RESPONSE TO REVIEWERS LETTER

5

Dear Editor:

Attached please find the revised version of the manuscript 'Groundwater erosion of coastal gullies along the Canterbury coast (New Zealand): A rapid and episodic process controlled
10 by rainfall intensity and substrate variability' (esurf-2020-29)**.** My co-authors and I would like to thank you and the reviewer for your comments.

What follows is a point-to-point discussion of these comments and how these have been addressed.

15

Comments made by Editor:

1.   *Line 70: Now that the landscape evolution modeling has been removed,…*

20 I am sorry but I could not understand this comment.

2.   *Table 1: I do not think this table adds much to the presentation of your study. You may consider simplifying this to a few sentences in the text.*

25 This modification has been carried out.

3.   *Figure 1: Colorbar on A is very small and difficult to see in b, the dashed boxes are difficult to discern, consider making a different color*

30 These modifications have been carried out.

4.   *Line 165: "Substrate samples were collected for geochronological analysis."*

We have not carried out this modification because the samples were collected for various
35 analyses. We have re-written the sentence as "Samples included outcropping sediment layers

1

across the cliff face for grain size analyses, sediments with coating for geochemical analyses, and loess sediments for geochronological analysis".

5.   *Line 177: Suggestion to change to centimeter-scale*

This modification has been carried out.

6.   *Line 203: "Has previously been successful in coastal hydrogeophysical studies"*

This modification has been carried out.

7.   *Line 274: be explicit that this is groundwater, not surface, water flow*

This modification has been carried out.

8.   *Line 306: Indicate the components of the model that this would affect (permeability)*

The sentence has been rewritten as "Each scenario is modelled for two sandy gravel slopes with different permeabilities - one with a 0.5 m thick sand lens and the other with a 0.5 m thick gravel lens".

9.   *Line 308: So RocScience solves equation 2? Is there a relevant citation for this? The order of operations of the modeling here is a bit confusing. I assume Slide2 is solving equations 1 and 2. Are equations 3-7 then being solved used a routine from Micallef et al 2020? What from this water modeling approach is being passed back to Slide2? If there are quantities being passed back to account for transient changes in pore fluid pressure and water flow, I cannot find those variables in the slope stability equation presented. Please clarify.*

Slide2 solves equation 3 to solve equation 2, but unfortunately we have no relevant citation for this. Slide2 also solves equations 4 to 7 to model groundwater flow and estimate pore fluid pressure, which is separate from the slope stability equation. We have included the equations for pore water pressure, which were missing in the revised manuscript.

10.   *Line 319: Distribution of what quantity about the gullies? Their position?*

Here we are referring to their spatial distribution. This is now clarified in the text.

11. *Figure 2: Perhaps plot figure c in loglog space so data in the 1-10 and 10-100 range is more visible.*

This modification has been carried out.

12. *Line 332: In plan view*

This modification has been carried out.

13. *Line 341: Delete initial part of sentence*

We think it is important to include this information because the number of gullies increases later in the year.

14. *Line 371: Reorder sentence to refer to these in order.*

This modification has been carried out.

15. *Line 384: Specify uncertainty or say "approximately"*

We have included the word "approximately".

16. *Line 384: I find this statement confusing, I thought there were only two surveys, one in May and one in October?*

In section 3.2 we had specified the dates of the fourteen UAV surveys.

17. *Line 389: Replace with "occurred"*

This modification has been carried out.

3

18. *Figure 4: The positioning of these are confusing. I would suggest a left to right comparison instead as it is more intuitive to read that way. As I was going through I was initially confused why there was no erosion specified in some of the rows.*

This modification has been carried out.

19. *Figure 5: This figure has quite a lot of white space and the overlapping of precipitation and groundwater are hard to see. It might look better if you made this two panels so you could shrink the figure and not obscure the lab between the precipitation and groundwater data.*

I am not sure I understand what is being recommended. I have tried dividing the figure into two panels and it results in a larger figure with more white space. I thought it may be better to leave the figure as it is so that the readers can see that there was no gully erosion when rainfall intensity was less than 40 mm per day.

20. *Line 401: Can you quantify your volume uncertainty?*

The uncertainty is now included in the figure legend.

