## Supplementary Material: Colluvial deposits as a possible weathering reservoir in uplifting mountains

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#### 1 Non-dimensionalisation

<sup>2</sup> In the main manuscript we developed the formulae for the erosion-sedimentation mass bal-

ance only. Here we give the whole set of non-dimensional equations including in situ regolith
 thickness and clast weathering.

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#### Erosion-sedimentation mass balance

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On a cell, the change in elevation obeys

 $elev. \ change = river \ eros. + river \ depos. - hillslope \ eros. + hillslope \ depos. - lateral \ eros. + uplift$  $\frac{\partial z}{\partial t} = -Kq^m S^n + \frac{q_{sr}}{\xi q} - \kappa S + \frac{q_{sh}}{\frac{dx}{1 - (S/S_c)^2}} - \frac{dq_{sl}}{dx} + U$ (1)

9 Using these scaling factors:

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- <sup>11</sup> H mountain height,
- $_{12}$  L mountain width,
- $^{13}$  P precipitacion rate,
- 14 U uplift rate,
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16 non-dimensional variables (with a star) are defined by:

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$$q = q_*PL, q_{sr} = q_{sr*}UL, q_{sh} = q_{sh*}UL, q_{sl} = q_{sl*}UL, S = S_*\frac{H}{L}, dx = dx_*L, z = z_*H,$$
  
19  $t = t_*\frac{H}{U},$ 

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so that Equation 1 becomes:

$$\frac{\partial z_*}{\partial t_*} = -N_{riv} q^m_* S^n_* + N_{depo} \frac{q_{sr*}}{q_*} - N_{hill} S_* + \frac{q_{sh*}}{\frac{dx_*}{1 - (S_*/S_{c*})^2}} - \frac{dq_{sl*}}{dx_*} + 1$$
(2)

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with the following non-dimensional numbers:

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Rivers erosion:  $N_{riv} = KU^{-1}P^m L^{m-n}H^n$ 

- <sup>25</sup> Rivers sedimentation:  $N_{depo} = \xi^{-1} P^{-1}$
- <sup>26</sup> Hillslope erosion:  $N_{hill} = \kappa H U^{-1} L^{-1}$
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Other non-dimensional numbers include the slope threshold  $S_c$  and proportionality factor  $\alpha$  in the lateral erosion law.

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A similarity is expected between the numerical experiments sharing identical values of  $N_{riv}$ ,  $N_{depo}$ ,  $N_{hill}$ ,  $S_c$  and  $\alpha$ .

With m = 0.5 and n = 1 (Whipple and Tucker, 1999) the non-dimensional numbers become:

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<sup>37</sup> Rivers erosion:  $N_{riv} = KU^{-1}P^{0.5}L^{-0.5}H$ <sup>38</sup> Rivers sedimentation:  $N_{depo} = \xi^{-1}P^{-1}$ 

<sup>39</sup> Hillslope erosion:  $N_{hill} = \kappa H U^{-1} L^{-1}$ 

#### 41 Regolith production

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The variation in the regolith thickness is the sum of the regolith production rate, erosion and deposition rates by the river and hillslope processes:

$$\frac{\partial B}{\partial t} = w - Kq^m S^n + \frac{q_s}{\xi q} - \kappa S + \frac{q_s}{\frac{dx}{1 - (S/S_c)^2}} - \frac{dq_{sl}}{dx}$$
(3)

Using the maximum regolith formation rate  $w_{op}$  (for optimum) as a scaling parameter for w, and the same scalings as for equation 2 we obtain

$$\frac{\partial B_*}{\partial t_*} = N_{reg} w_* - N_{riv} q_*^m S_*^n + N_{depo} \frac{q_{sr*}}{q_*} - N_{hill} S_* + \frac{q_{sh*}}{\frac{dx_*}{1 - (S_*/S_{c*})^2}} - \frac{dq_{sl*}}{dx_*}$$
(4)

where the non-dimensional number  $N_{reg} = \frac{w_{op}}{U}$  determines whether or not regolith exists at dynamic equilibrium.  $N_{reg} > 1$  produces a regolith-covered mountain, whereas  $N_{reg} < 1$ leads to a bare-bedrock mountain (see Carretier et al., 2014, for details).

