



1 **Theoretical Interpretation of the Exceptional Sediment**  
2 **Transport of Fine-grained Dispersal Systems Associated with**  
3 **Bedform Categories**

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10

11 **Abstract.** Being a widespread source-to-sink sedimentary environment, the fine-grained dispersal system (FGDS)  
12 features remarkably high sediment flux, interacting closely with local morphology and ecosystem. Such exceptional  
13 transport is believed to be associated with changes in bedform geometry, which further demands theoretical  
14 interpretation. Using van Rijn (2007a) bed roughness predictor, we set up a simple numerical model to calculate  
15 sediment transport, classify sediment transport behaviors into dune and (mega-)ripple dominant regimes, and discuss  
16 the causes of the sediment transport regime shift linked with bedform categories. Both regimes show internally  
17 consistent transport behaviors, and the latter, associated with FGDSs, exhibits considerably higher sediment transport  
18 rate than the previous. Between lies the coexistence zone, the sediment transport regime shift accompanied by  
19 degeneration of dune roughness, which can considerably reinforce sediment transport and is further highlighted under  
20 greater water depth. This study can be applied to modeling of sediment transport and morphodynamics.

21

22 **1 Introduction**

23 Shaped by fine-grained (median grain size  $d = 15 \sim 150 \mu\text{m}$ , i.e.  $6.0 \sim 2.7 \phi$ ) bed, the fine-grained dispersal system  
24 (FGDS) is a type of sedimentary environment that is rooted in coastal, riverine, deltaic, marine, and subglacial systems,  
25 as well as characterized by remarkably high total sediment fluxes (Ma et al., 2017). In science and engineering  
26 disciplines, FGDSs are of great importance because they are crucial source-to-sink systems, highlighting the unique  
27 role that suspended sediment transport processes play in developing phenomenal sediment transport. Generated from  
28 erosion in sources (mountains and riverbeds), transported as suspended load, and eventually preserved at sinks (coastal  
29 zone, continental shelves, and deep seas) (Kuehl et al., 2016; Leithold et al., 2016), riverine fine sediments increase  
30 turbidity of estuarine and nearshore waters, forming mud depositional systems of considerable thickness (Gao &  
31 Collins, 2014; Wright, 1995). The source-to-sink processes these sediments undergo not only notably alter local  
32 sediment dynamic environments (Wright & Nittrouer, 1995), material cycling processes (Blair & Aller, 2012; Kuehl  
33 et al., 2016), and ecosystems (Venkatesan et al., 2010), but will shape a distinctive sedimentary system over a long



34 time span as well (Gao & Collins, 2014). In addition, knowledge of FGDS will be of great benefit to tackling real-  
35 time engineering issues, including navigation channel dredging (van Maren et al., 2015), harbor construction  
36 (Winterwerp, 2005), monitoring morphological responses of tidal flat reclamation (Lee et al., 1999; Wang et al., 2012),  
37 and predicting coastline changes (Mangor et al., 2017).

38 Over the past century, established works of sediment transport (e.g. Engelund & Hansen, 1967; Julien, 2010; Soulsby,  
39 1997; van Rijn, 1993) has illustrated total sediment transport from a general perspective including both coarse and  
40 fine components. However, recently Ma et al. (2017) reports exceptionally higher sediment transport rate in Huanghe  
41 (also known as Yellow River; a FGDS) linked with its fine bed than that in coarse bedded flumes (Guy et al., 1966).

42 Starting from the Engelund-Hansen sediment transport formula (Engelund & Hansen, 1967) founded on the same  
43 flume data set, Ma et al. (2017) derive a generalized Englund-Hansen (GEH) formula of suspended sediment transport  
44 based on energy conservation theory, excluding the wash load, the fraction of suspended load that almost does not  
45 communicates with local bed and flow (Chien & Wan, 1999):

$$46 \quad C_D q_s^* = \alpha \theta_b^n \quad (1)$$

47 where  $C_D$  is the total bed drag coefficient;  $q_s^* = \frac{q_s}{\rho_s \sqrt{(s-1)gd^3}}$  is the dimensionless sediment transport rate, i.e. Einstein  
48 number;  $q_s = S \cdot uh$  is the suspended sediment transport rate by mass, and  $S$  is the vertically averaged suspended  
49 sediment concentration (SSC);  $\theta_b = \frac{\tau_b}{(\rho_s - \rho)gd}$  is the dimensionless total bed shear stress, i.e. Shields (1936) number;  
50  $\tau_b = \rho C_D u^2$  is the total bed shear stress;  $\alpha$  is the coefficient of  $\theta_b$ , and  $n$  is the exponent of  $\theta_b$ ;  $s = \rho_s/\rho$  is the specific  
51 gravity of sediment grains;  $g$  is the gravitational acceleration;  $c$  is the total sediment concentration by mass.