21. *Figure 6b: The quality of this graph is very low, and the peak storms are very hard to see. Perhaps a better strategy would be to report the mean and peak rainfall for each time interval between photos. This time series is not very informative as it is currently presented.*

The bars in the graph have been made more visible and the dates for the satellite images are now labelled.

22. *Figure 7: This figure is very confusing. Please try and clarify. Please give each individual element of this figure a different letter and reference. There are two A's and two B's which makes this very confusing. Please create legend items for each plot that include what the different colors of scatter points, vs. the smooth gold line are. Is the smooth gold a model or a best fit? May be useful to label the resistivity for sea water as you cite this as a marker for the model performance to be poor.*

These modifications have been carried out. We have also moved Figure 7b to Figure 8.

23. *Line 447: But how much spatial variability is meaningful? What is the minimum scale of variability that can be interpreted as a discrete lens of gravel or sand?*

The following text has been included: In general, due to lengthy signal-averaging times, ambient electromagnetic noise from the environment adds very small contribution to TDEM responses such that any along-profile variations are likely caused by geological heterogeneity. However, there is not a straightforward relationship between the magnitude of the TDEM voltage at any given time-gate and the resistivity within a particular subsurface volume. The situation becomes more complicated since the true Earth is characterised by multiscale heterogeneity such that spatial variations in the geology at all length scales superimpose their individual responses on one another to produce the final overall TDEM response that is measured. Thus, any analysis of the spatial variability of a time-gate plot, while informative, is largely qualitative and indicates only a first-order spatial distribution of causative subsurface structures.

24. *Line 449: It seems that this would be more appropriate with the actual time-gate data that you are showing in Figure 8. By keeping it in Figure 7, the reader will try and compare directly to other portions of figure 7, which may reduce the clarity of the manuscript.*

We have moved Figure 7b to Figure 8.

25. *Line 449: It seems that this would be more appropriate with the actual time-gate data that you are showing in Figure 8. By keeping it in Figure 7, the reader will try and compare directly to other portions of figure 7, which may reduce the clarity of the manuscript.*

We have moved Figure 7b to Figure 8.

26. *Figure 8: See previous comment of pairing Figure 7b with this figure. I do not think that insets are the clearest way to show this as it decreases the visualization of your time-gate profiles. I would suggest instead that you create a tiled plot with the image on the left and the associated time gate profiles on the right at a scale where they are easy to see. Please label the axes of the time gate figures. Please label Y axis of time gate graphs.*

These modifications have been carried out.

27. *Figure 9: Labels of these on the plots would make it easier for readers to differentiate at a glance. It would be really useful to see the time series of precipitation vs. the time series of Ff in addition to these plots, so readers can get a better idea of what the model is doing.*

What time in the model run does this represent? Please add this as a legend to the plot as well (or put in a text label).

These modifications have been carried out. The results shown are for the end of the simulation for each scenario. Unfortunately we were unable to generate the time series of precipitation vs. factor of safety in the time available.

28. *Please combine with previous figure, similar to next figure. Is plot C continuous data or discrete points? Is this for the entire model run or the ending point?*

These modifications have been carried out. The data are discrete. The results shown are for the end of the simulation for each scenario.

29. *Figure 11: Include a plot similar to 10c? or remove 10c? I would recommend making these consistent. What are the red dots in this and the previous plot? Please label and refer to in caption or remove.*

These modifications have been carried out. The red dots have been removed.

30. *Line 545: Where does this come from? I assume model output, but this is not mentioned or presented as a result of the study, so it is a bit confusing to talk about seepage flux here. If the argument is that seepage flux is a key term in erosion (which I feel like it is), it may be useful to show us that model output prior to the discussion.*

This observation has now been moved to the Results section.

31. *Line 591: Where does this rainfall intensity threshold come from? The modeling or the observational data. If this is from observational data, given the temporal spacing of your repeat surveys, how do you identify this threshold?*

We now explain that the threshold value is based on UAV and satellite imagery observations, which show that gullies form after rainfall events with an intensity higher than 40 mm per day (Figs. 5, 6), and the plot of factor of safety with rainfall intensity from the slope stability model for the first scenario ((I-D)3 for the slope with sand lens (Fig. 9).

