# Response to reviewers on "How does the downstream boundary affect avulsion dynamics in a laboratory bifurcation?"

Gerard Salter, Vaughan R. Voller, Chris Paola

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We thank both anonymous reviewers for their helpful comments, which greatly improve the manuscript. In this document, we list the reviewers' comments in black, and our response in blue. Line numbers correspond to lines in the manuscript with highlighted changes, where P#L# denotes the page and line numbers.

### Response to Reviewer #1

General comments: Salter et al., present results from experiments that build on their previous numerical modeling work to examine discharge partitioning through a single bifurcation. Unlike previous models by other researchers, the authors allow net deposition in the system. In the experiments, the authors observe frequent switching of water and sediment discharge between the two branches, with asymmetry increasing for increasing width-to-depth ratios and decreasing dimensionless sediment fluxes. The authors argue that discharge partitioning is strongly affected by progradation vs. bypass, as well as by bar dynamics that generate high frequency oscillations in discharge partitioning. Asymmetry is higher during bypass, as progradation is hypothesized to autocorrect strong asymmetry. In the absence of bars (sand pile experiments), the authors find increased asymmetry and a 'frozen' stable asymmetry during bypass, as bars are not present to reroute sediment and reactivate an abandoned channel.

Overall, I find the paper very interesting and of great importance to the scientific community. The authors present a thorough explanation of their experimental methods and analysis of their results. I also find their explanations of avulsion and bar-induced switching compelling, and I appreciate their discussion of the applicability of their experiments. Below I highlight several concerns largely

around the presentation of figures, results, and discussion that will strengthen the paper and clarify several key points.

Specific major comments: Due to a general shortage of referencing, it is often difficult to tell which statements are the authors' own opinions and which are based on previous research/literature. For example, Page 1, Lines 23-24: Which studies? List some examples. Page 2, Lines 8-10: This is clearly based on other studies. Which ones? Include references here. The authors should also more directly relate their results to those of Bertoldi and Tubino (2007) and Bertoldi et al. (2009) (and/or others) throughout the results and discussion. This will put their results better into the broader context.

We intended for the references on pg 2 L4-5 of the original manuscript to apply to the entire paragraph; we have now moved the references to the first sentence of the paragraph to make this more clear (P1L23). Additionally, as also requested by the second reviewer, we added an additional paragraph in the discussion section on the role of bars in our experiments. In this paragraph, we relate our results more directly to Bertoldi et al. 2007/2009 (P19L26).

I find the language regarding the effects of 'deposition' and the 'downstream boundary' on avulsion dynamics confusing. The authors are examining how the partitioning of water and sediment down two branches of a bifurcation is affected by progradation vs. bypass. Yes, of course progradation is deposition, but 'progradation' is also more specific and informative to the reader. It also then makes it clear that the authors are not changing anything about the downstream boundary, but instead the boundary condition is changing as the system progrades. I suggest changing 'deposition' to 'progradation.' This is especially important in cases like Page 3 Line 28: 'The purpose of our experiments was to test the effect of deposition on bifurcation dynamics.' This is misleading on several fronts. First, deposition is a part of bifurcation dynamics, so it is hard to understand how you test the effect of it. Second, it sounds like you are examining bifurcation development and evolution, when in fact you are examining discharge partitioning in a bifurcation. This needs to be explicitly stated and clarified. Finally, this distinction will really help in your discussion (e.g., Page 19, lines 17-19). You state that deposition is not necessary for avulsion, as bar migration also allows for channel reactivation. But bar migration necessarily involves 'deposition,' so this statement is not as impactful as it could be. Progradation is not necessary for avulsion, as bar migration can also induce oscillations and channel reactivation.

We thank the first reviewer for pointing out an area of ambiguity in our terminology. We found several instances where we used "deposition" to refer to the first phase of the experiment, which we should have called "progradation" for the sake of consistency and clarity. However, we do find it useful to retain the use of the word "deposition" to refer to the condition that the sediment supplied at the upstream boundary exceeds the sediment exiting the downstream boundary. In other words, we use "deposition" as a descriptor of the systemwide mass balance, which we contrast with "bypass", where on average the input

and output sediment fluxes are in balance (albeit with statistical fluctuations due to autogenic dynamics, e.g. bar migration). A first reason is that it is useful to distinguish the first two net depositional phases of the experiment from the bypass phase, but the word "progradation" applies only to the first phase. Secondly, our hypothesis based on the SPV numerical model is that deposition vs. bypass is the critical control, not necessarily progradation. We showed in that paper that deposition even without progradation yields ongoing avulsion dynamics. Furthermore, using the SPV model, it is possible to design a scenario where relative sea level fall allows progradation to occur without deposition upstream at the bifurcation, and under this scenario the bifurcation dynamics are frozen. Therefore, the important role of progradation in our experiments is that it results in net deposition, producing the two-way feedback between sediment flux partitioning and the downstream bed slopes. We added a sentence (P2L26) to explain that net deposition is the key control. We also modified Figure 3 by choosing a more representative simulation which illustrates that switching can continue into the transitional period (which we note is what we observed in both of the model runs used later in the paper). The reviewer rightly points out that bar migration involves deposition. However, this deposition occurs locally at the bar-scale, whereas we are referring to deposition at the system-wide scale. In order to remove this ambiguity, we have replaced "deposition" with "net deposition" or "system-wide deposition" anywhere in the text where the two meanings could potentially be confused. Additionally, we added the following text in the introduction to clarify our usage of the term, as well as clarify the importance of the downstream boundary (P4L1):

Our usage of the term "deposition" here refers to the system-wide mass balance condition that the sediment flux input exceeds the sediment flux exiting the downstream boundary. In contrast, we define "bypass" as the condition that the sediment flux input and output are in balance on average. Because the sediment flux input from upstream is fixed, the downstream boundary controls whether the system is net-depositional or in bypass. We note that local deposition (e.g. due to bar migration) can occur even when the system is in a bypass state.

There is a lot of useful information in the supplemental material, but there is not one reference to it in the manuscript. The authors should reference the supplemental material where appropriate to guide readers to additional data and figures. This is especially helpful for the argument regarding estimations of Shields stresses. I understand that the experimental movies are available through the NCED data repository, but it would also be helpful to have them as supplemental information with the manuscript to make them easier to access.

We have added references to the supplemental info where relevant in the manuscript. We also uploaded the videos to the TIB AV-Portal, which is how ESURF handles video supplements.

Figures 4 and 5: I suggest adding some more labeling to these figures to make it easier on the reader. Authors should add text above each plot stating the channel aspect ratio and dimensionless sediment flux. I also strongly recommend calculating and plotting the mean asymmetry for each period (i.e., progradation, transition, bypass) for each experiment and adding that text to the plot. The authors describe differences in asymmetry in each period and between experiments, but quantifying it here would really drive that point home and make interpretation much easier.

### Thank you for the suggestions, done.

Page 8, Line 16: What is the justification for saying exp 2 bypass portion does not have periods of higher asymmetry? From Fig 5, it looks like exp 1 bypass has periods of 0.55 in RL vs. 0.45 in RR. There are comparable numbers in exp 2 bypass, and occasionally an even stronger asymmetry. This needs to be clarified. Quantifying it on the plot will also make this easier.

We meant relative to the degree of asymmetry earlier in the same experiment. In order to clarify, we added the word "relatively" to the sentence in question (P11L17).

Page 12 first paragraph: Call readers attention to the relevant parts of Figure 6. It is hard to follow without knowing which image to look at when. Looking at 6a, it appears the deepened branch is the right one, but the authors refer to a deepening on the river left. So is the left deepening in b? This needs to be clarified.

We added references to the specific relevant subfigures througout the paragraph, which should make the explanation easier to follow. And yes, between subfigures (a) and (b) the depth of the RL branch increases.

Figure 8: Also needs labeling. Add estimated timescales from your analysis as vertical lines or asterisks or some symbol. Otherwise the reader has to find your numbers in the text and then go back to the plot and figure out where those go. Your statements regarding controls on avulsion timescales will be easier to digest if the figure is clear.

We have implemented the suggestion and agree that it greatly improves the quality of the figure.

Page 15, Lines 30-33: Where do alpha and r come from? What are they? Why are they important? You introduce variables that are not defined, are not in an equation in the paper, and appear to never be used again. If this is central to your argument, then you need to elaborate. Since the timescale is not sensitive to them, why are they here? I recommend removing this and, if necessary, adding a supplemental section that elaborates on the model and any relevant sensitivity analysis.

We added an explanation for these parameters earlier in the paper when describing the model (P7L5). Because BRT-based bifurcation models tend to be

highly sensitive to these parameters, we think it is worth mentioning briefly that we tested their effect.

What are the previously unrecognized long-timescale bar dynamics mentioned in the abstract? Your bar timescales described in the paper are all very short. You restate something similar on Page 18, Lines 12-14: Are you arguing bars induced the longer-period switching during bypass? Where is the explanation of this in the data? Your bar-related switching timescales were all < 3 minutes. If you are not arguing this, then you need to reword.

We reworded to emphasize that the long-period dynamics are associated with a steady bar; we do not attribute the long-period dynamics to the action of migrating bars (P1L12, P19L14).

Specific minor comments: Page 5 Lines 6-8: I don't follow this explanation of your image processing. Why were you only looking in the 0.2-0.3 m range downstream? Are you averaging the cross-stream direction within each branch? So should this be 0.02 - 0.03? This needs to be clarified in the text.