52 By linking Huanghe and the flume data with the GEH formula, Ma et al. (2017) find similar  $\alpha$  and  $n$  values for distinct  
53 zones of  $d$  (for Huanghe data,  $d < 130 \mu\text{m}$ ,  $\alpha = 0.895$ ,  $n = 1.678$ ; for the flume data,  $d > 190 \mu\text{m}$ ,  $\alpha = 0.0355$ ,  $n = 3.0$ );  
54 these zones containing data points representing similar sediment transport behaviors ( $\alpha$  and  $n$  values) can be identified  
55 as sediment transport regimes. In between lies a narrow transition zone, where exceptionally high sediment load is  
56 initiated as  $d$  becomes finer. Furthermore, they suggest that such phenomenal sediment transport is associated with  
57 the absence of dune by relating sediment transport regimes to bathymetry data of lower Huanghe ( $d = 90 \mu\text{m}$ , low  
58 bedform height) and lower Mississippi River ( $d = 280 \mu\text{m}$ , significant dune presence).

59 Notwithstanding these recent advances, a quantitative theoretical interpretation of the relationship between sediment  
60 transport regimes and prevailing bedforms is still absent, yet achievable through parameterizing the relationship  
61 between bedform geometry and sediment transport rate. Unlike preceding semi-empirical ways, we try to interpret the  
62 mentioned problems with sediment dynamic theories that bridge the gap between bedform prediction and sediment  
63 transport modeling. In this paper, we first set up a sediment transport model based upon van Rijn (2007a) bedform  
64 roughness predictor, then analyze the model calculation results to classify sediment transport behaviors into two  
65 regimes and a transition zone, and finally discuss the causes of the regime shift in sediment transport associated with  
66 bedform changes.

67



68 **2 Methods**

69 2.1 Theories

70 In order to estimate the sediment transport in FGDSs associated with bedform changes, a numerical model is set up  
 71 to calculate values of variables in the GEH formula, so as to explore the relationship between the suspended sediment  
 72 transport rate  $q_s$ , a proper approximation of total sediment flux when  $d < 250 \mu\text{m}$  (van Rijn, 2007a), and dimensionless  
 73 total bed shear stress  $\theta_b$ .

74 The suspended sediment transport rate  $q_s = S^*uh$  is controlled by depth-averaged flow speed  $u$  and SSC  $S^*$ , which is  
 75 particularly governed by their vertical profiles. Based on the basic assumptions that (1) currents are the sole driving  
 76 force of sediment transport, (2) flows over the bed are unstratified, and (3) suspended sediment transport dominates  
 77 total sediment transport when  $d < 250 \mu\text{m}$ , the logarithmic law of the wall:

78 
$$U(z) = \frac{u_*}{\kappa} \ln\left(\frac{z}{z_0}\right) \quad (2)$$

79 and the Rouse (1937) profile:

80 
$$\begin{cases} c(z) = c_a \left( \frac{z}{z_a} \frac{h-z_a}{h-z} \right)^{-b} \\ b = \frac{w_s}{\kappa u_*} \end{cases} \quad (3)$$

81 are utilized in this model to derive  $u$  and  $S^*$ , directing to the final estimate of total sediment transport rate.

82 In the law of the wall,  $U(z)$  stands for the horizontal flow speed at height  $z$  to the bed,  $u_* = \sqrt{\tau_b/\rho} = \sqrt{C_D} \cdot u$  is the  
 83 friction velocity,  $\kappa = 0.4$  denotes the von Kármán constant, and  $z_0$  refers to the total roughness length. In the Rouse  
 84 profile,  $c(z)$  symbolizes the suspended sediment concentration at height  $z$  to the bed,  $c_a$  signifies the reference  
 85 concentration (i.e. the SSC at reference height  $z_a$ ) by mass;  $b$  represents the Rouse number, which is decided by  $u_*$   
 86 and  $w_s$ , the settling velocity of bed sediment.

87 Being the average of  $U(z)$ ,  $u$  is linked to  $C_D$  (related to  $u_*$  and  $z_0$ ) and  $\tau_b$  (related to  $u_*$ ). Similarly,  $S^*$  is associated  
 88 with the ripple roughness height  $k_{s,r}$  (related to  $z_a$ ),  $d$  (related to  $c_a$  and  $w_s$ ),  $C_D$  (related to  $u_*$ ),  $\tau_b$  (related to  $u_*$ ), and  
 89 skin bed shear stress  $\tau_{bs} = \rho C_{Ds} u^2$  (related to  $c_a$ ). Given vertically averaged flow speed  $u$ , median bed grain size  $d$ ,  
 90 and water depth  $h$ , we still need to figure out total bed drag coefficient  $C_D$ , skin bed drag coefficient  $C_{Ds}$ , and ripple  
 91 roughness height  $k_{s,r}$  to finish the calculation of sediment transport rate.