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#### 51 Clast weathering

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53 The rate of mineral volume decrease is

$$\frac{\partial v_m}{\partial t} = -w_m \tag{5}$$

Using the following equation for  $w_m$ 

$$w_m = \frac{P}{P_0} \left[ V_m \ \lambda \ 4\pi r_m^2 \ k_m \ e^{E_a \left(\frac{1}{R \ 298.15} - \frac{1}{R \ T}\right)} \right] \tag{6}$$

<sup>55</sup> equation 5 can be written as

$$\frac{\partial v_m}{\partial t} = -\frac{1}{\tau_m} v_m \tag{7}$$

<sup>56</sup> where the characteristic time scale for mineral dissolution is

$$\tau_m = \frac{r_m}{3 \frac{P}{P_0} V_m \lambda k_m e^{E_a (\frac{1}{R \, 298.15} - \frac{1}{R \, T})}} \tag{8}$$

A characteristic time scale for the mineral residence in the regolith on the hillslopes at dynamic equilibrium ( $\epsilon = U$ ) is  $\tau_r = \frac{B_o}{U}$  (e.g. Granger et al., 1996), where  $B_o$  is the equilibrium regolith thickness. It is not easy to derive  $B_o$  from Equation 3. We simplify it by considering erosion only and by neglecting the hump in the regolith production law ( $k_1 = 0$ ). At dynamic equilibrium,  $\epsilon = U$  and we obtain:

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$$B_o \sim d_1 \ln(\frac{w_o}{U}) \tag{9}$$

where  $w_o$  represents the kinetic dependence of the regolith production law given by 64

$$w_o = k_{\rm w} \frac{P}{P_{\rm o}} \left[ e^{\frac{-E_{\rm a}}{R} \left( \frac{1}{T} - \frac{1}{T_{\rm o}} \right)} \right]$$
(10)

Dividing  $\tau_r$  by  $\tau_m$ , we obtain a non-dimensional number

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$$N_{clast} = 3 \frac{P}{P_{o}} d_{1} ln(\frac{w_{o}}{U}) V_{m} \lambda k_{m} e^{E_{a}(\frac{1}{R^{298.15}} - \frac{1}{R^{T}})} r_{m}^{-1} U^{-1}$$
(11)

This Damköholer number indicates the weathering grade of a clast leaving the hillslopes. When  $N_{clast}$  is large, a clast leaving the regolith is very depleted, while it remains fresh if  $N_{clast}$  is small. The first situation has been called a "supply" or "transport" or "erosion" limited weathering (e.g. Dixon et al., 2009). The second situation has been called a "kinetr\_1 ically" limited regime.

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#### <sup>74</sup> 2 Illustration of the similarity of the experiments

The similarity between the numerical experiments with different parameters but sharing the same non-dimensional numbers is illustrated by Figure S5 in the case where the mountain is covered by regolith at dynamic equilibrium  $(N_{reg} > 1)$  and the case where no regolith remains  $(N_{reg} < 1)$ .

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$N_{reg} = \frac{w_{op}}{U}$	regolith production efficiency
$N_{riv} = K U^{-1} P^{0.5} L^{-0.5} H$	river erosion efficiency
$N_{depo} = \xi^{-1} P^{-1}$	river deposition efficiency
$N_{hill} = \kappa H U^{-1} L^{-1}$	hillslope erosion efficiency
$S_c$	hillslope non-deposition efficiency
$\alpha$	lateral erosion efficiency
$N_{clast} = 3 P d_1 \ln(\frac{w_o}{U}) V_m \lambda k_m e^{E_a(\frac{1}{R  298.15} - \frac{1}{R  T})} r_m^{-1} U^{-1}$	clast weathering efficiency
	(Damköholer number)

Tab. S1: Synthesis of non-dimensional numbers.

In the first case, the regolith production rate is large enough to form and maintain a 80 regolith even when the erosion rate reaches the uplift rate value, so that  $N_{reg} > 1$ . We 81 compare two sets of parameters indicated in Figure S5. The different parameters are the 82 erosion coefficient parameters, uplift rate, precipitation rate, mountain width, and clasts 83 (albite mineral) size. The regolith production law is kept the same in both cases. Five thou-84 sand clasts are seeded between 0 and 4 m at the beginning, and then recycled. Note that we 85 impose a constant temperature and precipitation rate with time and elevation, so that the 86 regolith production law is the same everywhere in the mountain. Despite different evolution 87 times and magnitudes of relief, erosion and weathering fluxes, both sets of parameters lead to 88 the same evolution once these variables are normalised. In particular, the ratio between the 89 regolith residence time and mineral dissolution time  $(N_{clast})$  is the same in both cases. This 90 similitude allows the weathering outflux to evolve in the same way, i.e. to increase regularly 91 with the erosion rate. This situation corresponds to the "erosion" or "supply" limited regime. 92 93

In the second case, the regolith production rate is much lower, so that the regolith production rate does not keep pace with the increasing erosion rate (Figure S5). Thus, the regolith developed in the early stage of the mountain erosion finally disappears (see also Carretier et al., 2014). This corresponds to  $N_{reg} < 1$ . Note that in this case, there is no regolith, so  $N_{clast}$  is not defined. This situation corresponds to the "kinetically" limited regime.

