden (2013) considered that the uncertainty in channel concavity derived from a linear regression of the log-transformed slope–area plot described how precisely one can measure the slope of the plot, not how precisely the parameter is known for a given landscape. They suggested that the difference between θ values that best linearize the main stem profile and that maximize the co-linearity of the main stem with its tributaries could be an estimate of uncertainty in θ for an individual drainage basin.

In most cases, the θ value that collapses the main stem and its tributaries is often used as a reference concavity (Mudd et al., 2014; Perron and Royden, 2013; Willett et al., 2014; Yang et al., 2015). In fact, supposing a drainage basin under uniform geologic and climatic settings, this kind of θ value can be compared with the mean value of concavities of the stem and its tributaries. We thereafter, name these two concavities θ_{Co} (derived from the collinearity test) and θ_{mR} (from averaging the concavity values of all the streams within a catchment), respectively.

We extracted the stems and tributaries of streams, Singley, Davis, Fourmile and Cooskie (Fig. 9a), based on A_{cr} of 0.1–0.16 km² (Fig. 5). We calculated the correlation coefficients of χ -z plots based on a range of θ (Figs. 9b-d). The θ_{mR} of catchments are 0.45, 0.48, 0.43, and 0.55. We also derived θ_{Co} which collapses the stem and tributaries, 0.45, 0.45, 0.45, and 0.55 (Fig. 10). Both θ_{Co} and θ_{mR} are similar to the stem concavities, 0.50, 0.42, 0.50, and 0.45 (Fig. 5). Hence, for steady state bedrock channels under uniform lithologic and climatic settings, all three kinds of concavities should be similar. Then, the difference between these θ values could be an estimate of concavity uncertainty.

However, it is different for streams consisting of both bedrock and alluvial channels. We extracted the stems and tributaries of streams, Hardy, Juan, Howard and Dehaven (Fig. 11a). The θ_{mR} values of them are 0.57, 0.68, 0.73, and 0.73 (Figs. 11b-e), similar to the stem concavities (0.63, 0.70, 0.72, and 0.75) (Figs. 11b-e), but larger than the θ_{Co} (0.45, 0.45, 0.45, and 0.55) (Fig. 12). In such case, differences between θ_{Co} and θ_{mR} are not random errors and cannot be estimates of concavity uncertainty.

Nevertheless, θ_{Co} values (0.45, 0.45, 0.45, and 0.55) are similar to the concavities of bedrock reaches of stems (0.55, 0.52, 0.55, and 0.40) (Fig. 5). Then, the differences between θ_{Co} and concavities of bedrock reaches may be estimates of

uncertainties in θ . Hence, the reference concavity collapsing the stem and its tributaries works well even for **all the profile data** consisting of both bedrock and alluvial channels.

In most cases, a somewhat higher constant critical area (e.g. 1 or 5 km²) is assumed to calculate χ values of fluvial channels (Goren et al., 2014, 2015; Willett et al., 2014; Yang et al., 2015). Here we extracted streams of four drainages (Fig. 13a), Hardy, Juan, Howard, and Dehaven, based on a critical area of 0.5 km² (three or four times the actual values). We then derived the concavities that best linearize stems (0.73, 0.78, 0.82, and 0.84) (Figs. 13b-e), θ_{mR} (0.60, 0.80, 0.75, and 0.75) (Figs. 13b-e), and θ_{Co} (0.40, 0.50, 0.45, and 0.55) (Fig. 14), respectively. All the results are similar to those based on actual critical areas (Figs. 11 and 12). Hence, choosing a uniform A_{cr} somewhat different to the actual values might be reasonable and would not have significant influence.

10 4.2 Steady state assumption of streams in the MTJ region

Usually, river shape may not be diagnostic of equilibrium conditions. In some places, recent work on inversion of drainage patterns for uplift rate histories indicates that river profile shapes are controlled by spatio-temporal variations in uplift rate moderated by erosional processes (Pritchard et al., 2009; Roberts and White, 2010; Roberts et al., 2012).

In the MTJ region, the uplift rates determined by marine terraces are variable in space and time (0-4 mm/a, Merritts and Bull, 1989). However, in the low-uplift zone (streams Hardy to Dehaven), uplift rates have been approximately constant for at least 0.33 Ma (Merritts and Bull, 1989). The bedrock-channel reaches are probably not affected by sea-level fluctuations (Snyder et al., 2000). These streams thus can be in or near equilibrium. Nevertheless, disequilibrium conditions are likely in regions of high-uplift rate (e.g. the rivers north of 40°N). To test the steady state assumption, we modelled the uplift rate histories.

Erosional parameters in the stream power model (e.g. m and n) and uplift histories can be determined from joint inversion of drainage network (Glotzbach 2015; Goren et al., 2014; Pritchard et al., 2009; Rudge et al., 2015). Here, we utilized the method of Goren et al (2014). For spatially variant rock uplift, the study area is divided into four distinct zones, from north to south, the north transition zone (streams Singley to Cooskie), the King Range high-uplift zone (streams Randall to Buck), the intermediate-uplift zone (stream Horse Mtn), and the low-uplift zone (streams Hardy to Dehaven) (Figs. 15a-d; Snyder et al., 2000). Within each zone, we assumed spatially invariant rock uplift for small drainage areas and similar uplift rates determined from marine terraces (Merritts and Bull, 1989). Snyder et al (2000) suggested $n \sim 1$ and variable K between the high- and low-uplift zones. According to the linear inversion model of Goren et al (2014), the present river channel elevation is determined by both rock uplift rate and response time, $\tau(x)$ (time for perturbations propagating from the river outlet, at $x=0$, to a point x along the channel):

$$30 \quad z(x) = \int_{-\chi(x)}^0 U^*(t^*) dt^* \quad (12)$$

$$U^* = U/(KA_0^m), \quad t^* = KA_0^m t \quad (13)$$

For the linear model ($n=1$) and $A_0=1 \text{ m}^2$, response time $\tau(x)=\chi(x)/K$. The scaled time t^* has the same unit of χ , and U^* is dimensionless rock uplift rate.

Since χ - z plot may be affected by other factors (e.g., climate and lithology), we extracted all the fluvial channels and calculated a mean χ - z plot for each zone (Figs. 15e-h). We defined z_1, z_2, \dots, z_N and $\chi_1, \chi_2, \dots, \chi_N$ to be the elevations and χ values of N data points along a fluvial channels network ($N=10$ here). Then, based on Eq. (12), the dimensionless rock uplift histories for the four zones are shown in Fig. 15i. For the low-uplift zone, alluvial channels in the lower reaches were excluded for them being affected by sea-level fluctuations.

We utilized variable erodibility ($K=U/k_{sn}$) values to calculate rock uplift rates. The K values for transition, high-uplift, intermediate and low-uplift zones are $6.17 \times 10^{-5} \text{ m}^{0.1}/\text{a}$, $3.82 \times 10^{-5} \text{ m}^{0.1}/\text{a}$, $3.38 \times 10^{-5} \text{ m}^{0.1}/\text{a}$, and $0.37 \times 10^{-5} \text{ m}^{0.1}/\text{a}$, respectively. According to the inferred uplift histories (Fig. 15j), the maximum response time (the perturbations migrating from the river outlet to water head) differs significantly from low- (0.43 Ma) to high-uplift (0.16 Ma) zones. The rock uplift rates in the low- and intermediate-uplift zones have been constant (~ 0.3 - 0.4 mm/a since 0.4 Ma, and ~ 2 - 2.5 mm/a since 0.16 Ma, respectively). The north transition and high-uplift zones both experienced increases in the uplift rates (from $\sim 2.5 \text{ mm/a}$ to 3.3 mm/a , and from $\sim 3.7 \text{ mm/a}$ to 4.3 mm/a , respectively) starting about 0.12 Ma ago. However, the increase ratios are much lower. Considering the maximum response time ($\sim 0.16 \text{ Ma}$), the uplift rates have been constant for a relatively long period. In addition, no large knickpoints are found along the rivers. All of these indicate that the rivers have been reshaped by the recent tectonic activities and have reached steady state.

In the recent 0.02 Ma, the rock uplift rates seem to be a bit lower (Fig. 15j). That may be due to variant channel concavities. The reaches downstream are usually characterized by rapidly decreasing gradient (higher concavities). Then, lower U^* will be produced when using a reference concavity (0.45). As a result, the modelled rock uplift rates will be low. The variance in channel concavity may indicate difference in river substrate (e.g. sedimentation affected by sea-level fluctuations) rather than tectonics (Snyder et al., 2000).