This was a typo, we meant 2-3 cm. We have added slightly more detail to explain this step (P5L15).

Figure 6: Also recommend labeling. Flow direction, location of bar/scour, quantified asymmetry value.

Done, and we added the quantified asymmetry values to the figure caption.

Page 16, Line 13: Why 3W? Include a reference to justify this choice. Why is this timescale so different from linear bar theory?

Reference added. The important thing is not whether it should be 3W or 5W, but rather to get a rough estimate. The simple calculation is useful because the linear bar theory calculations are much more involved. However, we found an error in the simple calculations: the corrected values for the simple bar timescale are half of the erroneous ones. We also found an unrelated error in the linear bar theory calculations. With the help of Dr. Marco Redolfi, who is an expert on linear bar theory, we revised those calculations and find that our new numbers are much more physically realistic than before. With the corrected numbers, we find that the simple bar theory timescales are short relative to the linear bar theory timescales. We therefore note (P17L12) that the assumption of no sediment bypassing the bar might explain why the simple bar calculations yield a relatively short timescale.

Page 18, Lines 3-4: So did you test all of these? More information on these experiments is necessary.

Yes. We provide some additional detail for exactly what we tested (P19L1).

Why was the angle of 16 degrees chosen if the authors acknowledge that this is very low compared to nature?

We added the following text as explanation (P3L27):

We selected a narrow angle due to space constraints and to reduce shadows in the topographic scans. We note that angle does not play a role in the quasi-1D model of Bolla Pittaluga et al. (2003), and Thomas et al. (2011) found that angle has little effect on discharge partitioning in fixed-bed experiments.

### Technical corrections:

Page 2 last paragraph: 'channel aspect ratio' presumably is width:depth, but please specify for the reader. This can be easily fixed by adding '(i.e., aspect ratio)' after 'width-to-depth ratio' earlier on this page. Done.

Page 3, Line 26: Change 'We did our best to level' to 'We leveled' Done.

Page 5, Line 16: delete comma after 'overhead images' Done.

Page 7, Line 11: replace 'that paper' with actual reference (Salter et al., 2018) Done.

Page 8, Line 8: 'water discharge increases (i.e., W/h decreases), asymmetry decreases.' Done.

Page 8, Line 15: Recommend adding 'where the river left branch is favored, but the asymmetry is still small (X).' Done.

Figure 3: It needs to be clarified if this is water or sediment discharge. Done.

Page 11, Line 1-2: Does this matter? Recommend deleting.

We included it because there is discussion in other parts of the paper about how slight imperfections in the setup tended to result in RL being favored. Experiment 2 is therefore an important exception, and highlights how subtle the bifurcation sensitivity to imperfections appears to be.

Page 11, Lines 11-12: 'The asymmetry magnitude during these periods. . .' Which periods? There is a 'these periods' phrase also in the preceding sentence. Please clarify.

We added specific time intervals in the preceding sentence, and added clarification in the sentence in question (P11L27).

Page 11, Line 24: Fix parentheses 'experiments of Bertoldi et al., (2009).' This error also occurs elsewhere in the paper. Fixed.

Figure 7: 'Histograms of the water discharge asymmetry' Also the asymmetry needs to be defined. It is on the horizontal axis but is never defined in the paper. RL and RR I assume are river left and river right, but this is similarly never defined anywhere. We fix both issues at P11L4.

Page 14, Line 4: This is confusing. Please reword. I assume this is meant to say that right branch-focused strong asymmetry is diminished under bypass relative to depositional phase. Your reading of the sentence is indeed what we intended, but we improved the wording (P13L25).

Page 15, Line 25: Which model? SVP 18? Specify. Fixed.

Page 16, Line 21-22: Reference needed. Fixed.

Page 18, Line 10: 'deposition acts as a stopgap:' Fixed.

Page 20, Line 15: Add Salter et al., 2018 reference for 'most relevant existing model.' Fixed.

### Response to Reviewer # 2

The paper by Salter et al. reports on two sets of experiments designed to investigate bifurcation dynamics. The first set reproduces depositional and equilibrium sediment configurations, whereas the third one involves only sand (and no water) to assess the role of downstream conditions, without the upstream effect of bar migration. The experiments are well designed and monitored, the results are relevant and well explained, and the paper is written clearly with informative figures. Overall, I think that the paper is very good and I have only a few minor comments. I really like figure 7, which to my knowledge is an innovative way to present the dynamics of fluvial bifurcations and figure 8, which reports on one of the few quantifications of bifurcation timescale.

My main comment is about the length of the upstream channel and the formation of bars (Page 3, line 21-23). The length of the upstream channel is 9 times its width. This means it is probably too short to observe free alternate bars formation and migration. There is probably space only for maximum one full wavelength. Could this have an impact on the bifurcation dynamics you observe? Did you observe migration of free alternate bars?

Yes, we observed free bar migration. We added an example of overhead images showing bar migration on timescales on the order of minutes to the supplemental info. Most likely these bars are not fully developed, but they appear to influence the flow partitioning nevertheless. During other parts of the experiment (such as the majority of the bypass portion of experiment 4), the presence of migrating bars is not as obvious, but nevertheless downstream-migrating features can be observed from the overhead videos. Even if it is wrong to consider these features as related to migrating bars, linear bar theory may provide a useful reference timescale. After revising our calculations based on linear bar theory, we find that the predicted time scales line up well with the short time scale peaks in our histograms. If the upstream branch were longer, we might expect the migrating bars to develop more fully. Fully developed bars migrate more slowly, so the timescale would increase. Additionally, an increase in bar height could enhance the influence of bars.

The large bar closing one of the bifurcates is a steady bar forced by the bifurcation and I imagine it does not migrate, right? This steady bar formed also

in the experiments reported in Bertoldi and Tubino, 2007. I think this issue should be discussed with more detail in the paper.

Yes, this is a steady bar, and it was always located upstream of the river right branch. It did not migrate except to the extent that the boundaries of the bar tend to fluctuate. We added a paragraph to the discussion section on the dynamics we observed associated with the steady bar and migrating bars, in the context of the previous work by Bertoldi et al. (2007/2009) (P19L26).

Other minor comments and suggestions: Page 3, line 24. 16 degrees is a low value for the angle between the two branches. This value was probably forced by space constrains, that are often impossible to overcome. Do you have any idea whether (and how) this could impact the observed dynamics?

The first reviewer makes the same point, which we now address. We cite Thomas et al. (2011), who found that angle did not significantly affect flow partioning. In our view, the effect of angle is most likely second order; the dynamics will most likely remain qualitatively similar regardless of angle. We added a sentence of explanation (P3L27).

Page 5, line 6-8. I do not understand this sentence and procedure. What is the center 0.2-0.3 m o of each branch?

This was a typo, we meant 2-3 cm. We have added slightly more detail to explain this step (P5L15).

Page 7, line 12. The length of these cells is a crucial parameter in the model. Maybe it is worth introducing it here? Now you only find them at page 15, line 30-31, but their meaning is probably a mystery for anyone not knowing the model.

We added a sentence in the model explanation on the role of  $\alpha$  and r in the model, which addresses this point as well as the point made by the first reviewer (P7L5).

Page 7, chapter 3. I miss a detail form the model. During the depositional and transitional phases, the longitudinal slope in the upstream branch is increasing. As a result the width to depth decreases and the shear stress increases, meaning that the bifurcation should increase its asymmetry (as predicted by BRT model). Does the SVP model take these changes into account? Or did you consider only the final value of the slope? Moreover, could this effect explain (at least partly) the observed differences between the transitional and the by-pass phases and the shift towards more asymmetrical configurations?

Yes, the change in the upstream slope is captured automatically in the model. We find that the slope typically increases by a little over 10% between the start of the progradation phase and the bypass phase. As the reviewer points out, this means the aspect ratio increases, which tends to increase the asymmetry. Because depth is inversely proportional to slope to the 1/3 power, the change in depth is less than 5%. The Shields stress is proportional to the slope to the

2/3 power. An increase in the Shields stress tends to decrease the asymmetry, meaning that changing the slope introduces two partially offsetting effects on the asymmetry. We used the BRT model (i.e. not including deposition) to check how much the change in the upstream parameters due to the slope change affects the asymmetry, independent of deposition. Whether the aspect ratio or Shields stress wins depends on the value of  $\alpha$ , which makes sense when considering the neutral stability curve reported by Bolla Pittaluga et al. (2015). In general, we find that the effect on the asymmetry is small. In our model runs, the change in asymmetry is therefore dominated by the strength of the downstream deposition feedback. We added clarification that the upstream branch is considered explicitly as part of the model runs (P7L9).

As to whether this affected our experiments, we find an 11% slope increase in experiment 2, and no appreciable changes in the usptream slope in any of the other experiments. In all our experiments, we do not detect a change in the upstream channel depth. Therefore, we rule out changes in the upstream slope as the source of the asymmetry changes we observe, and conclude that the downstream control is the best explanation.

Page 12, line1-13. This is an interesting observation. I wonder whether you can provide an estimate of this longer timescale. Probably it was not easy to observe many cycles, but still, it would be ggod. Are these longer cycles visible in figure 8? Is the small peak at  $2^8$  minutes for exp. 4 - bypass related to this process? Page 15, line 22. There is no indication on how many switches you observed.