Comments made by Reviewer 1:

215

32. *Line 25ff: Note that the "OSL" ages in the paper are not actually optically stimulated luminescence derived ages. They are from related methods within the broader field of trapped-charge dating. I recommend replacing all references to OSL or Optically Stimulated Luminescence dating with the more general term: "luminescence dating"*

220

(alternatively, you could also use infrared stimulated luminescence dating; IRSL)

We have now replaced "optically stimulated luminescence dating" with "luminescence dating" everywhere. When the ages obtained in this study are discussed, we use "infrared stimulated luminescence ages".

225

33. *Line 49: add a comma between "changes" and "such as"*

This modification has been carried out.

230

We hope that we have managed to address all your concerns and that you are satisfied with the above changes.

235 With best regards also on behalf of my co-authors,

Aaron Micallef

Groundwater erosion of coastal gullies along the Canterbury coast (New Zealand): A rapid and episodic process controlled by rainfall intensity and substrate variability

Aaron Micallef[1,2], Remus Marchis[3], Nader Saadatkhah[1], Potpreecha Pondthai[4], Mark E. Everett[4], Anca Avram[5,6], Alida Timar-Gabor[5,6], Denis Cohen[2], Rachel Preca Trapani[2], Bradley A. Weymer[1], Phillipe Wernette[7]

[1]Helmholtz Centre for Ocean Research, GEOMAR, Kiel, Germany
[2]Marine Geology & Seafloor Surveying, Department of Geosciences, University of Malta, Malta
[3]Department of Geological Sciences, University of Canterbury, Christchurch, New Zealand
[4]Department of Geology and Geophysics, Texas A&M University, Texas, USA
[5]Faculty of Environmental Science and Engineering, Babes-Bolyai University, Cluj-Napoca, Romania
[6]Interdisciplinary Research Institute on Bio-Nano-Sciences, Babeş-Bolyai University, Cluj-Napoca, Romania
[7]School of the Environment, University of Windsor, Ontario, Canada

Correspondence to: Aaron Micallef (amicallef@geomar.de)

Abstract: Gully formation has been associated to groundwater seepage in unconsolidated sand to gravel sized sediments. Our understanding of gully evolution by groundwater seepage mostly relies on experiments and numerical simulations, and these rarely take into consideration contrasts in lithology and permeability. In addition, process-based observations and detailed instrumental analyses are rare. As a result, we have a poor understanding of the temporal scale of gully formation by groundwater seepage and the influence of geological heterogeneity on their formation. This is particularly the case for coastal gullies, where the role of groundwater in their formation and evolution has rarely been assessed. We address these knowledge gaps along the Canterbury coast of the South Island (New Zealand) by integrating field observations, ~~optically stimulated luminescence dating~~luminescence dating, multi-temporal Unoccupied Aerial Vehicle and satellite data, time-domain electromagnetic data, and slope stability modelling. We show that gully formation is a key process shaping the sandy gravel cliffs of the Canterbury coastline. It is an episodic process associated to groundwater flow that occurs once every 227 days on average, when rainfall intensities exceed 40 mm per day. The majority of the gullies in a study area SE of Ashburton has undergone erosion, predominantly by elongation, during the last 11 years, with the most recent episode occurring 3 years ago. Gullies longer than 200 m are relict features formed by higher groundwater flow and surface erosion >2 ka ago. Gullies can form at rates of up to 30 m per day via two processes: the formation of alcoves and tunnels by groundwater seepage, followed by retrogressive slope failure due to undermining and a decrease in shear strength driven by excess pore pressure development. The location of gullies is determined by the occurrence of hydraulically-conductive zones, such as relict braided river channels and possibly tunnels, and of sand lenses exposed across sandy gravel cliff. We also show that gully planform shape is generally geometrically similar at consecutive stages of evolution. These outcomes will facilitate reconstruction and prediction of a prevalent erosive process and overlooked geohazard along the Canterbury coastline.