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This analysis has limitations when the weathering varies with the elevation. For example, 101 the cooling of the surface temperature imposed by the mountain uplift decreases the regolith 102 production rate through time. This decrease will be more pronounced in high mountains 103 than in low mountains. During the rise of high mountains, the initial regolith that formed 104 at low (warm) elevations may rapidly disappear. On the contrary it may continue to cover 105 the low mountains. The weathering outflux will evolve differently in both cases. In these 106 cases,  $N_{clast}$  and  $N_{reg}$  are calculated using the temperature and precipitation at base level 107 of the final topography. 108

# <sup>109</sup> 3 Pedon scale: Comparison with the data for the Santa <sup>110</sup> Cruz terraces data (White et al., 2008)

Before exploring the weathering outflux at the mountain scale, we tested the model at the pedon scale, using the data of four uplifted marine terraces of Santa Cruz, California, studied by *White et al.* White et al. (2008). These authors obtained depth profiles of the resid-



Fig. S1: Illustration of the similarities between some experiments sharing the same nondimensional numbers as in Table S1 but with different mountain widths, uplift and precipitation rates, clast radiuses, erosion and weathering parameters. (A)- Topography and maximum elevation at steady-state for models a-c and b-d. (B)- Parameters used for each experiment. Models a and b share the same non-dimensional numbers as do models c and d. (C)- Evolutions of the mean regolith thickness, erosion rate, weathering rate in a and b. (D)- Similarity between models a and b for which the time was divided by the time to reach steady-state, and the erosion and weathering rates by their maximum value. (E)- Same as (C)- for models c and d. (F)- Same as (D)- for models c and d.  $N_{reg} > 1$  (models a-b) means that the regolith covers the mountain even at a large erosion rate, which is not the case for models c and d for which  $N_{reg} < 1$ .

<sup>114</sup> ual amount of albite showing increasing depletion with increasing terrace age. White et al. <sup>115</sup> White et al. (2008) applied a transport-reactive model including the water flow, reaction <sup>116</sup> rate constant for each mineral, reactive surface area based on the spherical minerals and the <sup>117</sup> roughness coefficient  $\lambda$ , mineral solubility, thermodynamic disequilibrium between the rock <sup>118</sup> and fluid. Their modelled profiles for the residual amount of albite is reproduced in Figure <sup>119</sup> S2A.

In order to model these profiles with Cidre, we started with clasts of albite located every 10 cm below the surface. Their initial radius is from White et al. (2008). We use the reaction rate constant estimated by White et al. (2008) for albite and each terrace, and the same  $\lambda = 160$ . We impose a constant regolith production rate calculated by White et al. (2008) for each terrace (Table S2). The erosion rate is assumed to be zero as in *White et al.*'s model. Contrary to *White et al.*'s model, our model does not include the thermodynamic disequilibrium between the rock and fluid (always maximum disequilibrium).

 $k_m e^{E_a(\frac{1}{R\,298.15} - \frac{1}{R\,T})}$  $w_o \ (m \ a^{-1})$  $r_m$  (m) Terrace age (ka)  $(mol m^{-2} s^{-1})$ SCT1 65 8.00E-016 3.85E-0051.80E-004SCT290 5.44E-0051.40E-0151.45E-004SCT3 1375.34E-0058.00E-016 1.23E-004 SCT52263.64E-0054.80E-0169.50E-005

Tab. S2: Cidre parameters used to model the Santa Cruz depletion profiles (Figure S2)

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Following White et al. (2008), we calculate the model profile using the parameters determined for one terrace, and we also calculate the profiles for the other terraces predicted by using the same parameters and different ages.

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The predicted profiles fit the data relatively well for each terrace. The depletion profiles display angular extremities, differently from *White et al.*'s model, which shows sigmoid profiles. This difference arises from the assumption that the fluid-rock disequilibrium is always maximum in Cidre (White et al., 2008; Brantley and Lebedeva, 2011).

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Both *White et al.*'s model and the Cidre model show significant misfit for the other terraces when using the parameters calibrated on one of them. This misfit was attributed to time variations in the fluid flow by White et al. (2008). The fit is slightly better for Cidre for the youngest and oldest terraces. For the younger terrace, a significantly lower flow (precipitation) rate was estimated by White et al. (2008) In order to take this drier condition into account In Cidre, we simply use a smaller regolith production rate.



Fig. S2: Test of Cidre at the pedon scale using data from four marine terraces of different ages close to Santa Cruz, California from White et al. (2008). (a-) Depth profiles of the percentage of residual albite and adjusted models of White et al. (2008). For each terrace, the model was adjusted to the corresponding profile (solid lines), and the other profiles that were predicted using the same adjusted parameters and different times (dashed lines) (see details in White et al., 2008). The grey area is the area between the oldest and youngest profiles. Modified from White et al. (2008). (b-) Modelled profiled obtained using Cidre, initially setting albite clasts at depth in the fresh parent rock.