4.3 Influence of elevation data uncertainty

Roberts et al (2012) noticed that the slope-area methodology might produce unstable results because small amounts of randomly distributed noise added to river profile will cause significant change in channel gradient. In spite of little knowledge about the elevation data uncertainty here, we utilized different datasets and various data handling methods (data smoothing and sampling) to calculate channel slope with different uncertainties. Then, to some extent, the influence of data uncertainty can be tested.

In the analysis above, the channel slope is derived from 1 arc-second SRTM DEM via 300 m smoothing window and 20 m contour sampling interval. Then, we reanalysed the streams in high- and low-uplift zones based on 1/3 arc-second USGS DEM (downloaded from <https://catalog.data.gov/dataset/national-elevation-dataset-ned-1-3-arc-second-downloadable-data-collection-national-geospatial>). We calculated the channel slope via 300 m smoothing window and 20 m contour sampling interval (Figs. 16a and d), 300 m smoothing window and 10 m contour sampling interval (Figs. 16b and e), and 100 m

smoothing window and 10 m contour sampling interval (Figs. 16c and f), respectively. To get average values, **slope-area data from all the streams within the same zone were composited.**

We chose 0.1-3 km² as regression limits for the high-uplift zone and 0.2-8 km² for the low-uplift area. The channel concavity and steepness (k_{sn}) were calculated by linear regressing the log-transformed slope-area data and χ -z plots ($\theta_{ref}=0.45$), respectively. The stream concavity indices in the high-uplift zone (0.41±0.05) and low-uplift region (0.48±0.03) are similar to or within error of the estimates reported by this study (0.45±0.10, 1 Arc-second SRTM DEM), Wobus et al (2006) (0.57±0.05, 10-m-pixel USGS DEM), and Snyder et al (2000) (0.43±0.11, 30 m USGS DEM). All the error estimates are characterized by 1 σ . Mean k_{sn} values of 109 and 60 m^{0.9} in the high- and low-uplift zones, respectively, yield a ratio of $k_{sn}(\text{high})/k_{sn}(\text{low})$ of ~1.82, which is a principal conclusion upheld by both Snyder et al (2000) and Wobus et al (2006). Then, no distinct difference is found in concavity and channel steepness indices when using different datasets and data handling methods.

We do not deny that utilising different datasets may cause limited difference in parameter estimate for an individual catchment. For example, when using the integral approach, the resulting channel concavity of stream Cooskie is 0.45 (in Sect. 3) (1 arc-second SRTM DEM) but 0.36 in Perron and Royden (2013) (1/3 arc-second USGS DEM). However, for averaging results (as done in Sect. 4.3), uncertainty in elevation data may not cause distinct differences in parameter estimates in this study area (e.g. θ and k_{sn}).

4.4 Disequilibrium circumstances in large rivers

The case study has disadvantages of including only short (<10 km long; < 20 km² area) and steady streams. In many landscapes, especially large rivers, this steady assumption will not be met (Harkins et al., 2007; Wobus et al., 2006; Yang et al., 2014). Then, we took Mattole, a large river in the MTJ region (Fig. 17a), for example, to extract the unsteady signals. Here, 1/3 arc-second USGS DEM was used.

Using 300 m smoothing window and 20 m contour sampling interval, we derived a log-transformed slope-area plot of the stem (Fig. 17b). We found the critical threshold of drainage area, A_{cr} , ~0.1 km² and at the elevation of ~450 m (Figs. 17b and c). A knickpoint was detected by the scaling break in the slope-area data and then marked in the shaded-relief map (Fig. 17a) and the river profile (Fig. 17c). The knickpoint **is located at an elevation of ~280 m.** The concavity indices above (0.61±0.01) and below (0.58±0.07) the knickpoint are nearly the same. To compare with the adjacent streams, a reference concavity $\theta_{ref}=0.45$ was used to calculate the channel steepness. Using the integral approach and two statistic tests, we derived the k_{sn} above (10.81±0.86 m^{0.9}) and below (17.44±1.16 m^{0.9}) the knickpoint. However, in the adjacent streams, (e.g. Davis, Fourmile), the k_{sn} values are much larger than 60 m^{0.9}. In addition to spatial variations in Holocene uplift rates of marine platforms (Merritts, 1996), **these steepness indices suggest** that other variables (e.g. sediment flux and lithology) may affect channel steepness. This might limit our ability to quantitatively relate steepness indices to uplift rates in this field setting, as noticed by Wobus et al (2006).

Usually, the method of best linearizing χ -z plot is used to compute θ for a steady state bedrock river profile (Perron and Royden, 2013). However, in many cases, whether a stream is in equilibrium is unknown. We computed the correlation coefficients between the channel elevation and χ values ($A_{cr}=0.1 \text{ km}^2$, $A_0=1 \text{ m}^2$) of the stem based on a range of θ (Fig. 17d). The best linear fit corresponds to $\theta=0.30$ ($k_s=1.45\pm 0.06 \text{ m}^{0.6}$, $R=0.985$, Fig. 17e), which is distinctly different from the result of slope-area analysis.

We extracted all the tributaries of the Mattole river and calculated their χ -z plots based on a range of θ values (Figs. 18a-d). The elevation scatters of the χ -z plots are plotted against θ values (Fig. 18e). The θ value that collapses the main stem and its tributaries is 0.45, showing the reasonability of using 0.45 as a reference concavity to calculate the stem k_{sn} . As shown by Fig. 18c, the knickpoint (with an elevation of about 280 m) can also be detected from the χ -z plot of the stem. **Both the slope-area data (Fig. 17b) and the χ -z plot based on a θ value derived from collinearity test (Fig. 18c) detect the unsteady signal on the trunk stream of the Mattole river, despite the best linearity for the integral approach (Fig. 17e). Then, we can find that a river may be in disequilibrium condition in spite of a linear relationship in the χ -z plot. In some cases, uplift can be inserted along rivers, which makes values of χ difficult to interpret (Czarnota et al., 2014; Paul et al., 2014; Pritchard et al., 2009; Roberts and White, 2010; Roberts et al., 2012; Wilson et al., 2014).**

Based on $\theta_{ref}=0.45$, we calculated the map of channel steepness with an elevation interval of 100 m. The channel steepness values range from 1 to 273. As shown in Fig. 19, the lower k_{sn} values are along the whole stem and its tributaries (low elevation) above the knickpoint while higher values are along the upstream (high elevation) of tributaries below the knickpoint. Among the tributaries in the west of the stem, channel steepness decreases from the central part (near streams Big to Shipman, high-uplift zone) towards both north (close to stream Fourmile, north transition zone) and south (near streams Horse Mtn and Telegraph, intermediate-uplift zone). Both the spatial pattern of k_{sn} and the positive relationship between k_{sn} and elevation may indicate a tectonic control on channel steepness despite other potential variables.

5 Conclusion

In this contribution, we coupled the advantages of slope-area analysis and the integral approach to steady state bedrock river profile analysis. First, we identified colluvial, bedrock and alluvial channels from a log-transformed slope-area plot. Utilizing the integral approach, we then derived concavity and steepness indices of a bedrock channel. Finally, via Durbin-Watson statistic test, we examined and eliminated serial correlation of linear regression residuals, which produced more reliable and robust estimates of uncertainties in stream power parameters.

Acknowledgement

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Table 1. Range of DW statistic and the related meaning

DW Statistic	Meaning
$0 \leq DW \leq D_L^*$	Positively auto-correlated residuals
$D_L < DW \leq D_U^*$	Beyond the suitability of Durbin-Watson test
$D_U < DW < 4 - D_U$	Mutually independent residuals
$4 - D_U \leq DW < 4 - D_L$	Beyond the suitability of Durbin-Watson test
$4 - D_L \leq DW \leq 4$	Negatively auto-correlated residuals

* D_L and D_U represent the critical value of Durbin-Watson test and can be found in Durbin and Watson (1950).

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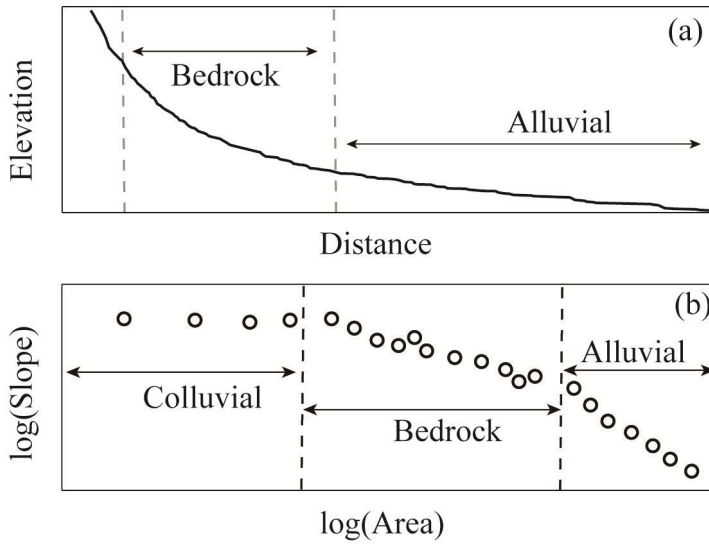


Figure 1. Schematic of a steady state river profile consisting of colluvial, bedrock and alluvial channels, revised from Figures 7A and B in Snyder et al (2000). (a) Stream profile. (b) Log-transformed slope-area plot.