92  $C_D$  is a function of total bed roughness height  $k_s = 30 z_0$  and water depth  $h$  (Soulsby, 1997):

93 
$$C_D = \left[ \frac{\kappa}{1 + \ln\left(\frac{z_0}{h}\right)} \right]^2 = \left[ \frac{\kappa}{1 + \ln\left(\frac{k_s}{30h}\right)} \right]^2 \quad (4)$$

94 Likewise,  $C_{Ds}$  is a function of grain roughness height  $k_{s,g} = 2.5 d$  (Nikuradse, 1933) and water depth  $h$  (Soulsby, 1997):

95 
$$C_{Ds} = \left[ \frac{\kappa}{1 + \ln\left(\frac{k_{s,g}}{30h}\right)} \right]^2 = \left[ \frac{\kappa}{1 + \ln\left(\frac{d}{12h}\right)} \right]^2 \quad (5)$$



96  $k_{s,g}$  and  $k_s$  symbolize bed friction from different perspectives. The grain roughness  $k_{s,g} = 2.5d$  is only related to the  
97 grain size of bed sediments, referring to skin friction on the bed, whereas the total bed roughness height  $k_s$  is estimated  
98 in relation to bedform size, a function of the mobility parameter  $\Psi = \frac{u^2}{(s-1)gd}$  (Manohar, 1955) and water depth  $h$  (van  
99 Rijn, 2007a).

100  $k_s$  is composed of three components, namely ripple roughness height  $k_{s,r}$ , megaripple roughness height  $k_{s,mr}$ , and dune  
101 roughness height  $k_{s,d}$  (van Rijn, 2007a). In this study, as the mobility parameter  $\Psi$  increases,  $k_{s,r}$  was linearly weakened  
102 from  $150d$  to  $20d$ , while both  $k_{s,mr}$  and  $k_{s,d}$  first grow from zero and then decrease. Subsequently, when  $\Psi$  is very large  
103 (over 600),  $k_{s,mr}$  remains  $0.02f_{fs}$  ( $f_{fs}$  denotes fine sand factor. For  $d \geq 100 \mu\text{m}$ ,  $f_{fs} = 1$ ; for  $d < 100 \mu\text{m}$ ,  $f_{fs} = 10000d$ ), a  
104 value usually larger than  $k_{s,r}$  by an order of magnitude, whereas  $k_{s,d}$  is cleared. In this regard,  $k_{s,d}$  is normally  
105 predominant in  $k_s$  when  $\Psi$  is small, but no longer exists when  $\Psi \geq 600$ .

106 In addition,  $k_{s,g}$  and  $k_s$  interact with the flow in different ways. Determined by  $k_{s,g}$ , the skin portion of bed shear stress  
107  $\tau_{bs} = \rho C_{Ds} u^2$  directly initiates sediment movement and suspension. Meanwhile, with a considerable input from form  
108 drag,  $k_s$  decides the total bed drag coefficient  $C_D$ , which (1) significantly increases total bed shear stress  $\tau_b = \rho C_D u^2 =$   
109  $\rho u^2$  by directing its majority to balancing bedform drag, and (2) motivates vertical distribution of turbulence, which  
110 resists vertical stratification and diminishes the Rouse number  $b$ . In this regard, changes in the mobility parameter  $\Psi$   
111 lead to different bedforms, which furthermore affect sediment transport rates.

112 For simplicity, our detailed algorithm is listed in Supporting Information S1 for readers' reference.

113

## 114 2.2 Model settings

115 For current-induced sediment transport in FGDSs, van Rijn (2007a) summarizes that  $q_s$ , the transport rate of suspended  
116 load, is larger by one order of magnitude than  $q_b$ , the transport rate of bedload, as long as the grain size  $d$  of bed  
117 sediment does not exceed  $250 \mu\text{m}$  ( $2.0 \phi$ ). To underscore the role suspended sediment transport plays in FGDSs, we  
118 set the upper boundary of bed sediment grain size  $d$  as  $250 \mu\text{m}$  ( $2.0 \phi$ ), so that  $q_s$  will remain a good approximation of  
119 the total sediment flux. As a non-cohesive modeling approach, the lower boundary of  $d$  here is placed at  $62.5 \mu\text{m}$  ( $4.0$   
120  $\phi$ ), the tipping point between sand and silt. Thus, in this numerical study, the grain size of bed sediment,  $d$ , ranges  
121 from  $4.0 \phi$  to  $2.0 \phi$ , with step length  $0.1 \phi$ .

122 In the same time, covering scenarios in real-time fluvial and coastal settings, the water depth  $h$  is continuously doubled  
123 from  $0.3125 \text{ m}$  to  $20 \text{ m}$ , and the vertically averaged horizontal flow speed  $u$  is increased from  $0.5 \text{ m/s}$  to  $1.5 \text{ m/s}$  at a  
124  $0.1 \text{ m/s}$  step size.