We observe around 2.5 cycles in experiment 4. In Figure 5, the first cycle starts around minute 1000, the second cycle starts around minute 1600, and the start of the third cycle is around minute 2200. The small peak in figure 8 at 2<sup>8</sup> minutes is only 3 switches, but yes, they are associated with the cycles (although they don't take up the full duration of a cycle). P13L14 we add a sentence stating how many cycles we observed.

Page 15, line 22 and following paragraphs on time scale estimation. I have two observations about this. First: from your estimations it looks like roughly the time scale for exp. 5 (both considering bars and downstream control) is 2-4 time that of exp. 4, mainly due to the lower sediment flux. It means 1-2 steps on your log scale in figure 8. It is difficult to tell (and the statistical test you performed do not allow for a quantitative assessment), but it looks reasonable, looking at the plots. Maybe you could add a comment about that.

Thank you for the interesting observation; we added a comment on this (P17L16).

Also, would that mean that the long switching scale for exp. 5 could be  $2^9 - 2^{10}$  (and therefore that the experiments were not long enough?)

We presented an argument in the paper/supplemental info for why we believe the complete avulsion was most likely permanent (the scour-widening mechanism that reopened branch RR during experiment 4 occured but did not result in a

reopening of branch RR, because the bed level in RR was significantly higher than the water level), but the reviewer is correct that running the experiment longer would make this point more convincing. We note that if a switch were to occur at the end of the experiment 5 run time, this would yield a switching time of  $2^9$  minutes.

The second point is about the timescale related to alternate bar migration. Did you really observed bar migration on the order of (a few) minutes during the experiments? As for the main comment above, with a relatively short upstream channel I do not expect formation (and migration) of free alternate bars.

Yes, as mentioned above, we observed bar migration on the timescale of minutes. We agree that it is surprising given the short length of the upstream branch; in fact we originally chose the upstream branch length to be long enough to accommodate reasonable values of  $\alpha$  but short enough to avoid the formation of bars. However, we found that it is impossible to understand the dynamics we observed without accounting for the influence of bars (or at least protobars).

## How does the downstream boundary affect avulsion dynamics in a laboratory bifurcation?

Gerard Salter <sup>1</sup>, Vaughan R. Voller <sup>2</sup>, and Chris Paola <sup>1</sup>

**Correspondence:** Gerard Salter (salte040@umn.edu)

**Abstract.** Bifurcations play a major role in the evolution of landscapes by controlling how fluxes such as water and sediment are partitioned in distributary and multi-thread channel networks. In this paper, we present the first experimental investigation on the effect of the downstream boundary on bifurcations. Our experiments in a fixed-wall Y-shaped flume consist of three phases: progradation, transitional, and bypass; the first two phases are net depositional, whereas during the third, the sediment flux exiting the downstream boundary matches the input on average. We find that deposition qualitatively changes bifurcation dynamics; we observe frequent switching in the discharge partitioning under net depositional conditions, whereas bypass results in long periods of time where one branch captures most of the flow. We compare our results with a previously developed model for the effect of deposition on bifurcation dynamics. The switching dynamics we observe are more irregular and complex than those predicted by the model. Furthermore, while we observe long periods of time where one branch dominates under bypass conditions, these are not permanent, unlike in the model. We propose that the range of switching timescales we observe arises from a complex interplay of downstream-controlled avulsion, and the effect of bars in the upstream-channel, including previously unrecognized long-timescale bar dynamics associated with a steady bar. Finally, we describe bifurcation experiments conducted with sand but no water. These experiments share the essential feedbacks of our fluvial bifurcation experiments, but do not include bars. In these experiments, we find that the sandpile grows symmetrically while it progrades, but bypass leads to one branch permanently capturing all avalanches. We conclude that the downstream control of deposition vs. bypass is likely a major influence on bifurcation dynamics across a range of physical systems, from river deltas to talus slopes.

### 1 Introduction

Fluvial bifurcations are common in depositional systems such as deltas and alluvial fans, as well as braided and anastamosing rivers (Kleinhans et al., 2013). Non-fluvial bifurcations are also observed on debris flow fans (De Haas et al., 2018), submarine channels (Limaye et al., 2018), and lava flow networks (Dietterich and Cashman, 2014). Bifurcations are the 'switches' that steer fluxes such as water and sediment through distributary and multi-thread channel networks, controlling the evolution and form of the resulting landscape — for instance, controlling where land is built and/or maintained in river deltas.

Although bifurcations are common in depositional systems, most previous studies on bifurcation flow partitioning (Bolla Pittaluga et al., 2003; Edmonds and Slingerland, 2008; Bolla Pittaluga et al., 2015; Redolfi et al., 2016) have assumed no net

<sup>&</sup>lt;sup>1</sup>Department of Earth Sciences, University of Minnesota

<sup>&</sup>lt;sup>2</sup>Department of Civil, Enviornmental, and Geo-Engineering, University of Minnesota

deposition (i.e. sediment bypass). This work has shown that bifurcations are susceptible to internal instability, where given a small initial perturbation, the bed morphology of the bifurcation evolves in such a way that an initially symmetric discharge partitioning becomes increasingly asymmetric. Depending on the interplay between a positive feedback favoring the deepening of one branch, and the negative feedback of cross-stream sediment transport, a symmetric bifurcation is either stable or unstable; in the latter case there may be a stable asymmetric configuration. Here, we use "stability" in the mathematical sense: an equilibrium is unstable if a small perturbation causes the system to diverge from that equilibrium (for example, a pencil balancing on its point is in unstable equilibrium), and stable if the system returns to its original state after a small perturbation (e.g., the pencil resting on its side). The stability is affected by multiple parameters, but arguably the most important is the width-to-depth ratio (i.e. aspect ratio). At low values of the width-to-depth ratio, symmetric bifurcations are stable; at high values, they become unstable.

While this aforementioned work assumes a symmetric bifurcation geometry and forcing, additional work has shown that asymmetry in boundary conditions produces a bias in the flux distribution. For example, Kleinhans et al. (2008) showed that an upstream meander steers flow in a bifurcation, and Bertoldi et al. (2009) studied the role of migrating bars in steering the flow. Imposing a difference in the downstream slopes also results in a bias (Bolla Pittaluga et al., 2003). Redolfi et al. (2019) synthesized the contribution of internal instability versus external forcing, showing that bifurcations without internal instability are completely controlled by the forcing, but when internal instability is present, for small forcings, bistability occurs, whereas for large forcing, only a single solution exists.

Edmonds et al. (2011) observed that deltas distribute sediment flux asymmetrically between their branches, which would be expected to lead to a highly asymmetric shoreline as branches receiving more sediment prograded faster. To prevent runaway asymmetry in the shoreline, they hypothesized that over time, a delta might redistribute its flux without creating or destroying any branches, a process they termed "soft avulsion."

To explore this effect, Salter et al. (2018) (hereafter SPV) added deposition to the theoretical model of Bolla Pittaluga et al. (2003). Bolla Pittaluga et al. (2003) showed that without net deposition, a bifurcation evolves towards a frozen state, either a stable symmetric state or a stable asymmetric state arising when the symmetric state becomes unstable. However, SPV showed that system-wide deposition produces ongoing avulsion dynamics, with behavior ranging from stable symmetry to soft avulsion up to full avulsion, depending on the parameters of the system. Deposition has a similar qualitative effect regardless of whether it occurs due to progradation or via purely vertical aggradation. Under symmetric forcing conditions, deposition prevents the occurrence of a steady asymmetric state.

Bertoldi and Tubino (2007) ran a set of bifurcation experiments in a Y-shaped fixed-wall flume with an erodible bed. They ran several experiments across a range of upstream channel aspect ratios and Shields stresses. They found that experiments with relatively high Shields stresses and/or low aspect ratios maintained a close to symmetric discharge partitioning. On the other hand, experiments with a larger aspect ratio and/or lower Shields stress became asymmetric. In some of these experiments, the bifurcation evolved towards a stable asymmetric state, where the discharge partitioning remained close to constant indefinitely. However, other experiments displayed large oscillations in the discharge partitioning associated with migrating bars. In these

experiments, the branch capturing the majority of the discharge switched back and forth during the course of an individual experiment, alternating between asymmetric states in which one branch was favored or the other.

Bertoldi et al. (2009) performed additional experiments and theoretical analysis to better understand the role of migrating bars in the dynamics of bifurcation flow partitioning. On the basis of their theory, and with strong agreement from their experiments, they classified bifurcations under the influence of migrating bars into four categories: "balanced," where the bifurcation remains close to symmetric and migrating bars induce only small oscillations in the discharge partitioning; "bar-perturbed," where bars induce small oscillations about an asymmetric state; "bar-dominated," where bars induce large oscillations in the flow partitioning, causing the asymmetry to switch back and forth from one branch to the other; and "one branch closed", where all of the discharge goes down a single branch. They found that the boundaries of these four phase regions were set primarily by the aspect ratio and Shields stress of the upstream branch.

In this paper, we investigate the role of the downstream boundary in controlling the dynamics in a set of laboratory fluvial bifurcation experiments, which for the first time include the effect of system-wide net deposition. Our experiments included both a net-depositional and bypass stages, allowing us to isolate the effect of deposition on the dynamics of the bifurcation, and thereby test the theory of SPV. Consistent with the theory, we find that deposition results in more frequent avulsions, whereas bypass leads to long periods of time where one branch captured the majority of the flow. However, unlike in the SPV theory, bypass does not stop avulsion entirely. We also find that the avulsion dynamics are significantly more complex than the simple oscillations predicted by theory. Additionally, to remove the effect of bars and extend our work to non-fluvial bifurcations, we ran an experiment with sand but no water, and found that avalanches occurred in both branches during progradation, but ultimately went down a single branch under bypass. Overall, our results indicate that deposition increases the frequency of bifurcation avulsion, but rich switching dynamics occur even without net deposition.