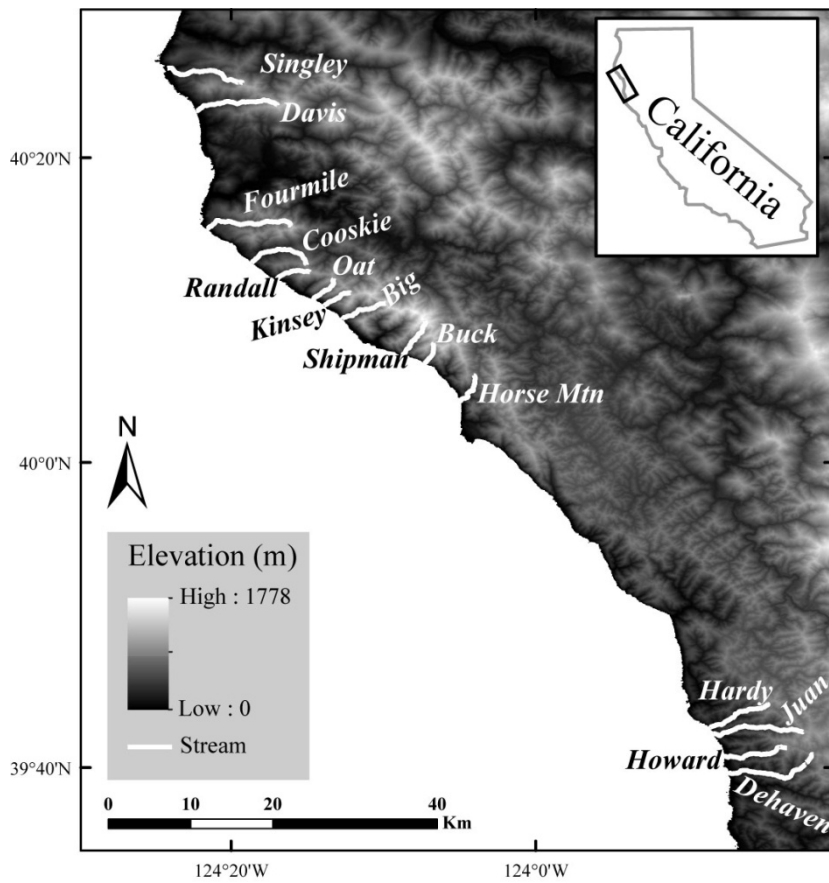


Figure 2. Streams in the Mendocino Triple Junction (MTJ) region of northern California, USA. Streams are from Snyder et al (2000). The elevation data are from 1 Arc-Second SRTM (<http://earthexplorer.usgs.gov/>)

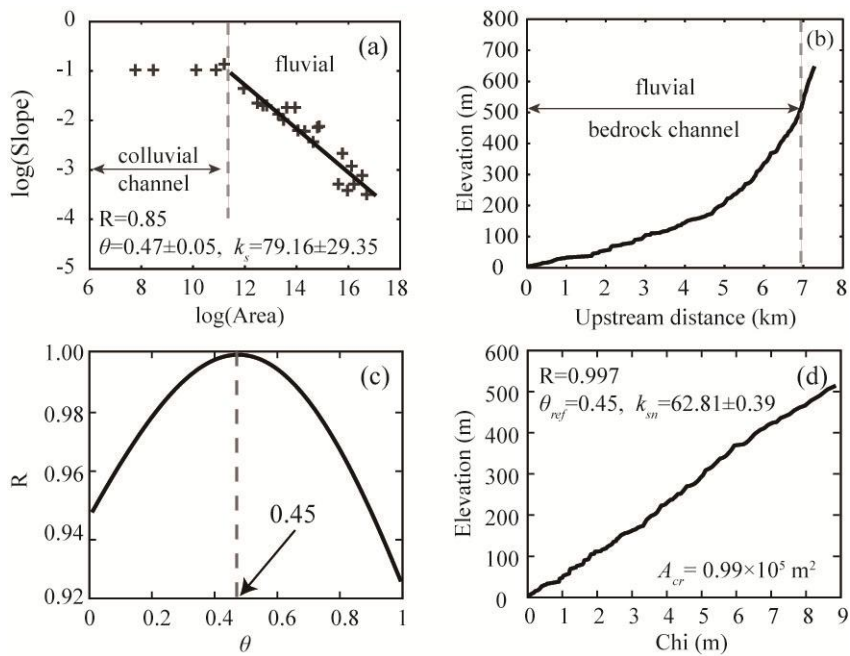


Figure3. Stream profile analysis of Cooskie. (a) Log-transformed slope-area plot. The slope was derived from the smoothed (horizontal distance of 300m) and re-sampled (elevation interval of 20m) elevation data. (b) The full river profile (without any smoothing or re-sampling) of Cooskie. (c) The correlation coefficients, R , as a function of θ for least-squares regression based on Eq. (5). The maximum value of R , which corresponds to the best linear fit, occurs at $\theta=0.45$ (dotted line and black arrow). (d) χ - z plot of the bedrock channel profile, transformed according to Eq. (3) with $\theta=0.45$, $A_{cr}=0.1 \text{ km}^2$, and $A_0=1 \text{ m}^2$.

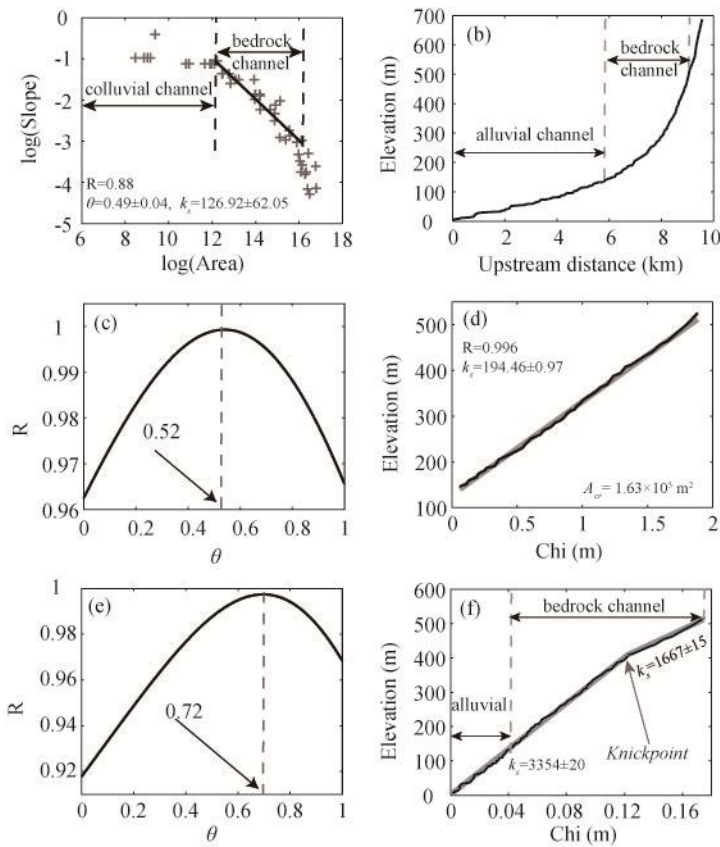


Figure 4. Stream profile analysis of Juan. (a) Log-transformed slope-area plot. The slope was derived from the smoothed (horizontal distance of 300m) and re-sampled (elevation interval of 20m) elevation data. (b) The full river profile (without any smoothing or re-sampling) of Juan. (c) The correlation coefficients of χ - z plots as a function of θ for the bedrock portion of the river. The maximum value of R occurs at $\theta=0.52$. (d) χ - z plot of the bedrock channel profile based on a concavity value of 0.52. (e) The correlation coefficients of χ - z plots as a function of θ for fluvial (both bedrock and alluvial) channel. The maximum value of R occurs at $\theta=0.72$. (f) χ - z plot of the fluvial (both bedrock and alluvial) channel profile based on a concavity value of 0.72.