8

1   Introduction

1.1   Coastal gullies

285   Gullies can be incised into coastal cliffs and bluffs in a variety of geologic settings around the world, owing their formation to a complex interaction of hydrologic, lithospheric, tectonic, and atmospheric processes. While much research has focused on gully formation and evolution in non-coastal settings in response to changes, such as land cover and use, natural hazards, and/or changes in precipitation, relatively little work has focused on gully geomorphology and morphodynamics in coastal cliffs and bluffs. The most commonly accepted mechanism for

290   coastal gully formation is through concentrated overland flow and knickpoint migration (Leyland and Darby, 2008; Leyland and Darby, 2009; Limber and Barnard, 2018; Mackey et al., 2014; Ye et al., 2013). Changes in land cover and use due to agriculture, logging, forest fire, and other factors can decrease surface roughness and increase concentrated overland flow, which, given sufficient energy and/or time, can erode a narrow section of coastal cliff and form a knickpoint. Depending on the resistive forces (e.g. geology, uplift) relative to the erosive

295   force of the overland flow, this knickpoint will migrate inland over time, incising a gully into the cliff or bluff. Recent work has focused on modelling coastal gully formation and evolution as knickpoint migration (Limber and Barnard, 2018).

Coastal cliff stability and gully incision can be affected by processes of concentrated overland flow, quarrying by

300   waves at the base of the cliff, and groundwater discharge (Kline et al., 2014; Limber and Barnard, 2018), although it is unclear when and where each of these factors is important (Collins and Sitar, 2009; Collins and Sitar, 2011). While overland flow is a common formation mechanism, it is possible to have coastal gullies form where the cliff is affronted by a beach, which limits the basal quarrying or notching by waves, and where there is no outward sign of overland flow. Relatively little attention has been paid to the potentially important role of groundwater as

305   a driver of coastal gully formation and evolution, despite the potential for groundwater to affect the geotechnical properties of coastal cliffs (Collins and Sitar, 2009; Collins and Sitar, 2011).

1.2   Channel erosion by groundwater seepage

310   Groundwater has been implicated as an important geomorphic agent in channel network development, both on Earth and on Mars (Abotalib et al., 2016; Dunne, 1990; Harrison and Grimm, 2005; Higgins, 1984; Kochel and Piper, 1986; Malin and Carr, 1999; Salese et al., 2019). The classic model entails a channel headwall that lowers the local hydraulic head and focuses groundwater flow to a seepage face. This leads to upstream erosion by undercutting, the rate of which is limited by the capacity of seepage water to transport sediment from the seepage

315   face (Abrams et al., 2009; Dunne, 1990; Howard and McLane, 1988). Groundwater seepage has been shown to unambiguously lead to channel formation in unconsolidated sand to gravel sized sediments (Dunne, 1990; Lapotre and Lamb, 2018) (Table 1): e.g. gravel braided river deposits in Alaska (Sunderlin et al., 2014) and Canterbury Plains (Schumm and Phillips, 1986), conglomerates in the Kalahari (Nash et al., 1994), outwash and alluvial sands in Florida (Schumm et al., 1995), Martha's Vineyard (Uchupi and Oldale, 1994) and Vocorocas (Coelho Netto et

320   al., 1988), dune sand and tephra in South Taranaki (Pillans, 1985), and granodorite regolith in the Obara area of

9

Japan (Onda, 1994). In sediments finer than sands, erosion is typically limited by detachment of the grains at the seepage face. In silts and clays, the permeability is so low that the groundwater discharge is often less than that required to overcome the cohesive forces of the grains (Dunne, 1990). The role of groundwater seepage and channel formation in bedrock, on the other hand, remains controversial (Lamb et al., 2006; Pelletier and Baker, 2011).

Table 1: Examples of studies documenting channels attributed to groundwater seepage erosion in unconsolidated sediments (sand- to gravel-sized).

Location	Substrate type	Reference
Alaska, USA	Gravel braided river deposits	(Sunderlin et al., 2014)
Canterbury Plains, New Zealand	Gravel braided river deposits	(Schumm and Phillips, 1986)
Florida Panhandle, USA	Non-marine quartz sands that contain discontinuous layers of clay or gravel	(Schumm et al., 1995)
Kalahari, southern Africa	Conglomerates, marls, duricrusts and unconsolidated sands	(Nash et al., 1994)
Martha's Vineyard and Nantucket Island, USA	Outwash gravelly sand	(Uchupi and Oldale, 1994)
Obara area, Japan	Granodiorite regolith	(Onda, 1994)
South Taranaki, New Zealand	Terrestrial dune sand and tephra overlying marine sands and gravels	(Pillans, 1985)
Vocorocas, Brazil	Alluvial sands	(Coelho Netto et al., 1988)