### 2 Fluvial Bifurcation Methods

### 2.1 Experiment Design

We performed a series of five experiments in a fixed-wall Y-shaped flume (Fig. 1). The upstream branch was 0.9 m long, and the two downstream branches were 2.1 m long measured along the outside wall. Roughly following hydraulic geometry scaling, the upstream branch was 0.1 m wide, and the two downstream branches were both 0.07 m wide. The angle between the two downstream branches was 16°, which is a relatively low angle compared to delta bifurcations in nature (Coffey and Shaw, 2017). We selected a narrow angle due to space constraints and to reduce shadows in the topographic scans. We note that angle does not play a role in the quasi-1D model of Bolla Pittaluga et al. (2003), and Thomas et al. (2011) found that angle has little effect on discharge partitioning in fixed-bed experiments. Water and sediment were introduced from upstream and fed directly into a rock crib, which diffused the flow. In each branch, a 30 mm high broad-crested weir acted as the downstream boundary condition. We did our best to level leveled the table supporting the flume such that when no sediment was fed, the water discharges in each branch were nearly equal.

# (a) side view (schematic) water sediment water level rock crib bed weir (b) overhead view water sediment 50 cm

**Figure 1.** a) Schematic side-view of an experiment. As water and sediment are fed from upstream, the delta deposit grows and progrades until it reaches the downstream weir. The downstream weir is also responsible for setting the base level. b) Overhead image from an experiment, showing the geometry of the Y-shaped bifurcation flume.

The purpose of our experiments was to test the effect of net deposition on bifurcation dynamics. Our usage of the term "deposition" here refers to the system-wide mass balance condition that the sediment flux input exceeds the sediment flux exiting the downstream boundary. In contrast, we define "bypass" as the condition that the sediment flux input and output are in balance on average. Because the sediment flux input from upstream is fixed, the downstream boundary controls whether the system is net-depositional or in bypass. We note that local deposition (e.g. due to bar migration) can occur even when the system is in a bypass state. Each experiment consisted of three phases. Starting from an empty flume with no initial slope, we fed water and sediment continuously from upstream. In all three experiment phases, water freely runs off over the downstream weirs. In the first phase of the experiment, progradation, all sediment is trapped within a growing delta that progrades down each branch, and therefore no sediment exits over the downstream weirs. In the second phase of the experiment, the transitional stage, the delta fronts reach the downstream weirs and some sediment begins to exit over the downstream weirs, but the sediment output is smaller than the sediment input, meaning that the system is still net-depositional. Finally, the last phase of the experiment is bypass, where on average all of the sediment fed from upstream exits downstream.

We used 0.3 mm quartz sand in all of our experiments. Table 1 shows the run parameters for each of the five experiments. The only variables we changed between experiments were the input water and sediment fluxes. The first four experiments have approximately the same sediment flux but different water discharges; the fifth has a lower sediment flux. We also include in Table 1 several measured dependent variables, which represent spatially and temporally averaged values over the upstream portion of the flume, measured once the system had reached bypass.

Experiment	$Q_w$ (mL/s)	$Q_s$ (mL/s)	h (mm)	S (-)	W/h (-)	$q_{s*}$ (-)
exp 1	182	0.61	4.7	0.027	21	0.29
exp 2	140	0.61	3.6	0.033	28	0.29
exp 3	103	0.60	2.3	0.054	44	0.29
exp 4	46	0.52	1.4	0.071	72	0.25
exp 5	125	0.29	2.9	0.042	35	0.14

**Table 1.** Parameter values for each run. The independent variables are water discharge  $Q_w$  and volumetric sediment flux  $Q_s$ . Dependent variables are depth h and slope S, measured over the upstream 20 cm of scans once the system reached bypass. Aspect ratio W/h and dimensionless sediment flux  $q_{s*}$  are also listed, where the dimensionless sediment flux is defined  $q_{s*} = \frac{Q_s}{W} \left( d_s^3 g \frac{\rho_s - \rho}{\rho} \right)^{-1/2}$ ,  $d_s$  is the grain size, q is gravitational acceleration,  $\rho_s$  is the sediment material density, and  $\rho$  is the density of water.

### 2.2 Data Acquisition

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We took time lapse images from overhead and orthorectified them using a grid of control points and Matlab's projective image transformation. We dyed the water blue so that the qualitative depth pattern was visible; in our images deeper areas are a deeper blue. To enhance the contrast between deep and shallow flow, we compute the color index C:

$$10 \quad C = \frac{B - R}{B + R} \tag{1}$$

where B and R are the intensities of the blue and red bands of the image, respectively. Examples of C obtained from overhead images are shown in Fig. 2.

Using the images, we obtained a time series of the sediment front position (Figure S1 of the supplemental info). This was done automatically by thresholding a differenced image between the current time and a reference time where no deposit was present, isolating pixels within the delta deposit. We then extracted the boundary of the binarized delta deposit, and identified the pixels corresponding to the sediment front. We averaged the positions of the sediment front pixels in the center 2-3 cm of each branch, and projected the position onto a line that was parallel to each branch, with the origin at the branch entrance. We defined the start of the progradation deposition phase as the time at which the sediment fronts reached the bifurcation point, and the start of the transitional phase as the time at which the first sediment front reached the downstream weir.

We used a laser sheet system to measure the topography of the experiment with 1 mm horizontal resolution and submillimeter vertical accuracy. We turned off the experiment periodically to measure the bed surface topography. Immediately before turning off the experiment, we also measured the water surface elevation. This was done by introducing a slurry of water and titanium dioxide from upstream, which turned the water opaque, allowing the scanner to measure the water surface. We obtained the depth by subtracting the bed scan from the water surface scan. Fig. 2 shows a comparison between the qualitative pattern obtained by computing C from overhead images and the quantitative measure of depth obtained from scans. The approximate time interval between scans was 2 hours, whereas the time interval between images is 30 seconds.

The sediment discharges at the downstream end of both branches were measured continuously. Below each overfall,  $\sim 19$  liter buckets received the water and sediment exiting the experiment. Each bucket was placed on a logging scale. Water was free to flow out over the top of the bucket, but the sediment settled out within the bucket. Because the density of the sediment  $\rho_s$  was 2.65 times the density of water  $\rho$ , and the total volume of water and sediment was roughly constant, we use the mass M on the scale to calculate the mass of sediment  $M_s$  as:

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$$M_s = \frac{\rho_s}{\rho_s - \rho} (M - M_0)$$
 (2)

where  $M_0$  is the mass if the entire volume on the scale were water. We applied a small correction to  $M_0$  to account for slight variation in water level as a function of discharge using the parts of our time series where the sediment flux was known to be zero. We smoothed the time series of sediment mass with a moving average filter, and took the time derivative to obtain the sediment flux.

We also measured water discharge continuously. In each branch, water exiting the sediment collection bucket entered a cylinder with a small horizontal hole near the bottom. An outer cylinder prevented splash, and the water was allowed to exit from the outer cylinder to the drain through a relatively large opening to prevent water from pooling in the outer cylinder. The entire assembly was mounted on a logging scale. The flow rate out of the hole in the inner cylinder is a function of the water level in the inner cylinder. Using a calibration curve, we computed water discharge using the mass on the scale.

Given that the incoming discharge was constant, one of the discharge measurement devices is redundant, as the discharges of the two branches should sum to a constant value. We observed some deviations from constancy, associated with error in the calibration curve, and with one of the measurement devices, which did not lock on perfectly to the scale causing it to shift slightly over time. However, these errors are small enough that they do not affect the interpretation of our results. Additionally, in one experiment the maximum measurable discharge was triggered at times, in which case we had to rely on the measurement from a single scale.

### 3 Prediction Based on Salter et al. (2018) Model

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The model of Bolla Pittaluga et al. (2003) (hereafter BRT), which assumes bypass conditions, predicts that a bifurcation will evolve towards an unchanging discharge partitioning. This partitioning could be either symmetric or asymmetric, with a tendency towards greater asymmetry under a higher upstream channel aspect ratio or lower Shields stress. SPV added the effect of deposition to the BRT model. This resulted in a range of dynamics, from stable symmetry to soft avulsion and full avulsion, depending on parameters of the system. A key prediction from the model is that depositional bifurcations undergo frequent switching, whereas bypass leads to an unchanging discharge partitioning. However, we note that SPV did not include

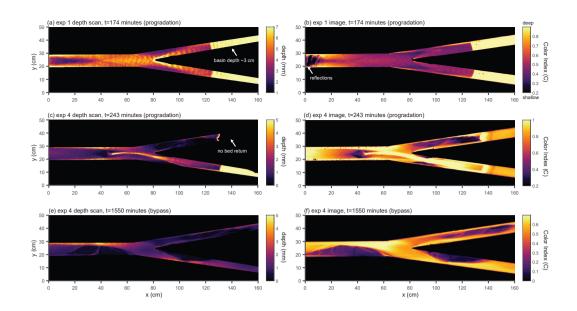


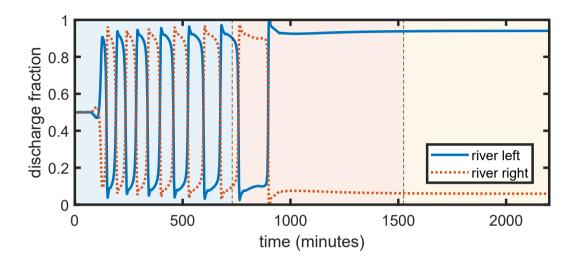
Figure 2. Comparison between water depth obtained from topographic scans (a, c, and e), and the Color Index C obtained from overhead images (b, d, f). Although the C does not map linearly to the water depth, it qualitatively reproduces the flow depth patterns. Examples are taken from the progradation phase of experiment 1 (a, b), progradation phase of experiment 4 (c, d), and bypass phase of experiment 4 (e, f).

the effect of migrating bars into the model. Bertoldi et al. (2009) coupled the effect of bar migration to the BRT model, and found that this can allow for oscillations under bypass conditions.