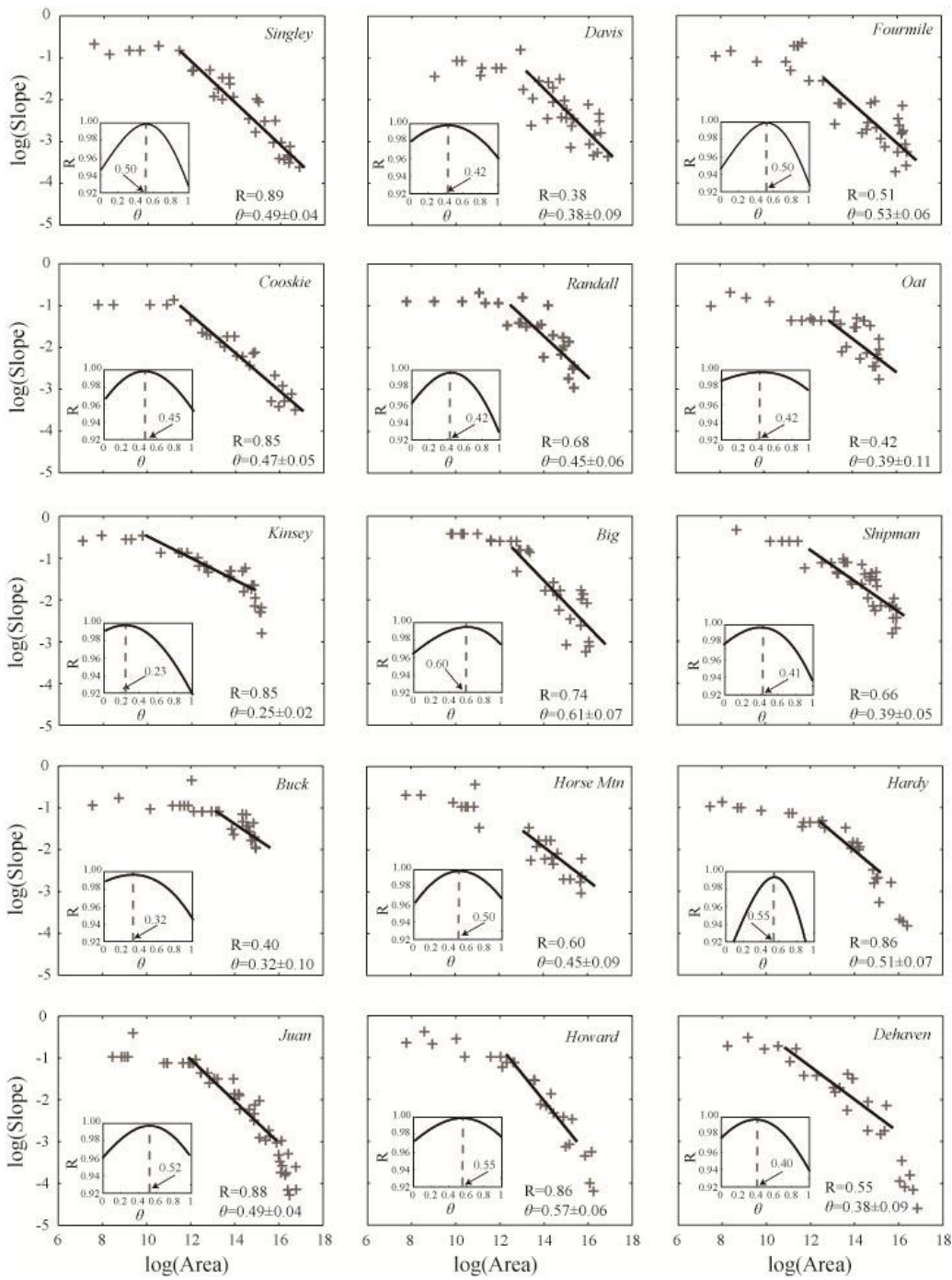


Figure 5. Correlation coefficients derived from slope-area analysis and the integral approach. The slope was derived from the smoothed (horizontal distance of 300m) and re-sampled (elevation interval of 20m) elevation data. The correlation coefficients of χ -z plots as a function of θ for bedrock channels are shown in the left bottom. Then mean θ value is 0.45.

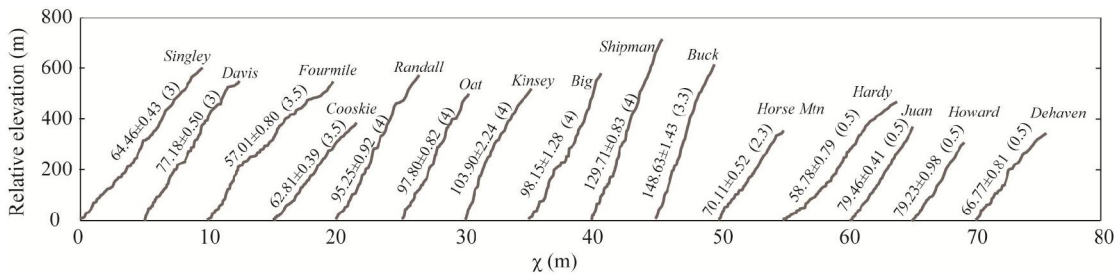


Figure 6. χ - z plots of the streams (bedrock channels) based on the mean concavity (0.45). Numbers are normalized channel steepness, k_{sn} , with the uncertainty estimates. Numbers in the parentheses are uplift rates with a unit of millimetre per year (Snyder et al., 2000). Italic characters are stream names.

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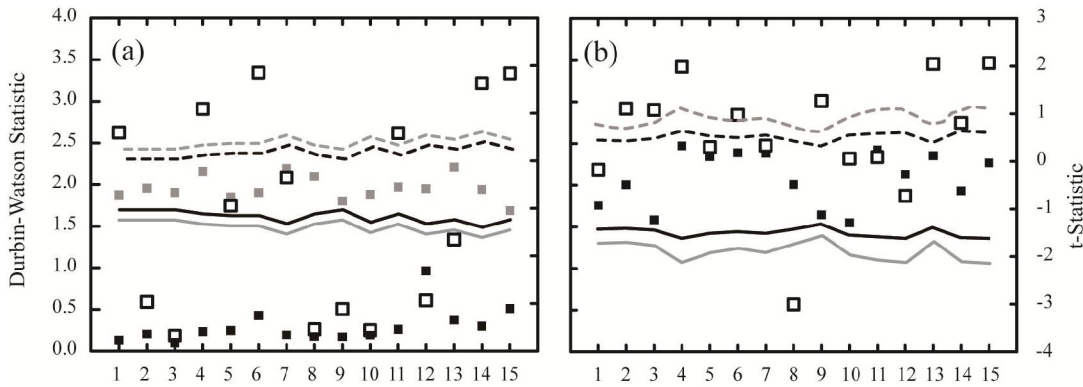


Figure 7. Statistic tests for the integral approach (a) and slope-area analysis (b). Black hollow squares are t-statistic of Spearman rank correlation coefficient. Black solid squares are Durbin-Watson statistics. The gray solid line, black solid line, black dashed line and gray dashed line are D_L , D_U , $4-D_U$, and $4-D_L$. Gray squares in Figure (a) are the Durbin-Watson statistics of revised χ - z plots. The river numbers 1 to 15 indicate streams: Singley, Davis, Fourmile, Cooskie, Randall, Oat, Kinsey, Big, Shipman, Buck, Horse Mtn, Hardy, Juan, Howard, and Dehaven.

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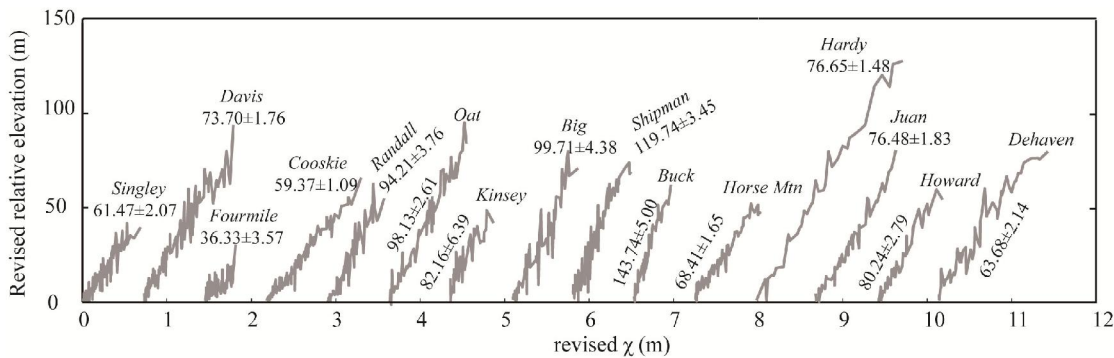


Figure 8. Revised relative elevation and χ values. Gray lines and Numbers are revised data and steepness index with uncertainty estimates.