125

## 126 3 Results

127 With the above settings, we calculate ripple roughness height  $k_{s,r}$ , megaripple roughness height  $k_{s,mr}$ , dune roughness  
128 height  $k_{s,d}$ , total bed roughness height  $k_s$ , total bed drag coefficient  $C_D$ , dimensionless total bed shear stress  $\theta_b$ , and



129 dimensionless sediment transport rate  $q_s^*$  for each case that combines specific median grain size  $d$ , water depth  $h$ , and  
130 flow speed  $u$ . These calculation results are saved in Data Set S1.

131 To highlight the importance of regime shift in sediment transport, we present a log-log plot, featuring the relationship  
132 between  $C_D q_s^*$  (y-axis), the product of total bed drag coefficient  $C_D$  and dimensionless sediment transport rate  $q_s^*$ , and  
133 the dimensionless total bed shear stress  $\theta_b$ .

134

135 In Figure 1, data points on the same straight line share identical exponent  $n$  and coefficient  $\alpha$  of dimensionless bed  
136 shear stress  $\theta_b$  in the GEH formula ( $C_D q_s^* = \alpha \theta_b^n$ ), thus belong to a specific sediment transport regime. Based on this  
137 conclusion, data points are therefore categorized into dune dominant and (mega-)ripple dominant sediment transport  
138 regimes, according to their different transport behavior (as marked in ovals in each graph) and their predominant  
139 component of  $k_s$  (see Data Set S1); typical sediment transport behavior in FGDSs corresponds with the (mega-)ripple  
140 dominant regime (pink ovals).  $\alpha$  and  $n$  are subsequently calculated for both dune and (mega-)ripple dominant regimes  
141 in each case; they are listed in Data Set S1 as well. Sandwiched by these two regimes is the narrow coexistence zone,  
142 where sediment transport behavior is influenced by both regimes (Lapotre et al., 2017) and undergoes notable changes.

143

#### 144 **4 Discussion**

##### 145 4.1 The predominant bedform category of a sediment transport regime

146 As van Rijn (2007a) and our calculation suggest, we set  $\Psi = 400$  and  $\Psi = 600$  as criteria for defining bedform categories  
147 (Figure 2). In the dune region ( $\Psi < 400$ ), the dune roughness height  $k_{s,d}$  is predominant in the total bed roughness  
148 height  $k_s$ , whereas  $k_{s,d}$  diminishes rapidly in the transition zone ( $400 \leq \Psi < 600$ ) and ultimately stays zero in the  
149 (mega-)ripple region ( $\Psi \geq 600$ ) (Figure 3); the megaripple roughness height  $k_{s,mr}$  takes control of  $k_s$  then.

150 Based on the classification of bedform categories, we further propose related cut-off points for sediment transport  
151 regimes. For typical flow speed values ( $u \in [0.5, 1.5]$  (m/s)) in fluvial and coastal environments, if a particular  
152 bedform category prevails (the contribution of such bedform data points counts for more than 50% on a grain-size-  
153 fixed bed), then the corresponding sediment transport regime is referred to this type of bedform. Hence,  $d = 3.22 \phi$   
154 and  $d = 2.63 \phi$  are identified as tipping points of sediment transport regimes (Figure 2).

155 Chien et al. (1987) took Yellow River (Huanghe) as an example and notice that, in FGDSs, bedform drag can be far  
156 greater than the skin part of total bed friction in lower flow regime, and will diminish considerably to almost zero in  
157 upper flow regime. As suggested above, sediment transport regimes are closely associated with the predominant  
158 bedform category. In the dune region ( $\Psi < 400$ , i.e. lower flow regime or coarse bed),  $k_{s,d}$  upholds a considerable  
159 weight (usually more than 50%, Figure 3) in  $k_s$ , leading to a larger total bed drag coefficient  $C_D$  and dissipating the  
160 majority of total bed shear stress  $\tau_b$  to overcoming significant dune friction; only a small fraction of total bed shear  
161 stress is utilized for suspended sediment transport. However, in the (mega-)ripple region ( $\Psi \geq 600$ , i.e. upper flow



162 regime or fine bed, the representative setting in FGDSs), dunes are destroyed ( $k_{s,d} = 0$ , Figure 3) by the flow over bed,  
163 which can reduce the total  $k_s$  by up to one order of magnitude and halve the total  $C_D$  (see Data Set S1). In the meantime,  
164 the importance of grain roughness  $k_{s,g}$  has increased, initiating the exceptional suspended sediment transport (Figure  
165 1). Therefore, we suggest that increased  $\Psi$  (stronger fluid flow or finer bed sediment) accelerates the degeneration of  
166 dunes and the considerable decline in  $C_D$ , greatly enhancing suspended sediment transport, finally shaping the two  
167 disparate sediment transport regimes (dune dominant and (mega-)ripple dominant).