For reference, we run the SPV model using the same geometry and run parameters as our experiments. A full description of the model is found in Salter et al. (2018) that paper, but in short, we model the bifurcation branches in one dimension, and divide the reach immediately upstream of the bifurcation into two laterally interacting cells. The length in the longitudinal direction of these two cells is an important parameter of the model, and is given by  $\alpha W$ , where W is the upstream channel width, and  $\alpha$  is an order-one parameter. Transverse exchange of sediment between these two cells occurs as a result of cross-stream flow and the presence of a transverse bed slope; the strength of the latter control is specified through the parameter r. The whole system, including the two laterally interacting cells, upstream feeder channel, and two downstream upstream cells and the branches, evolves using sediment transport and mass conservation equations. Variation in the lateral bed slope upstream of the bifurcation and longitudinal bed slopes into the branches allows for discharge partitioning dynamics.

Like our experiments, our numerical runs consist of three phases: prograding, transitional, and bypass. We start from a symmetric initial condition with a small initial perturbation. During the first phase, once switching of the discharge partitioning starts, it occurs regularly, with a gradual increase in amplitude and period. Then, starting in the transitional period, the dynamics slow dramatically, and under bypass conditions dynamics stop entirely. The final configuration under bypass conditions is a frozen state, with a discharge asymmetry that depends primarily on the aspect ratio and Shields stress of the upstream channel. We note that in the model, once a sediment transport formula is chosen, choosing a value for the Shields stress is equivalent

to setting the dimensionless sediment flux. When comparing our the SPV model results with experiments, we prefer to use the dimensionless sediment flux instead of the Shields stress, because it is the independent variable, and our estimation of the Shields stress is complicated by non-uniformity in the upstream channel (see supplemental info). In the model, we observe greater asymmetry, all else equal, for larger aspect ratios and lower dimensionless sediment flux, and greater asymmetry with bypass compared to deposition. Figure 3 shows an example of a model run.

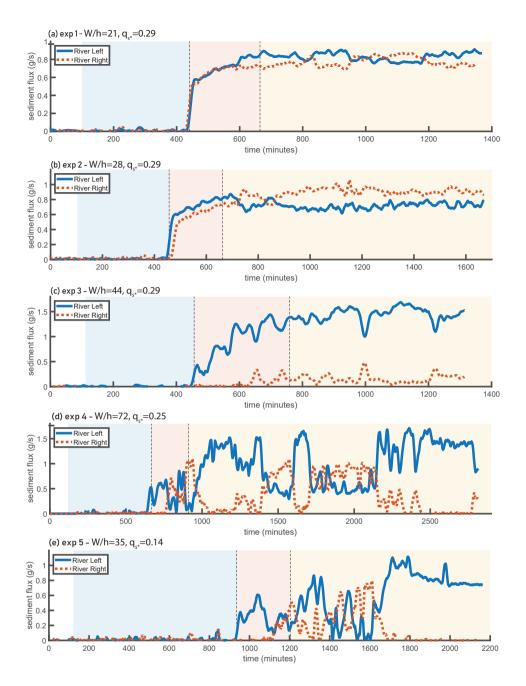


**Figure 3.** Typical water discharge partitioning time series obtained from the SPV model. Background colors represent the progradational depositional, transitional, and bypass portions of the experiment, respectively.

In the next section, we describe the results from our experiments, and compare the results to the predictions of our the SPV model.

### 4 Fluvial Bifurcation Experiments

As stated previously, each experiment consists of three phases: progradation, transition, and bypass. After an initial building period that is not relevant to our study, the start of the first phase occurs when the delta deposit first enters the 'Y' portion of the flume, as determined from overhead images. Once one of the two branches reaches the downstream weir, the next phase begins. The length of this transitional phase varies between experiments. Due to variability in the total output sediment flux, and the fact that the approach to bypass is gradual, determining the change from transitional to bypass phases is not obvious. We defined the start of the bypass stage as the point where the output sediment flux is within one standard deviation of the average sediment flux of the bypass stage. The sediment flux time series for each experiment are shown in Fig. 4, and the water discharge asymmetry time series are shown in Fig. 5.



**Figure 4.** Time series of sediment flux exiting each branch. The data have been smoothed using a double moving average with a window of 20 minutes. Background colors represent the progradational depositional, transitional, and bypass phases of each experiment. During the progradation depositional portion of the experiments, no sediment leaves the flume. The outgoing sediment flux gradually increases during the transitional phase, and reaches a statistical steady state during the bypass phase.

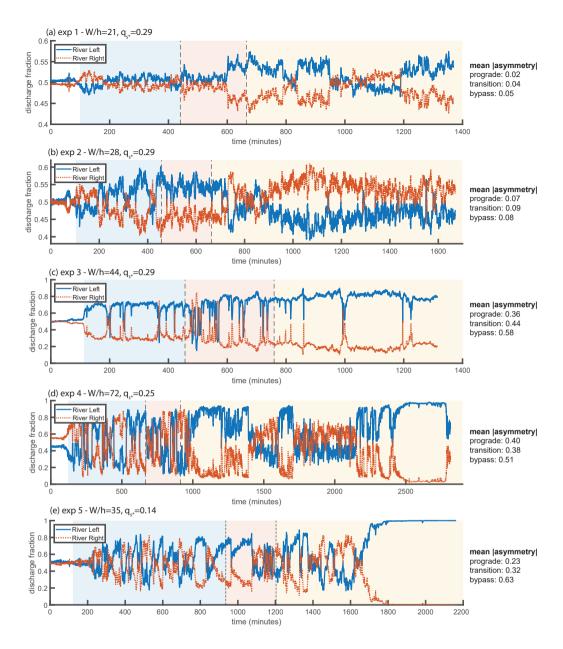


Figure 5. Time series of the water discharge fraction exiting each branch. Background colors represent the progradational depositional, transitional, and bypass phases of each experiment. Mean values of the absolute value of the asymmetry ( $|\Delta Q|$ ) of each phase are provided to the right of each time series. Note that  $|\Delta Q|$  is equivalent to the difference between the larger discharge fraction and smaller discharge fraction.

### 4.1 Mean Asymmetry

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Based on the original BRT model and our own model simulations, we predict that increasing the upstream width-to-depth ratio should increase the asymmetry of the experiment, and decreasing the dimensionless sediment flux also increases asymmetry. Following the definition from Bertoldi et al. (2009), we define the discharge asymmetry  $\Delta Q$  as  $\frac{Q_{RL}-Q_{RR}}{Q_{RL}+Q_{RR}}$ , where  $Q_{RL}$  and  $Q_{RR}$  are the water discharges through the river left and river right downstream branches, respectively. In our experiments, we control the width-to-depth ratio by changing the input water discharge. As can be seen in Fig. 5, comparing experiments 1 through 4, run with approximately the same sediment flux but differing water discharges, we find that as input water discharge increases (i.e. aspect ratio decreases), asymmetry decreases. This is consistent with the model prediction. Experiment 5 was run with a lower dimensionless sediment flux. This results in greater overall asymmetry (for the given aspect ratio), consistent with the model.

### 4.2 Qualitative Description of Experiments

Experiments 1 and 2 were the closest to symmetric of the experiments. As shown in Fig. 5, some switching in the water discharge asymmetry occurs during the progradational depositional and transitional portions of these runs, with a few switches in sign, and superimposed high frequency variability. In the bypass portion of experiment 1, there are times of measurably higher discharge asymmetry where the river left branch is favored, but the asymmetry is still small ( $\Delta Q \sim 0.1$ ). However, these periods are interspersed with periods of milder asymmetry. The bypass portion of experiment 2 does not have these periods of relatively high asymmetry, but does have a tendency to favor the right branch. Interestingly, this was the only experiment that favored the right branch; to the extent that other experiments favored a branch, it was always the left side.

Experiment 3 was unusual in that there was a clear bias towards favoring the river left side in not just the bypass stage but for the entire duration of the experiment. Despite this preference, we do observe a change in dynamics between the progradational and bypass portions of the experiment. The progradational and transitional portions of the experiment have occasional short-duration periods where the right branch becomes highly favored; these are almost entirely absent from the bypass portion of the experiment. We also observe that the maximum asymmetry during the bypass portion of the experiment is slightly larger than during the progradational depositional phase.