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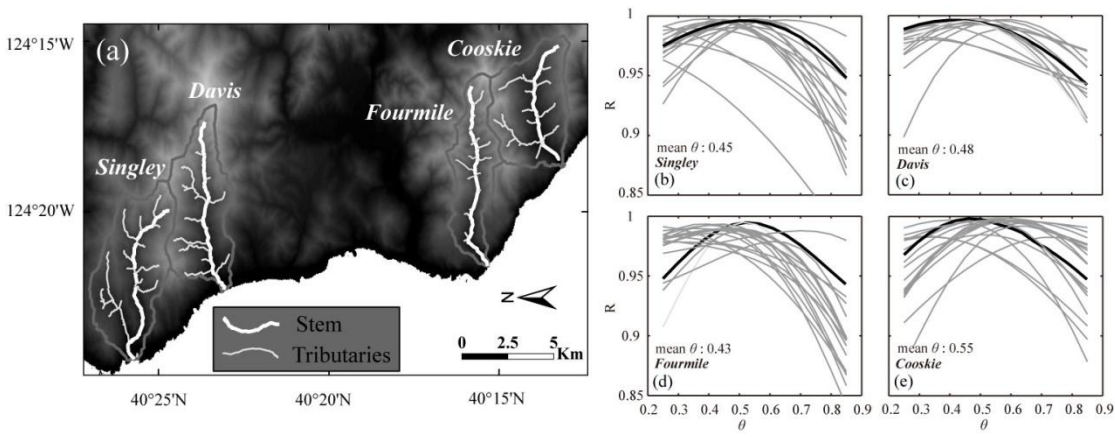
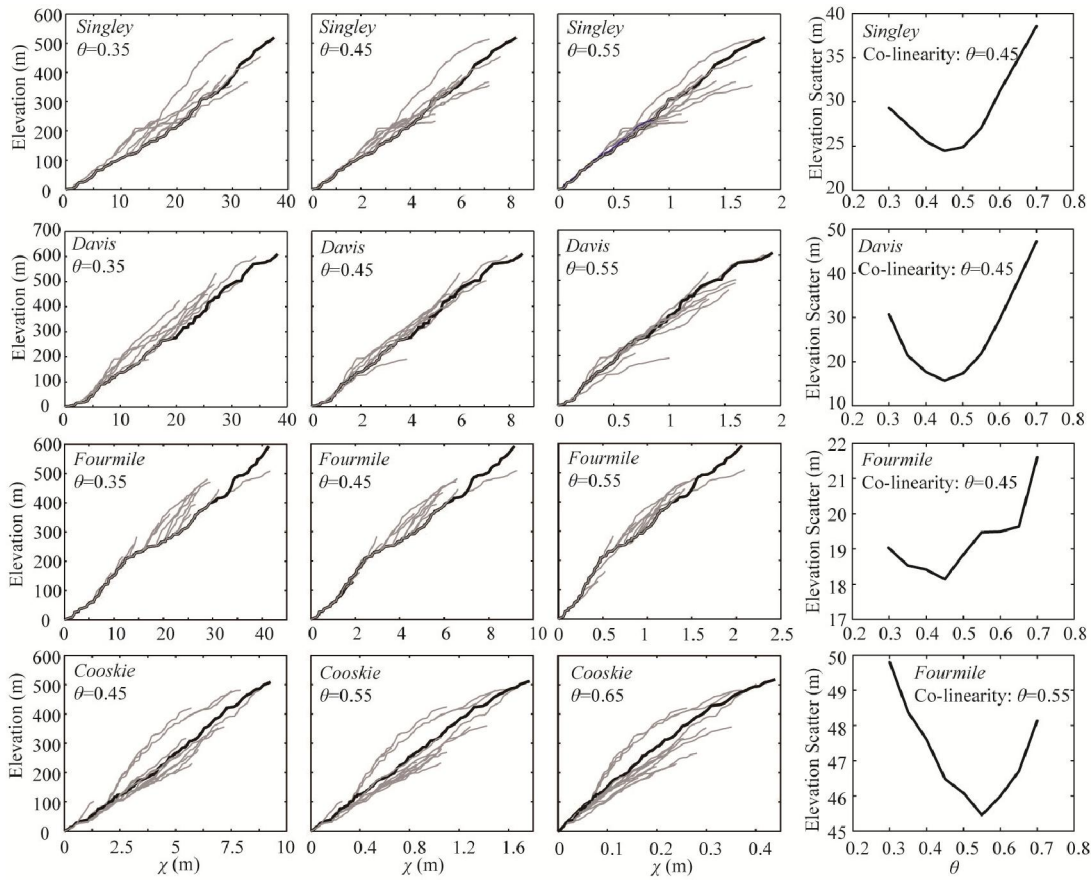


Figure9. Correlation coefficients of χ - z plots as a function of θ . (a) Location of the streams. (b-e) Correlation coefficients of χ - z plots based on a range of θ values. Black thick lines indicate stems.



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Figure10 Concavity values that maximize the co-linearity of the main stem with its tributaries. Black thick lines in the χ - z plots are stems.

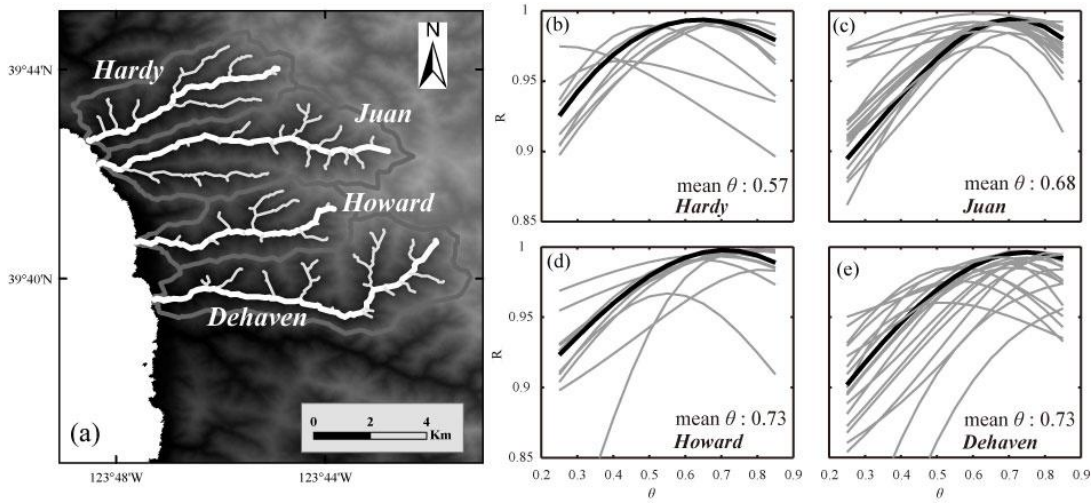
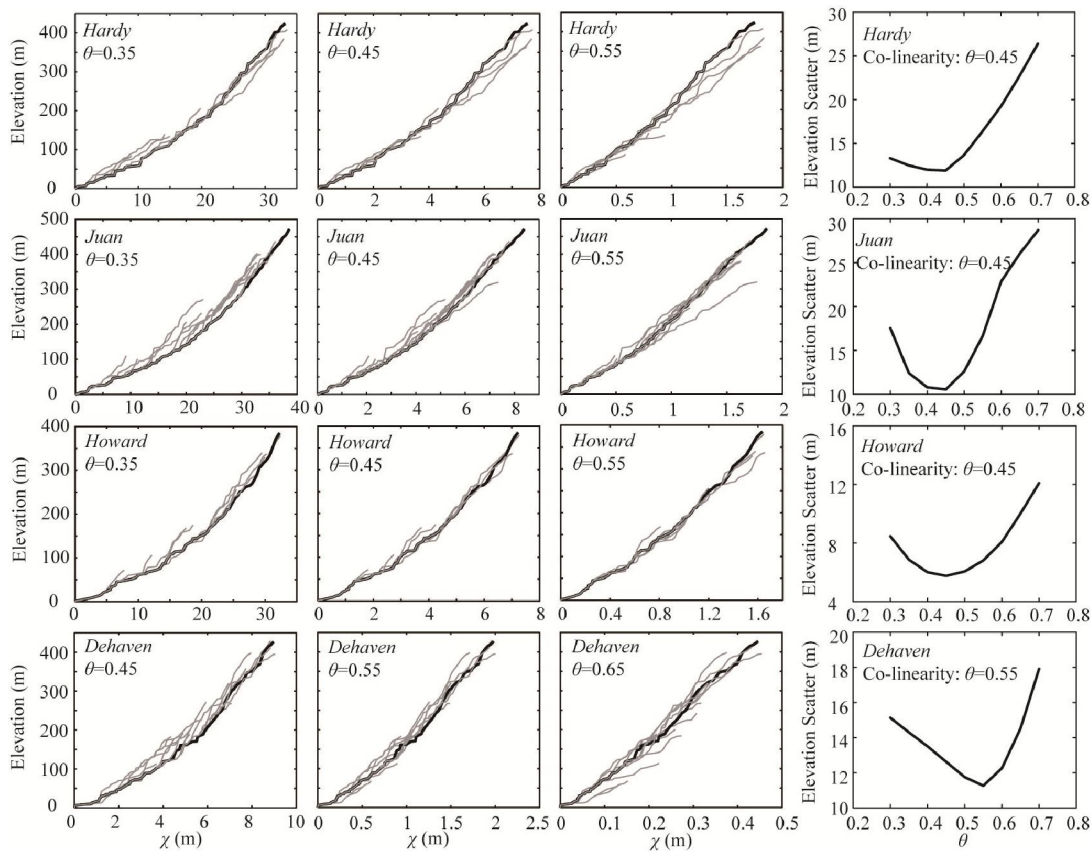


Figure 11. Correlation coefficients of χ - z plots as a function of θ . (a) Location of the streams. (b-e) Correlation coefficients of χ - z plots based on a range of θ values. Black thick lines indicate stems.