## <sup>145</sup> 4 Complementary Table

Tab. S3: Synthesis of main model parameters.	
$w_o [\mathrm{LT}^{-1}]$	saprolite production rate of exposed bedrock
$k_w [\mathrm{LT}^{-1}]$	kinetic weathering for exposed bedrock
$k_1 \ [\mathrm{LT}^{-1}]$	factor decreasing the saprolite production rate of exposed bedrock
$d_1$ [L]	parameter controlling the decrease in $w$ at large depth
$d_2$ [L]	parameter controlling the increase in $w$ at shallow depth
$T \left[ \theta \right]$	temperature at see level
$K  [\mathrm{T}^{-0.5}]$	river erosion coefficient
$\xi  [\mathrm{TL}^{-1}]$	parameter of the river transport length
$\kappa  [\mathrm{LT}^{-1}]$	diffusion coefficient: m $a^{-1}$
$S_c$ [1]	critical slope for sediment deposition
$\alpha$ [1]	factor controlling the lateral erosion
$P [\mathrm{LT}^{-1}]$	precipitation rate
$U [LT^{-1}]$	uplift rate
dx [L]	cell size
r [L]	clast radius
$V_m \left[ \mathrm{L}^3 \mathrm{N}^{-1} \right]$	molar volume of mineral $m$
$k_m \left[ \mathcal{N} \mathbf{L}^{-2} \mathbf{T}^{-1} \right]$	dissolution parameter of mineral $m$
$E_a \left[ \mathrm{M}^2 \mathrm{T}^{-2} \mathcal{N}^{-2} \right]$	activation energy
$\lambda$ [1]	mineral roughness coefficient

### <sup>147</sup> 5 Complementary Figures



Fig. S3: Effect of increasing the diffusion coefficient  $\kappa$  by 100  $(N_{hill} \ge 100)$  in experiment COOLING.  $\alpha$ =0.001. (a-) Despite different values for the non-dimensional parameter  $N_{hill}$ , the weathering outfluxes follow similar evolutions. This comparison illustrates that the weathering outflux follows the same humped evolution passing by a maximum weathering outflux and then that colluvial deposits produce the same significant weathering outflux whatever  $N_{hill}$  is. (b-) Topography (relief  $\ge 2$ ) and sediment thickness at 20 Ma for the COOLING experiment. (b-) The same for  $N_{hill} \ge 100$ .



Fig. S4: Effect of increasing the transport length coefficient  $\xi$  by 3 ( $N_{depo}$  / 3) in experiment COOLING.  $\alpha$ =0.001. (a-) Increasing the transport length, there is less deposition. Consequently, the sediment thickness in valley borders is smaller and the weathering outflux associated with colluvium is lower. The second effect of increasing the transport length is to increase the lateral erosion. Indeed, lateral erosion is proportional to the sediment flux. The sediment flux is greater if there is less deposition, thus the lateral erosion increases. Consequently, rivers are more straight and the residence of sediment in the river is shorter. This second effect contributes also to lower the weathering outflux associated with the weathering of colluvium. Note that the relief in the experiment with  $\xi \ge 3$  appears less realistic than in the COOLING experiment. Yet, the colluvial deposits produce all the weathering outflux during the cold period. This comparison illustrates that the weathering outflux follows the same humped evolution passing by a maximum weathering outflux and then that colluvial deposits produce a significant weathering outflux, although the value of this flux is lower for smaller  $N_{depo}$ . (b-) Topography (relief  $\ge 2$ ) and sediment thickness at 20 Ma for the COOLING experiment. (b-) The same for  $\xi \ge 3$  ( $N_{depo} / 3$ ).



Fig. S5: Effect of increasing the model resolution for experiment OROGRAPHIC with a rainfall peak at 2000 m. The experiment OROGRAPHIC presented in the main manuscript has 300x200 cells of size 500 m. The other experiment has 700x500 cells of size 200 m. The lateral erosion parameter  $\alpha$  is 2.5 times smaller. (a-) The weathering rate follows a similar evolution in both cases, but the experiment with the smaller cells ends up with a smaller weathering rate associated with colluvium weathering, resulting from the smaller lateral erosion parameter decreasing the volume of colluvium. This comparison shows that decreasing the cell size does not change fundamentally the fact that the weathering outflux follows the same humped evolution passing by a maximum weathering outflux and then that colluvial deposits produce a significant weathering outflux during the cold period, even in a more penalizing experiment with smaller lateral erosion. (b-) Topography and sediment thickness at 20 Ma in the OROGRAPHIC simulation using dx=500 m. (c-) The same for the OROGRAPHIC simulation using dx=200 m.

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