Experiment 4 had frequent high-magnitude switches during the progradational depositional and transitional phases of the experiment. In contrast, the bypass phase contains long periods of time where the left branch captures most of the discharge (i.e in Fig. 5 approximately minutes 1000 - 1400, 1600 - 1700, and 2200 onward). However, these periods are interspersed with times where the discharge asymmetry is milder. The asymmetry magnitude during these periods of milder asymmetry is actually lower than the asymmetry of the switches observed in the depositional portions phase of the experiment. We note that throughout the duration of the bypass portion of the experiment, there was a persistent steady bar immediately upstream of the river right branch. The dynamics we observe during the bypass portion of the experiment are associated with the partial erosion and re-formation of this bar, and are described in greater detail in the next section.

Experiment 5 was similar to experiment 4 during the progradational depositional and transitional portions of the experiment, displaying frequent switches. Towards the end of the progradational depositional phase and start of the transitional phase, there were a few relatively long duration switches favoring the left branch. The dynamics during the start of the bypass stage do not differ qualitatively from the preceding dynamics. However, starting around minute 1700, the left branch gains discharge, and eventually captures the entirety of the flow. There is no guarantee that a switch would not have occurred had we run the experiment longer. However, we believe that the complete avulsion was most likely permanent, due to the significant difference between the bed elevation of the right branch and the local water elevation (see supplemental figures S2 and S4). Even though we observed the growth of a region of scour in the upstream portion of the right branch, the downstream bed elevation was high enough to act as a barrier to avulsion. Permanent complete avulsions were also observed in some of the experiments of Bertoldi et al. (2009). While the frozen state we observed towards the end of the experiment is consistent with the prediction of our the SPV model, the switches that occurred during the first half of the bypass stage are not.

### 4.3 Bypass Dynamics

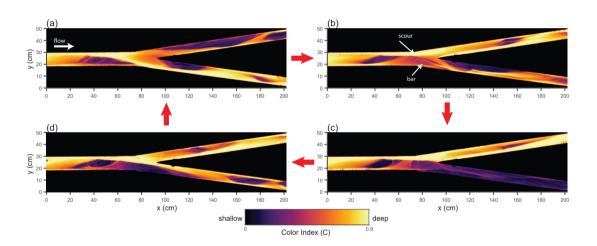


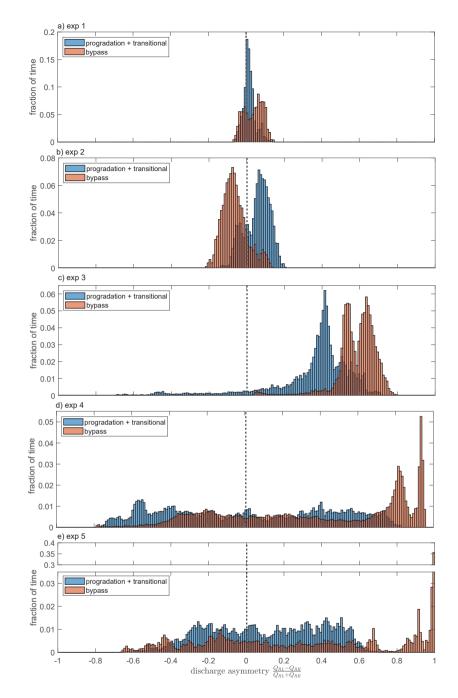
Figure 6. Color Index C obtained from overhead images, illustrating the bypass dynamics observed in experiment 4. Images are taken at time (a) 1595 minutes (b) 1602 minutes (c) 1698 minutes (d) 1707 minutes. Corresponding values of  $\Delta Q$  are: (a) -0.55 (b) 0.38 (c) 0.84 (d) 0.34.

Next, we describe in detail the dynamics of experiment 4, which displayed a dramatic change in dynamics between the net-depositional and bypass stages, as seen in Figure 5. In this experiment, frequent switching occurs during the progradational depositional and transitional stages of the experiment. On the other hand, during the bypass stage, the bifurcation favors the river left branch for long periods of time, appearing to become frozen. These periods coincide with the presence of a steady bar blocking the entrance to the right branch, and a region of scour at the entrance to the left branch. However, we find that the bifurcation occasionally unfreezes, and the right branch reopens and can remain open for an extended period.

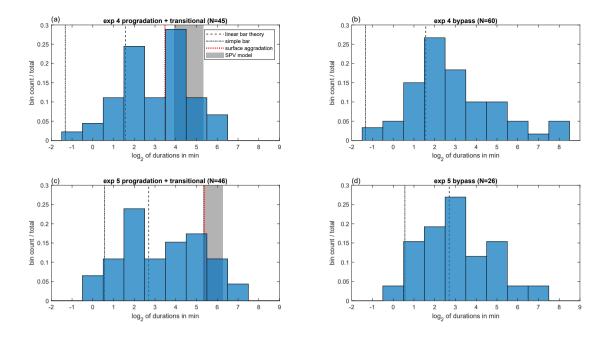
These dynamics of freezing and unfreezing appear to be a previously unrecognized type of autogenic cycle, as illustrated in Fig. 6. The cycle begins with the deepening of one branch due to a positive feedback (Subfigures (a) to (b) in Fig. 6), as described in the BRT theory. The fact that in our experiment this always coincides with the river left branch is probably due to small imperfections in the construction of the bifurcation geometry. At this stage in the cycle, immediately upstream of the bifurcation, cross-stream flow of water and sediment occurs from river right to left. Due to the nonlinearity of sediment transport, consolidation of the flow through a single branch enhances the downstream sediment flux, leading to erosion upstream of the bifurcation. This erosion causes the surface of the bar at the entrance to the right channel to become abandoned (Subfigure (c) in Fig. 6). However, cross-stream flow of sediment immediately upstream of the bifurcation appears to be important in stabilizing the scour region; as the bar surface is abandoned, the scour region widens until enough of the bar edge has been eroded that the right branch is reopened (Subfigure (d) in Fig. 6). However, with both branches open, less sediment flux is conveyed, forcing the system to aggrade (see bed profiles in supplemental Figure S2). This allows the flow to reoccupy any remnant portions of the bar upstream of the right branch, setting up the conditions for the cycle to begin again. This cycle is illustrated in Fig. 6. We observed similar dynamics associated with partial erosion and re-closure of the bar in experiments 3 and 5 as well, but the cycle was clearest in experiment 4. From Figure 5, we observe roughly 2.5 of these long cycles during the bypass portion of experiment 4 (notice long periods where the left branch dominates, followed by extended periods of reduced asymmetry), with higher frequency dynamics superimposed on the long cycles.

### 4.4 Distribution of Asymmetry Values

Figure 7 shows the distribution of the asymmetry in water discharge partitioning. For each experiment, the distributions of the two net-depositional phases are plotted separately from the distribution of the bypass phase. For all experiments except experiment 2, we find that the distributions shift towards greater values of asymmetry under bypass conditions, with a clear preference for the left branch over the right branch. Experiments 1 and 2 have the lowest overall degree of asymmetry, but nevertheless exhibit small shifts between the distributions of the depositional and bypass phases. The distribution for experiment 3 exhibits a persistent bias towards the left side. With bypass, this bias is even stronger. For depositional conditions, experiment 4 has a broad distribution of asymmetry values. In contrast, under bypass conditions, there is a relatively narrow double peak at very high asymmetry values favoring the left branch, and a very broad peak slightly favoring the right branch. with During the bypass phase, extreme negative asymmetry values (i.e. favoring the river right branch) have diminished frequency relative to the depositional phase. Like experiment 4, the histogram of experiment 5 exhibits a shift towards high asymmetry values favoring river left between the depositional and bypass phases, but also shows a slight increase in the frequency of highly negative asymmetry favoring river right, whereas this part of the distribution was suppressed in experiment 4. Experiment 5 exhibits a similar shift in the asymmetry distribution, except with a slight increase in the tail of the distribution favoring the right branch. The largest peak in the distribution coincides with the complete abandonment of the right branch.



**Figure 7.** Histograms of the water discharge asymmetry from each experiment. Blue shows the progradation and transitional phases, and orange is the bypass phase. Negative values of the discharge asymmetry indicate that the river right branch is capturing a greater proportion of the discharge, and vice versa for positive values. Note break in y-axis for subfigure (e).



**Figure 8.** Histograms of duration between switches for (a) experiment 4 progradation and transitional phases and (b) bypass phase, and (c) experiment 5 progradation and transitional phases and (d) bypass phase. Theoretical timescales are shown for comparison.

### 4.5 Avulsion Timescales

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Next, we seek to characterize the timescales of the switching behavior we observed in our experiments, and compare those timescales to those that would be predicted to arise from downstream-controlled avulsion and from migrating bar-induced switching.

We first used a Fast Fourier transform to look for characteristic frequencies. However, we found that there are no obvious peaks in the plot of power spectral density. The power is highest at low frequencies, and decays as approximately  $1/f^2$ . We also used wavelet analysis, following methods suggested by Torrence and Compo (1998), but similarly, we found that low frequencies dominated the Wavelet power spectrum, and that there were no persistent statistically significant peaks at higher frequencies.

Next, we looked at the statistics of switch duration. For each switch event, we start a timer when the discharge rises above an arbitrary threshold, here 55% of the total discharge, and keep the timer running until the discharge falls below 45% in that branch. We then record the duration, and start the timer for the next event. We repeat this procedure for the duration of our time series, obtaining a series of switch durations. While the precise distribution is sensitive to the choice of threshold, the results are qualitatively similar. We chose a threshold that is large enough that we could be confident that all switches we recorded are true switches, rather than arising from noise in our measurement. We note that durations are not recorded if we do not observe the end of the event. Both experiments 4 and 5 ended after favoring one side for a long period of time; these events are not

included in the duration histograms of Fig. 8, but they would represent an additional count on the long-duration tails of the histograms.