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Figure 12. Concavity values that maximize the co-linearity of the main stem with its tributaries. Black thick lines in the χ - z plots are stems.

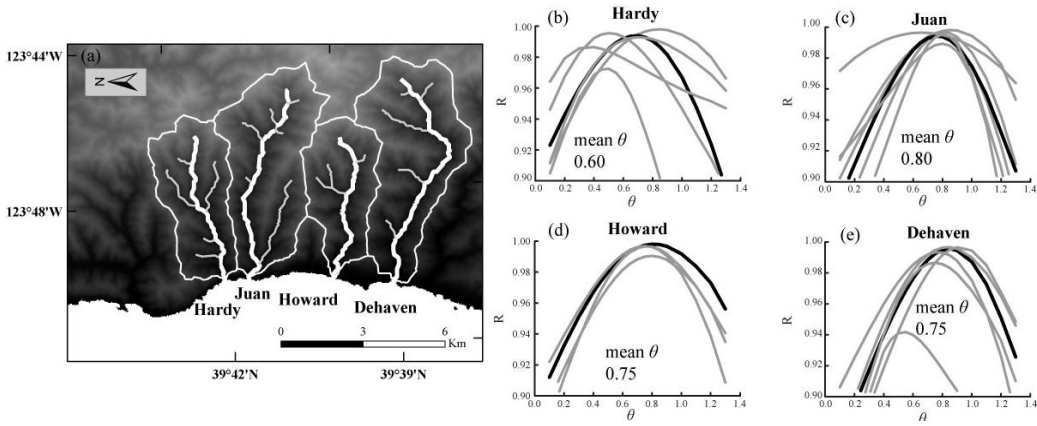


Figure13. Correlation coefficients of χ - z plots as a function of θ . (a) Location of the streams. Streams are extracted with a critical area of 0.5km^2 . (b-e) Correlation coefficients of χ - z plots based on a range of θ values. Black thick lines indicate stems.

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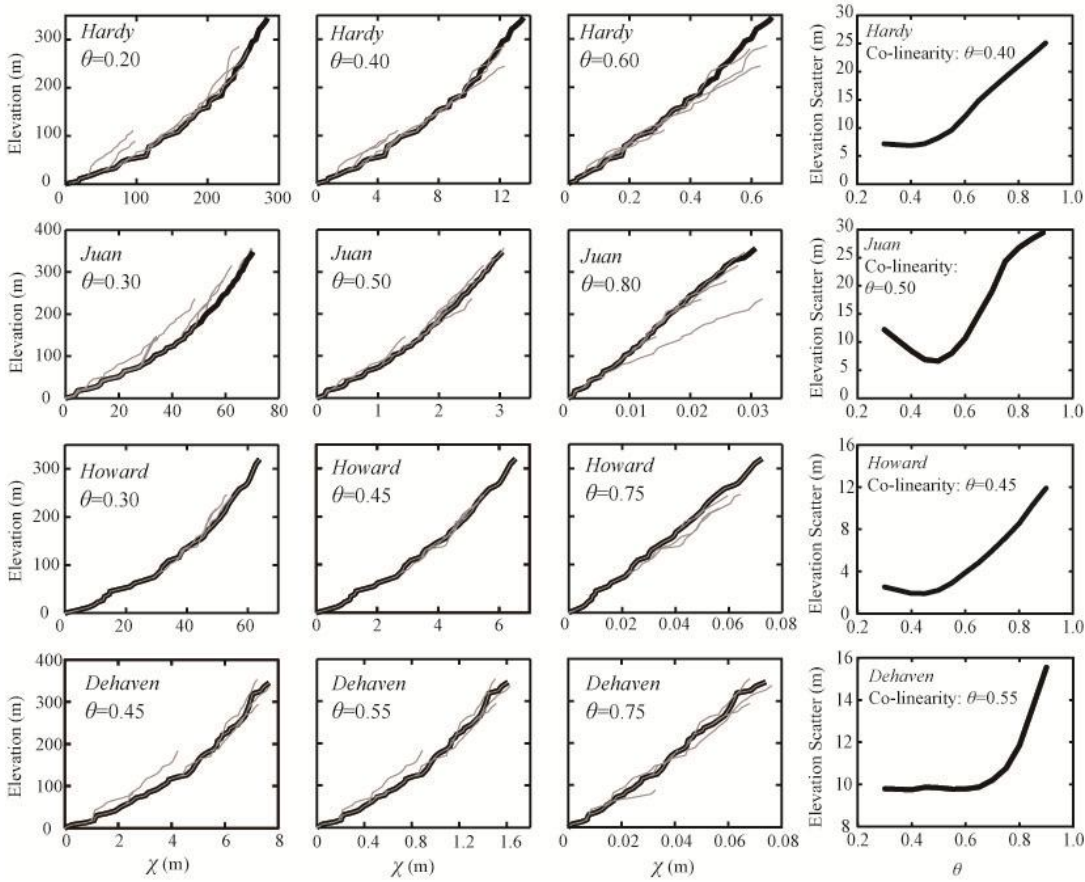


Figure14. Concavity values that maximize the co-linearity of the main stem with its tributaries. Black thick lines in the χ - z plots are stems.