168

#### 169 4.2 Comparison with measured data: Importance of water depth

170 Derived from field survey results in the Yellow River (Huanghe,  $h \approx 0.55 \sim 7.8$  m) and findings of Guy et al. (1966)'s  
171 (GSR) flume experiments ( $h \approx 0.06 \sim 0.40$  m), Ma et al. (2017) present Logistic curves, underlining sediment transport  
172 regime shifts, i.e. changes in exponent  $n$  and coefficient  $\alpha$  of dimensionless bed shear stress  $\theta_b$  in the GEH formula  
173 ( $C_D q_s^* = \alpha \theta_b^n$ ), with respect to bed sediment grain size  $d$ . Both  $n$  and  $\alpha$  are indicators of bedform geometry (Engelund  
174 & Hansen, 1967). In comparison with their results, our numerical experiments ( $h = 0.625 \sim 10$  m) illustrate similar  
175 trends in sediment transport regimes, regime shifts (coexistence zone), and estimated  $n$  and  $\alpha$  (Figure 4).

176 In our (mega-)ripple dominant regime of sediment transport ( $d = 3.22 \sim 4.0 \phi$ ), equivalent to their zone of suspended  
177 sediment domination (Huanghe data, with  $d$  finer than  $2.94 \phi$ ), our calculated mean  $n$  and  $\alpha$  are (2.3 ~ 2.8) and (0.10  
178 ~ 0.76) respectively, while theirs are 1.678 and 0.895 correspondingly. As for our dune dominant sediment transport  
179 regime ( $d = 2.0 \sim 2.63 \phi$ ), comparable to their sector of suspended load and bedload coexistence (GSR flume data,  
180 with  $d$  coarser than  $2.40 \phi$ ), our estimated mean  $n$  and  $\alpha$  are (3.5 ~ 4.6) and (0.028 ~ 0.033) correspondingly, whereas  
181 theirs are 3.0 and 0.0355 respectively. Both approaches suggest that for finer bed sediments, the exponent  $n$  is smaller,  
182 but the coefficient  $\alpha$  is larger; finer beds advocate remarkable efficiency and flux of suspended sediment transport. In  
183 view of the regime shift in sediment transport behavior, our results demonstrate a coexistence band with  $d = (2.63 \sim$   
184  $3.22) \phi$ , while they show a transition zone in  $d = (2.40 \sim 2.94) \phi$ .

185 Molinas & Wu (2001) point out the importance of water depth  $h$  in the original Engelund-Hansen (EH) formula.  
186 Derived out of Guy et al. (1966)'s flume experiment data, the original EH formula is only compliant with small water  
187 depths ( $h < 0.5$  m) and should be tested and even revised for larger  $h$ , due to differences in bedform development for  
188 small and large  $h$ . By grouping different typical  $d$ ,  $u$ , and  $h$  values in FGDSs in our calculation, we compensate for the  
189 lack of typical scenarios with different water depths in previous studies of FGDSs and furthermore demonstrate a  
190 diverging trend in data points for increasing water depths.

191 Given small water depths (e.g.  $h < 1$  m), dune ( $k_{s,d}$ ) and megaripple ( $k_{s,mr}$ ) components of total bed roughness height  
192  $k_s$  are comparable (Figure 3 & Data Set S1), regardless of the grain size  $d$  of bed sediment. Thus, although data points  
193 within a certain prevailing bedform (dune or (mega-)ripple) can indicate similar sediment transport behavior, it is not  
194 easy to tell apart different sediment transport regimes merely according to their data plots (Figure 1); the corresponding  
195 regime shift as reflected by  $n$  and  $\alpha$  (Figure 4) is not obvious as well. But in view of rising  $h$ , as the dune roughness  
196 height  $k_{s,d}$  becomes prevailing in the total bed roughness height  $k_s$  (Figure 3), dune dominant and (mega-)ripple



197 dominant sediment transport regimes commence to diverge (Figure 1, Figure 4), and the regime shift indicated by  $n$   
198 and  $\alpha$  (Figure 4) is thus more apparent.

199 Limited by room height, the water depth of flume experiments is usually on the order of ( $10^{-1} \sim 10^0$ ) m (Guy et al,  
200 1966), whereas fluvial (Ma et al, 2017) and coastal systems (Gao & Collins, 2014) feature a typical water depth on  
201 the order of ( $10^0 \sim 10^2$ ) m. As shown in van Rijn (2007a)'s formulae and our discussion above, the extent of bedform  
202 development and, consequently, the suspended sediment transport behavior are strongly influenced by water depth, in  
203 addition suggesting that a measured data set is comparable to another only if their water depths share the same order  
204 of magnitude. Hence, it is of great necessity to take water depth  $h$  into consideration in future studies of suspended  
205 sediment transport in FGDSs by distinguishing bedforms in small and large water depths.