We focused our analysis on experiments 4 and 5, because these were the experiments with the most robust and high-magnitude switching. We generated separate histograms of the switch duration for each of these two experiments with deposition (progradation and transitional phases) and bypass. The small number of switches makes drawing a meaningful distinction between the histograms impossible; using a two-sample Kolmogorov-Smirnov test or a two-sample Anderson-Darling test, we are unable to rule out the possibility that all four histograms are random realizations of the same underlying distribution. We tested the possibility that switches occur randomly according to a Poisson point process. A Poisson point process yields an exponential distribution of switch durations. If we relax the assumption of randomness and allow for short-time inhibition, the resulting distribution is a gamma, of which the exponential distribution is a special case. Using either a one-sample Anderson-Darling test or Kolmogorov-Smirnov test, we can reject the null hypothesis with p < 0.05 that our experimental distributions are drawn from a gamma distribution, with p < 0.05 that our experimental distributions are estimating the parameters of the distribution from the distribution itself. On the other hand, we find that our distributions are consistent with a lognormal distribution.

With the caveat that our experiments generated a small sample size of switches, we can compare the observed switch durations with those expected from different physical mechanisms. Therefore, we seek to estimate the timescales that would be expected for downstream-controlled avulsion, and for migrating-bar induced switching.

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We begin by running the SPV our model to generate a prediction of the downstream-controlled avulsion timescale. We use the parameter values reported in Table 1, and the Wong and Parker (2006) correction to the Meyer-Peter and Müller (1948) sediment transport formula. We note that because the imposed dimensionless sediment flux sets the upstream Shields stress, we cannot set both the upstream depth and slope independently. We choose to match the slope rather than the depth, because the slope is a more important control on the avulsion timescale. Using the parameter values from experiment 4, we obtain a switching timescale that ranges from approximately 15 to 40 minutes as the branches lengthen. We note that our the SPV model depends on the free parameters  $\alpha$  and r, chosen as  $\alpha = 1$  and r = 0.5. We find that these parameters do not strongly affect the switching timescale, but they strongly affect the degree of asymmetry and the onset time of switching. For example, when  $\alpha$  is doubled, the onset of switching is delayed, but the approximate switching timescale at the end of the progradation phase is 34 minutes. Using parameter values from experiment 5, we obtain a switching timescale that ranges from approximately 40 to 78 minutes. An alternative estimate for the downstream-controlled switching timescale that does not rely on the use of a numerical model is the time T to fill the surface area A of the experimental domain to one channel depth h, i.e.  $T = \frac{Ah(1-\lambda)}{Q_s}$ , where the porosity  $\lambda$  is assumed to be 0.4, and the surface area A is roughly 0.42 m<sup>2</sup>. This estimate does not account for the volume of sediment deposited in the foreset of the prograding branches, or the change in topset area over time. Using this method, we obtain an estimated timescale of 11 minutes for experiment 4 and 41 minutes for experiment 5.

The second physical mechanism to assess is switching induced by downstream-migrating bars in the upstream channel, as proposed by Bertoldi et al. (2009). Our first estimate of the timescale is derived from the linear bar theory of Colombini et al. (1987). The relevant timescale is the time for the fastest-growing bar to migrate 1/2 of the bar wavelength (the 1/2 bar

wavelength is the distance from a bar to the next downstream bar on the opposite side of the channel). We obtain our estimate using linear bar theory code from Redolfi et al. (2019). the Tremto code (Adami et al., 2014) Using parameter values from experiment 4, the angular frequency of the fastest growing bar is 0.003; this translates to a switching timescale of 3.0 minutes. Using parameter values from experiment 5, we obtain a switching timescale of 6.5 minutes. Alternatively, a simpler way to estimate the switching timescale T, which again is the time required for a bar to translate 1/2 bar wavelength, is as follows: we assume a rectangular cross-section with a height equal to the channel depth h and width equal to 1/2 of the channel width W, a typical bar 1/2 wavelength of 3W (Adami et al., 2014), and that all of the volumetric sediment flux  $Q_s$  contributes to the bar (i.e. no sediment bypasses the bar). Based on these assumptions, we obtain  $T = \frac{1.5W^2h(1-\lambda)}{Q_s}$ . From this expression, for experiment 4, we obtain a timescale of 0.4 minutes, and for experiment 5, we obtain a timescale of 1.5 minutes.

We can compare these theoretical timescales with those obtained from our experiments, shown in Fig. 8. Our theoretical estimates for bar-migration timescales are on the order of minutes, a few minutes or less, generally falling within or slightly less than the shortest observed switching times in our distributions. The simple bar timescale estimates are short compared to those from linear bar theory, perhaps due to the assumption that no sediment bypasses the bar. Our estimates for the downstream-controlled avulsion timescale are in the tens of minutes, and generally fall within the longest switching times we observed. However, we note that long switch-times are observed even during the bypass portion of our experiments, where SPV theory predicts an infinite downstream-controlled avulsion timescale. The theoretical timescales for both bars and the downstream control are approximately 2-4 times higher for experiment 5 compared to experiment 4, owing primarily to the differences in sediment flux and channel depth. Although based on statistical tests we cannot preclude that the experiment 4 and experiment 5 histograms differ purely by chance, a doubling of the switch durations (i.e a shift to the right by one bin in Figure 8) is reasonably consistent with the observed distributions.

### 5 Sand Pile Experiments

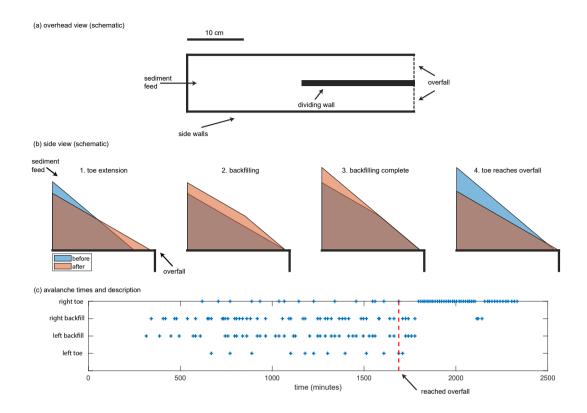
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Given the complexity we observe in the experiments described above, we decided to study a system stripped to the bare essentials: a positive feedback that causes a growth in asymmetry, and the presence or absence of progradation, which due to mass balance acts as a negative feedback via the slope. To accomplish this, we ran an additional set of experiments in which sand but no water is fed from upstream, producing a sand pile. These experiments were run on a table top with straight side walls roughly 40 cm in length and 10 cm apart, and a central dividing wall starting halfway downslope (Fig. 9a). Similar to the fluvial experiments, the downslope boundary condition was a free overfall. By running without water, these experiments are free of the complexity introduced by migrating bars while preserving the essential feedback described above.

In these experiments, we started with a flat, empty initial condition and then fed sediment continuously. A growing sand pile developed, which prograded through avalanching. We found that in the initial phase of the experiment where the sand pile toe had not reached the table edge, avalanches went down both sides of the bifurcation in roughly equal proportion, with neither branch advancing far ahead of the other. Many avalanches went down both branches simultaneously. Next, the sand pile toes reached the table edge and sand began to exit over the table edge. We found that eventually, once the pile reached the end of

the table, all of the avalanches went down a single side, and the other side was completely closed off indefinitely (Fig. 9c). We also observed that the avalanches became more regular in size and frequency.



**Figure 9.** (a) Schematic of the experimental setup for the sandpile bifurcation experiments. (b) Schematic side-view illustrating stages of sandpile growth. (c) Avalanche type and location vs. time. Red dotted line is when the sandpile toe first reached the overfall (table edge).

In addition, we observed that once the system reached its final state, the bed elevation was lower upstream of the entrance to the active branch than the closed branch. This lateral slope appeared to be responsible for steering the avalanches down a single side. We hypothesize that with progradation, the lateral slope is self-correcting. We observed that when prograding, the sand pile typically grows through large avalanches that erode the top of the pile and extend the toe of the pile. In response to the extension of the toe, smaller avalanches backfill from downstream to upstream. We hypothesize that large avalanches that create a lateral slope extend the sand pile toe further, allowing subsequent backfilling avalanches to erase the lateral slope (Fig. 9b). However, once the sand pile reaches the edge of the table, large avalanches are no longer free to extend the toe of the pile. This turns off the backfilling process. Without this self-correction, a positive feedback emerges where a slight lateral slope advantage produces larger avalanches which scour deeper, creating an even larger lateral slope until all avalanches are steered down a single side.

We found that this stark difference in dynamics was not sensitive to the details of how our experiments were conducted; we observed qualitatively similar behavior at both higher and lower sediment feed rates, with different sediment types (low-density walnut shell sediment or quartz sand), and different flume geometries (we tried both narrower and wider branches). the feed rate, grain size, sediment material density, or the precise geometry of the flume. We found that the choice of side once the pile reached the table edge was sensitive to the position of the sediment feeder. When the sediment feeder was slightly off center, the avalanches inevitably followed the branch closer to the feeder. However, we found that once a side had been chosen, shifting the feeder position closer to the opposite branch did not result in a switch, even when the feeder was moved past center. Only when the feeder was shifted far past center did the avalanches switch side. This indicates that while the choice of side is highly sensitive to any asymmetric imperfections, once a side is chosen it is stable to modest perturbations.