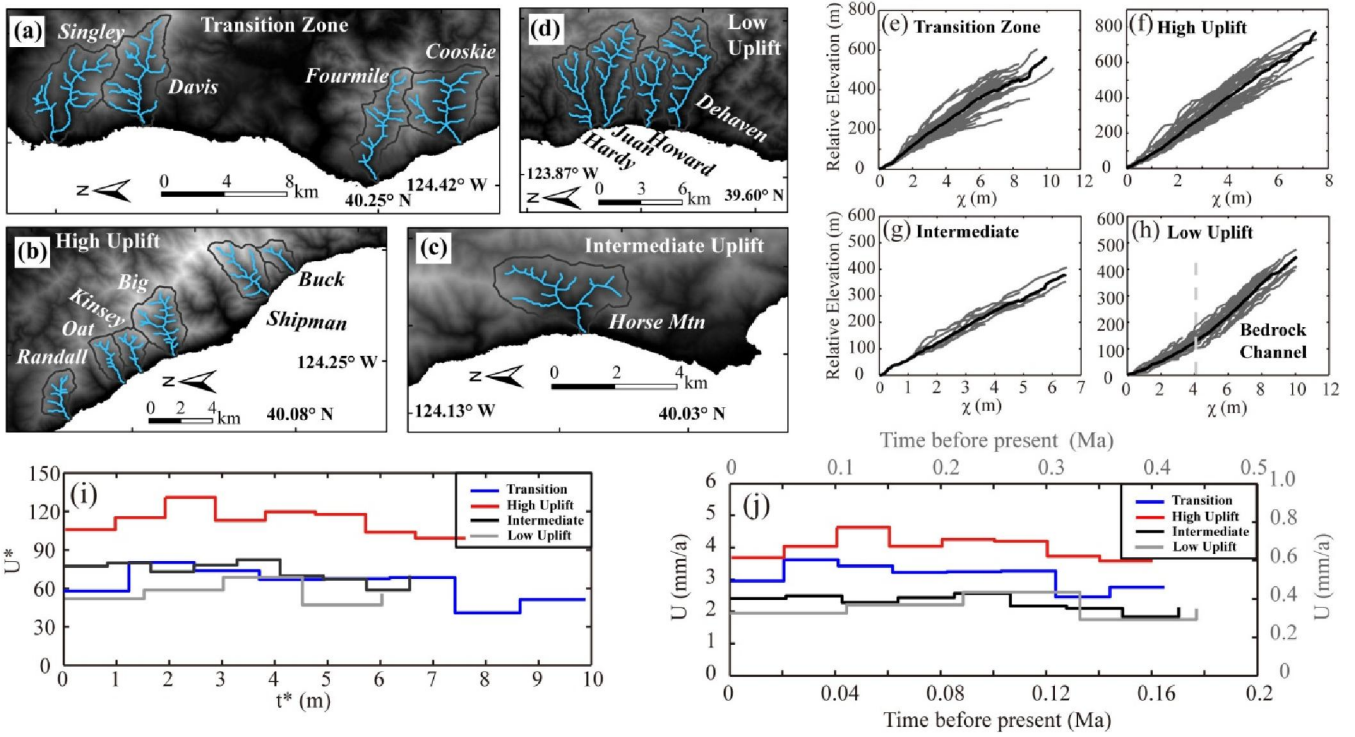


Figure 15. Uplift histories inferred from the stream profiles. (a)-(d) The map of streams in the four zones: north transition zone (a), King Range high-uplift zone (b), intermediate-uplift zone (c), and low-uplift zone (d). (e)-(h) The χ -z plots of the streams within each zone ($A_0=1 \text{ m}^2$). (i) Scaled U^* as a function of scaled time t^* . (j) Inferred relative uplift rate as a function of time before the present. The left-bottom black axes show the results of north transition, high-uplift and intermediate-uplift zones. The right-top gray axes show the result of low-uplift zone.

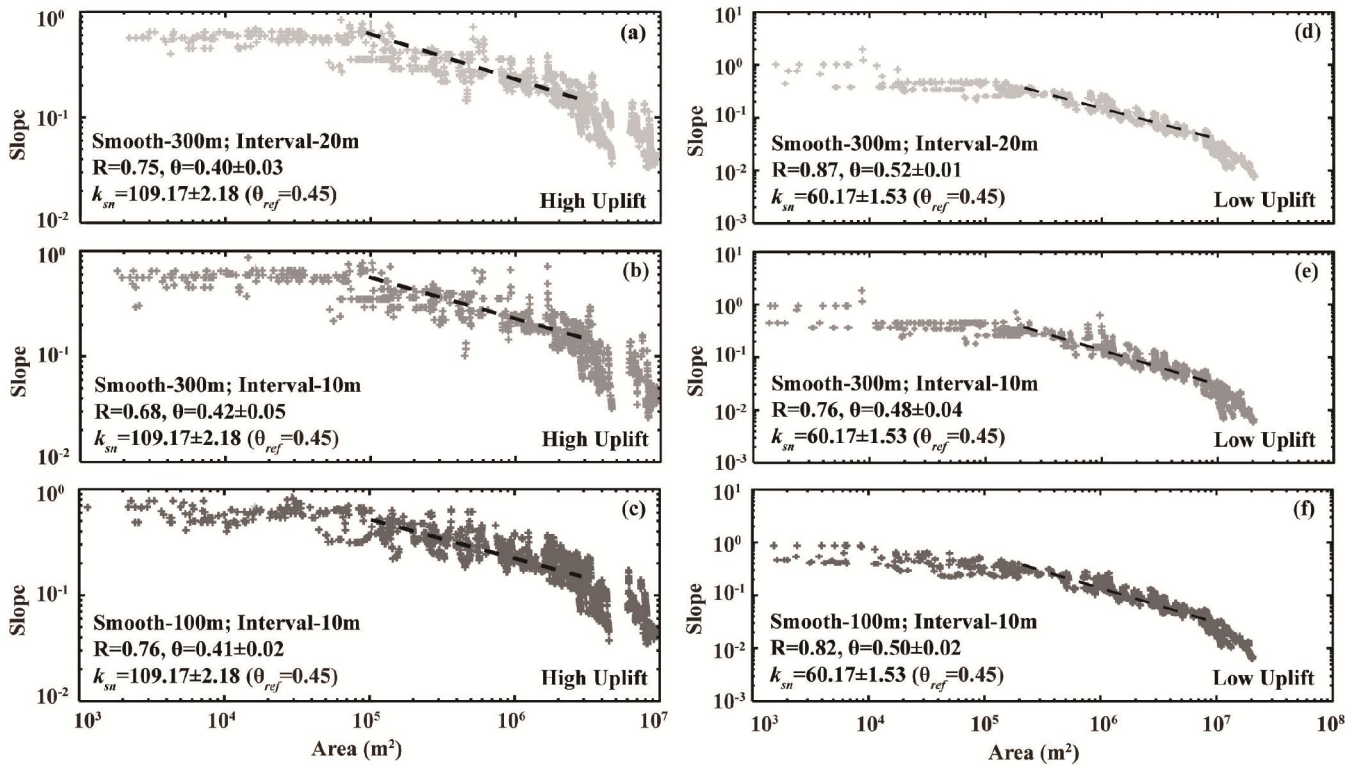


Figure 16. Log-transformed slope-area plots of streams in the high-uplift (a-c) and low-uplift (d-f) zones. Streams within the same zone are composited. The slope data are calculated via different methods: 300 m smoothing window and 20 m contour sampling interval (a and d), 300 m smoothing window and 10 m contour sampling interval (b and e), and 100 m smoothing window and 10 m contour sampling interval (c and f). Elevation data are from 1/3 arc-second USGS DEM (downloaded from <https://catalog.data.gov/dataset/national-elevation-dataset-ned-1-3-arc-second-downloadable-data-collection-national-geospatial>).

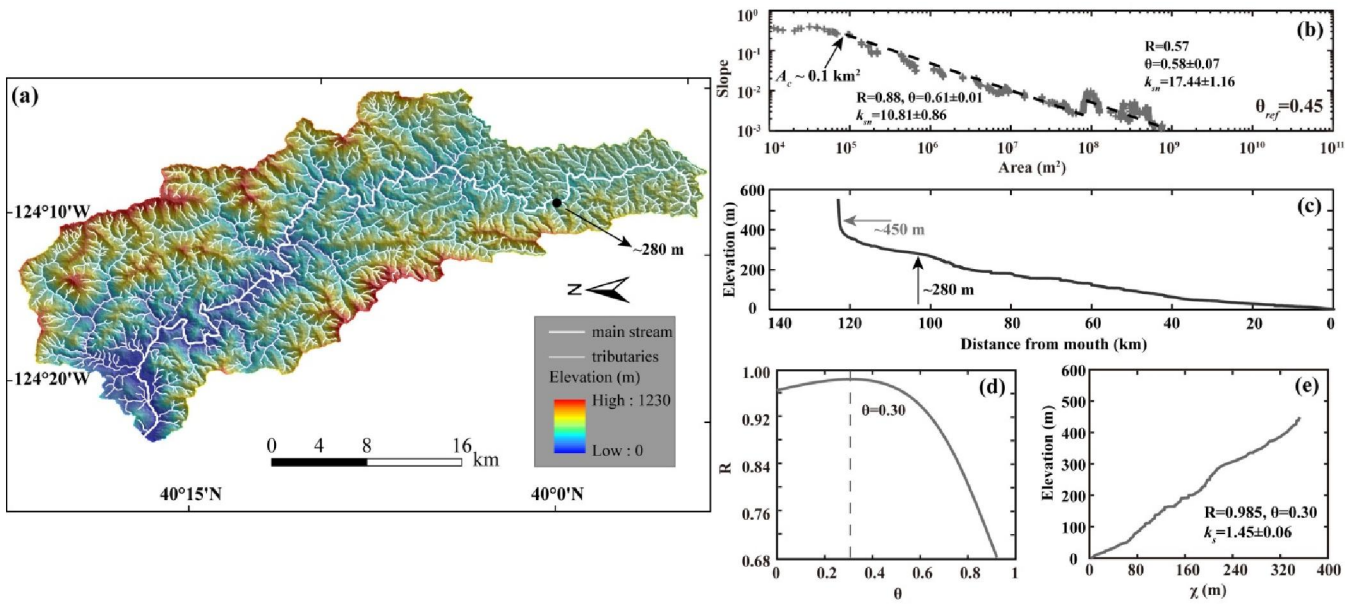


Figure 17. The slope-area data and χ - z plot of the stem of Mattole river. (a) Map of the stem and its tributaries in the Mattole drainage basin. Elevation data are from 1/3 arc-second USGS DEM (downloaded from <https://catalog.data.gov/dataset/national-elevation-dataset-ned-1-3-arc-second-downloadable-data-collection-national-geospatial>). (b) The log-transformed slope-area plot of the stem (300 m smoothing window and 20 m contour sampling interval). A knickpoint is detected from the plot with variant k_{sn} along the channel. (c) River profile of the stem. The gray arrow indicates the dividing point (~ 450 m) between the colluvial and fluvial portions. The black arrow shows the knickpoint (~ 280 m) on the stem. (d) The correlation coefficients between elevation and χ values as a function of θ . The maximum value of R , which corresponds to the best linear fit, occurs at $\theta=0.30$ (gray dashed line). (e) The χ - z plot of the stem, transformed according to Eq. (3) with $\theta=0.30$, $A_{cr}=0.1 \text{ km}^2$, and $A_\theta=1 \text{ m}^2$.