#### 206 4.3 Future work

207 Our study is a preliminary numerical attempt to examine the unique sediment transport behavior of FGDSs. In reality,  
208 due to FGDSs' high SSC, vertical stratification is amplified to a considerable extent under small  $u$  (Baas et al., 2009);  
209 even  $C_D$  is not vertically uniform, and the logarithmic law of the wall and Rouse profile will then no longer applicable  
210 for the whole water column. Under this circumstance, the water column should be sliced into layers in which vertical  
211 stratification is insignificant, and a revised (Rodi & Mansour, 1993) second-order  $k$ - $\epsilon$  model can be applied to estimate  
212 the vertical profile of flow speed (Maa et al., 2016). As  $u$  increases, bolstered vertical mixing will undermine vertical  
213 stratification, and our model can be effective in estimating total sediment transport in FGDSs.

214

### 215 5 Conclusions

216 With the assumptions that sediment transport is only driven by unstratified steady uniform currents and that bedload  
217 transport is negligible, a numerical model is set up to inspect the relationship between terms in the GEH formula on  
218 both sides of the equal sign, i.e.  $C_D q_s^*$  and  $\theta_b$ . Sediment transport regimes are differentiated according to differences  
219 in sediment transport behavior as indicated by calculation data. Between dune dominant and (mega-)ripple dominant  
220 regimes lies the coexistence zone, the regime shift in sediment transport, which is related to the degeneration of dune  
221 component in total bed roughness  $k_s$ , considerably reinforcing suspended sediment transport as the flow mobility  
222 parameter  $\Psi$  increases. Additionally, greater water depth  $h$  highlights such regime shift. Our study can be applied to  
223 future modeling of sediment transport and morphological evolution.

224

#### 225 Code availability

226 The code used in this analysis is available as a Supplement.

227



228 **Data availability**

229 All data used in this analysis are available as a Supplement.

230

231 **Author contribution**

232 QY designed the study, TZ, QY and YW performed the research, TZ and QY wrote the paper, and SG supervised  
233 the research.

234

235 **Competing interests**

236 The authors declare that they have no conflict of interest.

237

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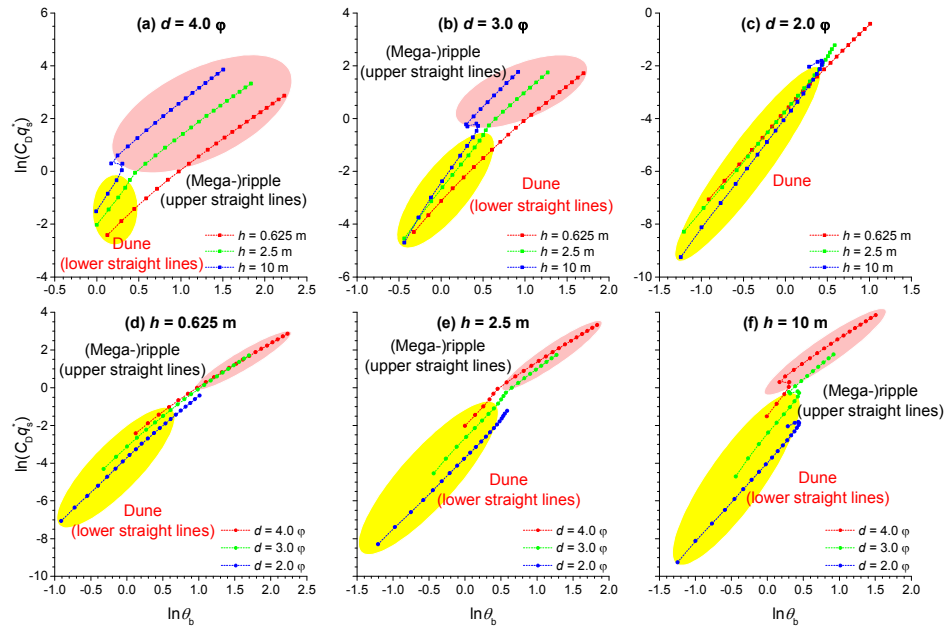




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321 **Figure 1: Log-log plotted relationships between y-axis: product ( $C_D q_s^*$ ) of total bed drag coefficient ( $C_D =$**

322  $\left[ \frac{0.4}{1 + \ln\left(\frac{k_s}{30h}\right)} \right]^2$ ) and dimensionless sediment transport rate ( $q_s^* = \frac{q_s}{\rho_s \sqrt{(s-1)gd^3}}$ , i.e. Einstein number), and x-axis:

323 dimensionless bed shear stress ( $\theta_b = \frac{\tau_b}{(\rho_s - \rho)gd}$ , i.e. Shields number), given specific combinations of typical bed

324 sediment grain size ( $d = 4.0, 3.0, 2.0 \phi$ ) and water depth ( $h = 0.625, 2.5, 10$  m) under fluvial, coastal, and flume

325 settings. Data points are categorized into dune dominant (lower straight lines) and (mega-)ripple dominant

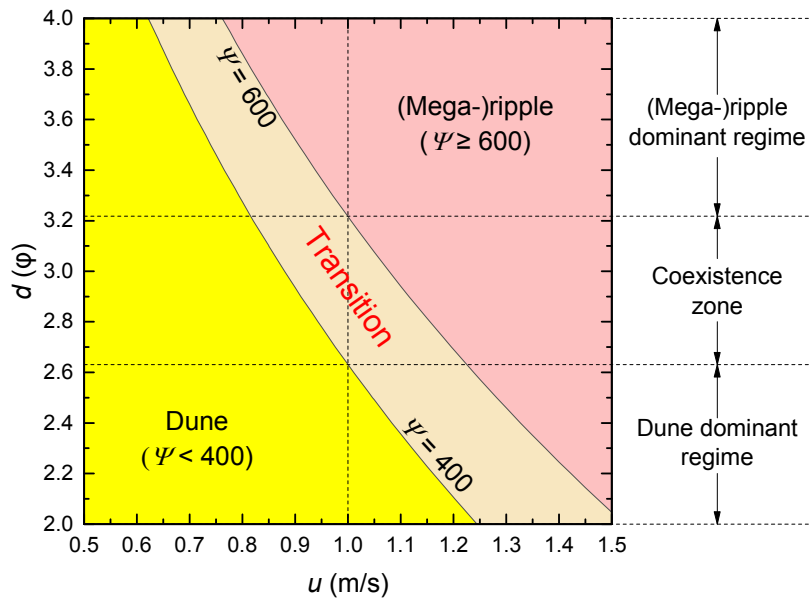
326 (upper straight lines, associated with typical sediment transport behavior in FGDSs) regimes, and the

327 coexistence (in-between shifts) zone, according to how the sediment transport behavior ( $C_D q_s^*$ ) responds to the

328 fluid flow ( $\theta_b$ ) through the bed. Bed sediment grain size fixed, the two regimes diverge as water depth increases

329 (a~c). The (mega-)ripple regime tend to vanish with respect to a coarser bed, regardless of the current water

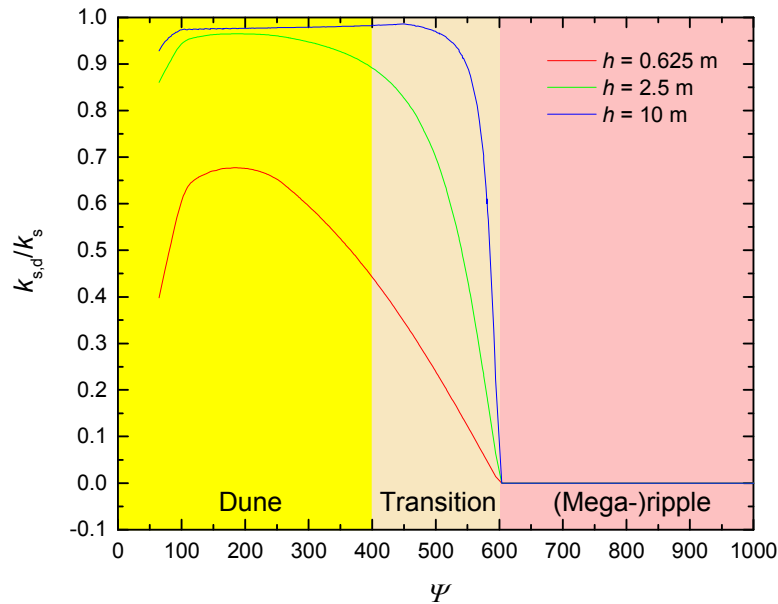
330 depth (d~f).



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332 **Figure 2: Bedform category as a function of flow mobility parameter ( $\Psi = \frac{u^2}{(s-1)gd}$ ).** Data points with specific  
 333  $\Psi$  values are classified as dune ( $\Psi < 400$ ), transition ( $400 \leq \Psi < 600$ ), and (mega-)ripple ( $\Psi \geq 600$ ) regions. For  
 334 typical vertical-averaged flow speed values ( $u \in [0.5, 1.5]$  (m/s)) in fluvial and coastal areas, sediment  
 335 transport over a particular grain-sized bed falls into: either a dominant regime (for (mega-)ripple dominant  
 336 regime,  $d = 3.22 \sim 4.0 \phi$ ; for dune dominant regime,  $d = 2.0 \sim 2.63 \phi$ ), as long as the contribution of  
 337 corresponding bedform data points exceeds 50%; or the coexistence zone ( $d = 2.63 \sim 3.22 \phi$ ), when both dune  
 338 and (mega-)ripple points fail to become predominant (>50%).