### 10 6 Discussion

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Our interpretation of the dynamics in our fluvial experiments is that they arise from a complex interplay between bar dynamics and the downstream control. As is clear from the bypass portion of our experiments, bars produce vigorous and complex dynamics by themselves. These include in the form of frequent oscillations induced by migrating bars, as proposed by Bertoldi et al. (2009), as well as the longer-period dynamics we describe in this paper associated with a steady bar. What then is the role played by net deposition? We propose that deposition acts as a stopgap: whenever bar dynamics alone are not sufficient to distribute sediment evenly between branches, deposition results in a self-correcting tendency via the difference in downstream slope between the two branches. In our experiments, we observed large asymmetries in the time-integrated sediment delivery to the two branches under bypass conditions. On the other hand, deposition prevents this asymmetry from growing without bound.

This view that the dynamics arise from the interplay of bars and the downstream control is supported by our sandpile experiments. In the sandpile, there was no source of internal variability to kick the system out of a frozen state once the system was in bypass. Again, deposition produced a self-correcting effect via the slope: if one branch grew a little faster than the other for any reason, the difference in downstream slopes allowed the opposite branch to catch up. Our sandpile experiments suggest that downstream-controlled avulsion is not limited to river deltas. We expect to find similar behavior in a range of physical systems, from debris flow fans to lava networks to talus slopes.

The rich bar-induced dynamics we observed during our experiments are surprising; given the relatively short length of the upstream channel ( $\sim 10W$ ), migrating bars, if they occur, are unlikely to be fully developed (Federici and Seminara, 2003; Fujita and Muramoto, 1985). Nevertheless, at times we observed free bar migration on the timescale of minutes in the downstream portions of the upstream channels (as an example, see Fig. S3 in supplemental info). Bar migration induced oscillations in the flow, consistent with previous work (Bertoldi and Tubino, 2007; Bertoldi et al., 2009). At other times, we observed the presence of a long steady bar, which in our experiments tended to block the river right downstream branch. Similarly, in several experiments, Bertoldi and Tubino (2007) observed a steady bar with a wavelength roughly twice that of migrating bars, and which they attributed to the downstream-to-upstream morphodynamic influence of the bifurcation. In

our experiments, the dynamics associated with the steady bar are far from steady. From overhead video of our experiments (see supplemental videos), we observe dynamics at timescales on the order of minutes: the boundaries of the steady bar and scour region on the opposite wall are constantly changing, and cross-stream channels on the bar surface are constantly shifting, sometimes in the downstream direction, and sometimes in the upstream direction. The possibility of both downstream and upstream-migrating features is consistent with existing morphodynamic theory (Zolezzi and Seminara, 2001). While these dynamics are clearly not as simple as alternate bar migration, the timescales predicted by bar theories may still provide a useful reference. Additionally, as previously described, we propose that a long-period cycle associated with the steady bar occurs in conjunction with these shorter-timescale dynamics.

We were unable to define a preferred switching frequency of our experiments using a Fourier transform or wavelet analysis. A possible explanation is that our experiments do not reflect a simple superposition of frequencies, but rather represent a concatenation of switches of variable duration. Instead, we quantified the frequency of our bifurcation experiments by compiling the intervals between threshold-crossings. A justification for this approach can be found in the asymmetry histograms of Fig. 7, showing that the bifurcation spends most of its time in an asymmetric state. This approach was inspired by work on the polarity intervals of the Earth's geomagnetic system. The standard view of polarity reversals is that they occur randomly (albeit with short-time inhibition), but that the underlying frequency of the reversal process changes through time (Merrill and McFadden, 1994). While a similar approach could be taken to modeling avulsion in our experiments, the small number of observations we have does not justify it (our data is fit by the simpler lognormal distribution). Theoretically, we do not expect downstream-controlled avulsion to be a completely random process. If the effect of the downstream-control is to create a tendency to correct asymmetries in the integrated sediment flux delivery, then the history of previous reversals should matter, even if our data set is not sufficient to define a preferred frequency.

The histograms for the net-depositional portions of experiments 4 and 5 show some indication of bimodality (Fig. 8), but as mentioned previously, due to the small total number of switches, we cannot rule out that these histograms are random realizations of an underlying lognormal distribution. In any case, we find that the range of switch durations we observe in our experiments spans the durations we would predict for migrating-bar-induced switching to downstream-controlled avulsion. Linear bar theory is known to over-predict the speed of fully-developed migrating bars (Adami et al., 2014). However, given the short length of our upstream branch, bars are unlikely to be fully developed; underdeveloped bars tend to migrate faster, and therefore more in line with linear theory (Federici and Seminara, 2003). and it is clear that our estimate for experiment 5 is unrealistically fast compared to our switch duration. Otherwise, Based on our estimates of bar migration timescales, bar migration could explain the short-duration switches we observed, but does not explain the entire distribution. Downstream-controlled avulsion could explain some of the longer-duration switches we observed. although our model seems to over-predict the duration for experiment 5. However, no existing theory explains the long-duration events we observed under bypass conditions; our theory predicts infinite duration, whereas ordinary bar migration would result in a much shorter timescale.

Previous work has tied interavulsion time to deposition rate normalized by the channel depth (Mohrig et al., 2000; Jerolmack, 2009). Consistent with this work, we find in our experiments that deposition reduces the maximum interavulsion time, whereas bypass leads to long periods of time without avulsion. However, our work also demonstrates that net deposition is

not strictly necessary for avulsion to occur. We find that upstream controls such as bar migration and lateral erosion allow for reactivation of the previously subordinate branch. Similar avulsion mechanisms have been observed in the field. Makaske et al. (2012) presents a case study of two avulsions on the Taquari megafan, Brazil. Although both avulsions are associated with channel-belt aggradation, the authors propose that lateral migration played an important role in the mid-fan avulsion, whereas downstream controls were more important in the lower-fan avulsion. Bertoldi (2012) presents an example of an upstream-dominated bifurcation in the Tagliamento River, Italy, and found that its evolution was dominated by bar migration from upstream. In our experiments, we observe a wide range in avulsion frequencies, which we propose arises from the interplay between upstream controls (e.g. bar migration, lateral erosion) and the downstream control (deposition vs. bypass). Previous work on the Rhine-Meuse Delta, The Netherlands, shows that interavulsion time and avulsion duration are highly variable (Stouthamer and Berendsen, 2001). While Stouthamer and Berendsen (2007) proposed using interavulsion time as a way to distinguish autogenic and allogenic causes for avulsion, our work demonstrates that autogenic dynamics alone are sufficient to produce high variability in interavulsion times.

Compared to bifurcations in nature, our experimental bifurcation has a reduced degree of freedom. In nature, channels can widen, and bifurcations can change their planform geometry. Our experiments are most directly analogous to bifurcations where the bed is free to evolve, but the banks are leveed and stabilized by engineering works. Despite the relatively simple design and geometry of our experiments, we observe highly complex switching dynamics. While a freely evolving planform geometry introduces additional degrees of freedom, we predict that the downstream control should influence the qualitative dynamics in a similar way. For example, on the broader scale of whole-delta response to downstream boundary conditions, the delta experiments of Kim et al. (2013) showed that progradation results in rapid lateral migration and avulsion, whereas bypass caused the delta to consolidate its flow into a single, static channel. Similarly, Carlson et al. (2018) showed that deeper basins increase autogenic timescales in delta experiments. Although we predict similar qualitative dynamics, bifurcations that are not laterally fixed will differ quantitatively relative to our fixed-geometry experiments. In particular, if each branch distributes sediment over a nourishment area rather than just the channel itself (Shaw et al., 2016), then the progradation mass balance will change, potentially increasing the inter-avulsion timescale.

### 25 7 Conclusions

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Based on a set of bifurcation experiments to test the influence of downstream boundary conditions (deposition vs. bypass) on the flux partitioning and its dynamics, we find:

- Bypass produces a qualitative change in avulsion dynamics compared to deposition. We observe frequent avulsions
  under depositional conditions, but bypass produces long periods of time where one branch dominates. The degree of
  asymmetry also tends to increase under bypass conditions.
- Consistent with existing theory, increasing the width-to-depth ratio of the upstream branch increases flux partitioning asymmetry.

- There are key differences between our experimental results and those of the most relevant existing model (Salter et al., 2018). With net deposition, avulsions are more irregular than those produced by the model. Under bypass conditions, long periods where one branch dominates occur, but unlike in the model, these are not permanent. These differences appear to be related to bar effects in the upstream channel, which are not included in the model.
- The switching timescales of our experiments span a range from bar timescales on the order of minutes of a couple minutes, to downstream-controlled avulsion timescales in the tens of minutes. However, we did not observe enough switches to define a preferred timescale or determine the underlying probability distribution.
  - An additional set of experiments, run with only sand but no water, shows that in the absence of bars, bypass results in complete freezing of the dynamics in a condition where all sediment goes down one branch. These experiments, along with our fluvial experiments, suggest that downstream controls affect the dynamics in a range of physical systems, from river deltas to talus slopes.

Code availability. Code for the SPV model can be downloaded through CSDMS at https://csdms.colorado.edu/wiki/Model:Bifurcation.

Data availability. Underlying experimental data can be obtained through the Digital Repository for University of Minnesota at https://doi.org/10.13020/ngys-r052

15 *Video supplement*. A video supplement can be accessed through the TIB AV-Portal: https://av.tib.eu/series/639/bifurcation+experiments. The same videos are also available in the above data repository.

Competing interests. The authors have no competing interests to report.

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