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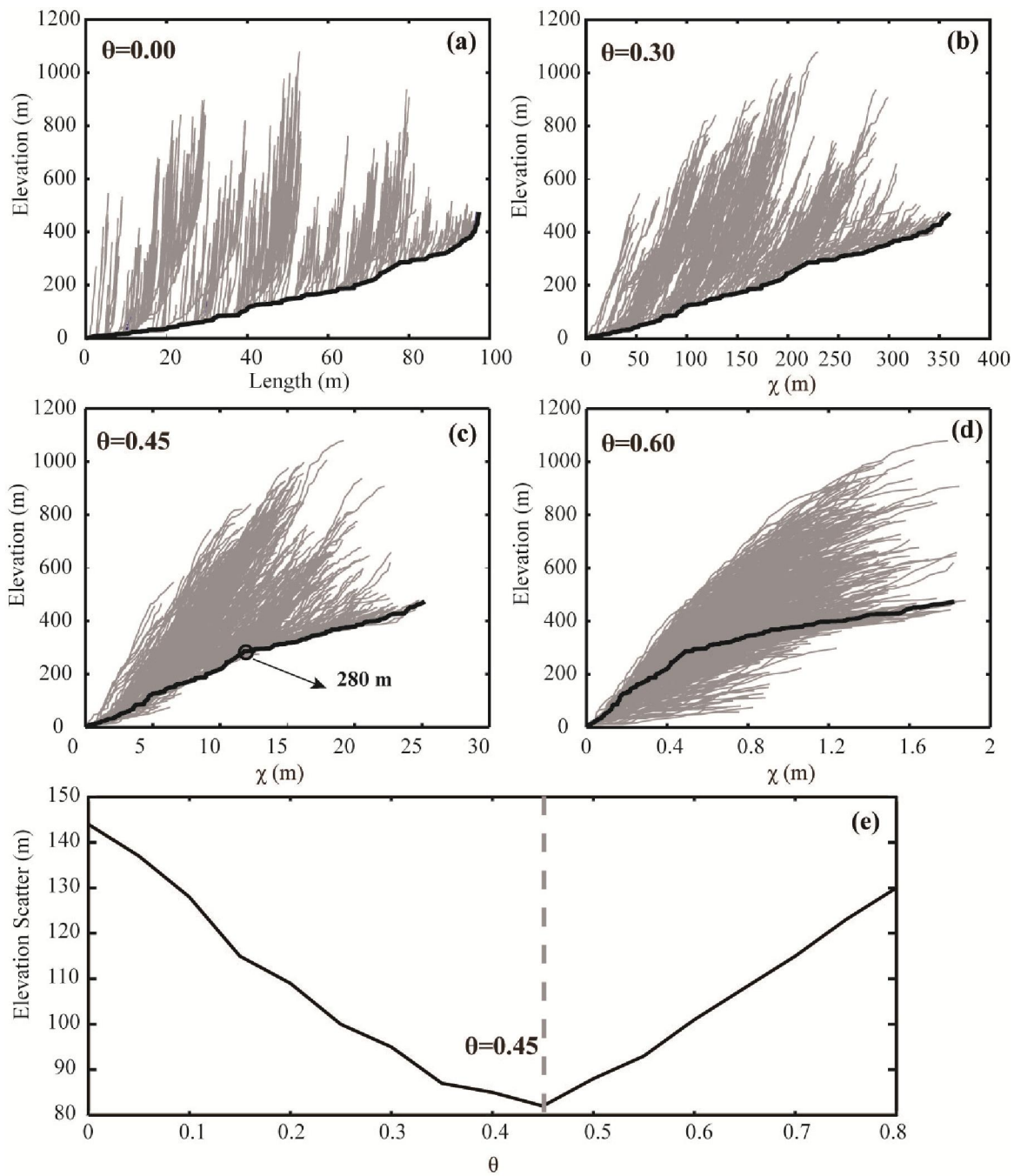


Figure 18. Concavity values that maximize the co-linearity of the main stem with its tributaries. (a)-(d) The χ - z plots of the stem (black line) and its tributaries (gray lines) using different values of θ ($A_{cr}=0.1 \text{ km}^2$, and $A_\theta=1 \text{ m}^2$). (e) The elevation scatter of the χ - z plots showing that minimum scatter is achieved with $\theta=0.45$.

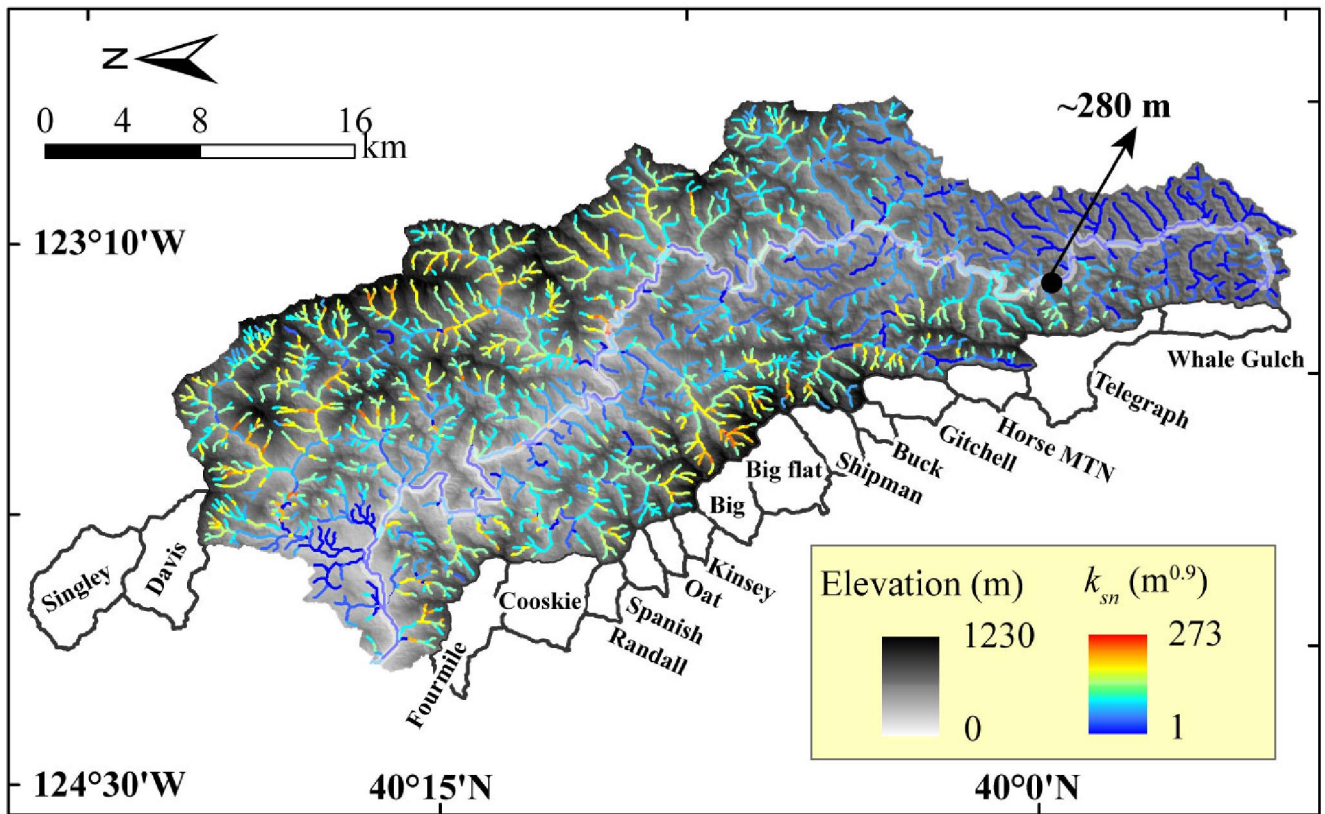


Figure 19. The map of k_{sn} ($\theta=0.45$, elevation interval of 100 m) of the Mattole drainage basin. The black circle indicates the knickpoint on the stem. Low values are shown along the whole stem and its tributaries above the knickpoint. High k_{sn} values are distributed along the upstream of the tributaries below the knickpoint.