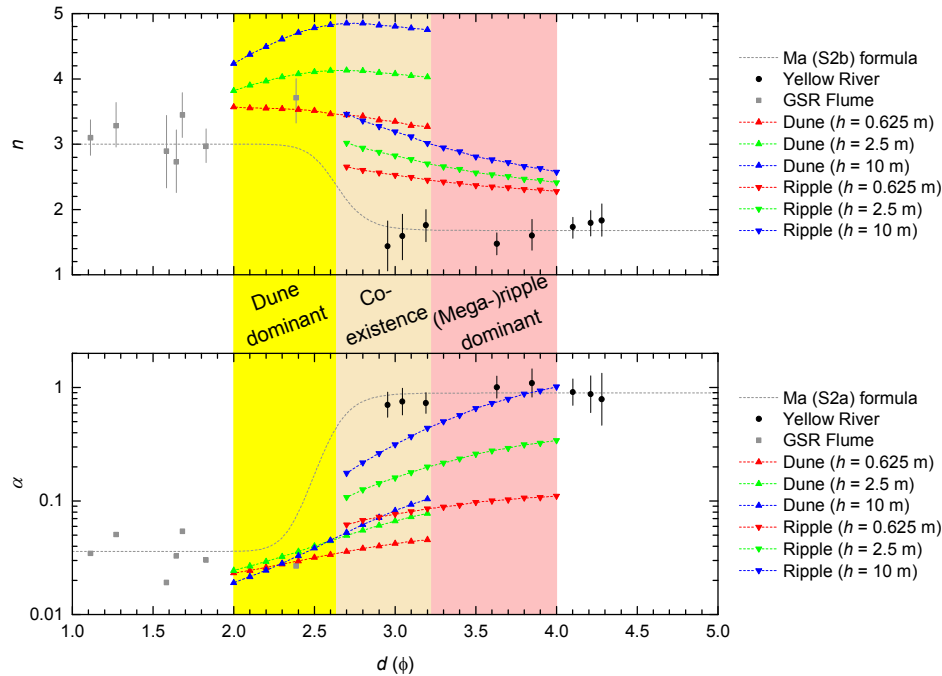
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341 **Figure 3:** Changes in the weight ( $k_{s,d}/k_s$ ) of dune component ( $k_{s,d}$ ) in total bed roughness height ( $k_s$ ), as a function  
 342 of flow mobility parameter ( $\Psi = \frac{u^2}{(s-1)gd}$ ). Bedform categories are marked as they are in Figure 2. Under a  
 343 specific water depth, the ratio  $k_{s,d}/k_s$  experiences a sharp increase to reach a high stage in the dune region, then  
 344 it declines hugely to 0 in the narrow transition zone, witnessing a bedform shift. As determined by the van Rijn  
 345 (2007) method, this ratio remains zero in the (mega-)ripple region, indicating no dune formation above the bed.  
 346 Aside from its variation with  $\Psi$ , the upper limit of this ratio increases rapidly as water depth goes up, exceeding  
 347 0.95 once the water depth is greater than 2.5 m.

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351 **Figure 4:** Changes of y-axes: exponent ( $n$ ) and coefficient ( $\alpha$ ) of dimensionless bed shear stress ( $\theta_b = \frac{\rho C_D u^2}{(s-1)\rho g d}$ ,  
 352 i.e. Shields number) in the Generalized Engelund-Hansen (GEH) formula ( $C_D q_s^* = \alpha \theta_b^n$ ), with respect to x-axis:  
 353 bed sediment grain size ( $d$ ). Bed regimes with respect to bed sediment grain size are marked as what they are  
 354 in Figure 2. As water depth ( $h$ ) increases, data plots see increases in average  $n$  (dune - 3.5 ~ 4.6, (mega-)ripple  
 355 - 2.3 ~ 2.8) and (mega-)ripple  $\alpha$  (0.10 ~ 0.76), while average dune  $\alpha$  (0.028 ~ 0.033) varies little. If relating dune  
 356 and (mega-)ripple points of a specific water depth, the joint curves ( $n-d$  and  $\alpha-d$ ) (1) show similar trends (almost  
 357 Logistic, and the regime shift/transition in the coexistence zone), as shown in Ma et al. (2017) where Logistic  
 358 functions are derived out of Yellow River and Guy-Simons-Richardson (1966) flume data; (2) travel upwards  
 359 and diverge as the water depth increases, representing a more crucial role that fluid flow ( $\theta_b$ ) plays in shaping  
 360 the sediment transport behavior ( $C_D q_s^*$ ).