Our understanding of channel evolution by groundwater seepage is predominantly derived from theoretical, experimental and numerical models (Chu-Agor et al., 2008; Higgins, 1982; Howard, 1995; Lobkovsky et al., 2004; Pelletier and Baker, 2011; Petroff et al., 2011; Wilson et al., 2007). Such studies suggest that the velocity at which channel heads advance is a function of groundwater flux and the capacity of seepage water to transport sediment from the seepage face (Abrams et al., 2009; Fox et al., 2006; Howard, 1988; Howard and McLane, 1988), and that channel head erosion occurs by episodic headwall slumping (Howard, 1990; Kochel et al., 1985). Channels incised by groundwater seepage have been shown to branch at a characteristic angle of 72° at stream tips, which increases to 120° near stream junctions (Devauchelle et al., 2012; Yi et al., 2017), whereas growing indentations competing for draining groundwater result in periodically-spaced channels (Dunne, 1990; Schorghofer et al., 2004). Channel network geometry appears to be determined by the external groundwater flow field rather than flow within the channels themselves (Devauchelle et al., 2012).

A number of fundamental questions related to the evolution of channels by groundwater seepage in unconsolidated sediments remain unanswered. Firstly, the temporal scale at which channels form is poorly quantified due to a paucity of process-based observations and detailed instrumental analysis. Field observations of groundwater processes are rare (e.g. Onda, 1994), primarily due to the difficulty with accessing the headwalls of active channels, the potential long timescales involved, and the complexity of the erosive process (Chu-Agor et al., 2008; Dunne, 1990). Quantitative assessments of channel evolution have relied on experimental and numerical analyses, but these tend to be based on simplistic assumptions about flow processes and hydraulic characteristics. Experimental approaches are based on a range of different methods, which limits comparison of their outcomes (Nash, 1996). Published erosion rates vary between 2-5 cm per century (Abrams et al., 2009; Schumm et al., 1995)

and 450-1600 m^3 per year (Coelho Netto et al., 1988). Secondly, the influence of geologic heterogeneities on channel evolution is also poorly understood. Lithological strength and permeability contrasts are rarely simulated by experimental and numerical analyses. Thirdly, there only a few places where the mechanisms by which seepage erosion occurs have been clearly defined (e.g. Abrams et al., 2009). Basic observations and measurements of channel erosion rates and substrate geologic heterogeneities are needed to test and quantify models for channel formation and improve our ability to reconstruct and predict landscape evolution by groundwater-related processes.

1.3   Objectives

In this study we revisited the Canterbury Plains study site (Schumm and Phillips, 1986) and carried out field observations, geochronological analyses, repeated remote sensing surveys, near-surface geophysical surveying and slope stability modelling of coastal gullies to: (i) identify the processes by which groundwater erodes gullies along the coast, (ii) assess the influence of geological/permeability heterogeneity on the gully formation process, and (iii) quantify the timing of gully erosion and its key controls.

2   Regional setting

The flat to gently inclined Canterbury Plains, located in the eastern South Island of New Zealand, extend from sea level up to 400 m above sea level, and cover an area of 185 km by 75 km (Fig. 1a). A series of high energy braided rivers emerge from the >3500 m high Southern Alps and flow south-eastwards to the shoreline (Kirk, 1991). The plains were formed by coalescence of several alluvial fans sourced from the these rivers (Browne and Naish, 2003; Leckie, 2003). The Quaternary sedimentary sequence comprises a >600 m thick succession of cyclically stacked fluvio-deltaic gravel, sand and mud with associated aeolian deposits and palaeosols (Bal, 1996; Browne and Naish, 2003). The gravels consist of greywacke and represent a variety of channel fill beds and bar forms, whereas the isolated bodies of sand are relict bars and abandoned channels. The interglacial sediments are better sorted and have higher permeability than the glacial outwash, resulting in a wide range of hydraulic conductivities (Scott, 1980). New Zealand's largest groundwater resource is hosted in the gravels down to at least 150 m depth (Davey, 2006). The upper Quaternary sediments are exposed along a 70 km long coastline south-west of the Banks Peninsula (Moreton et al., 2002). This coastline is retrograding at approximately 0.5–1 m per year and consists of cliffs fringed by mixed gravel and sand beaches (Gibb, 1978). The study area is a 2.5 km long stretch of cultivated coastline located 16 km to the south-east of Ashburton (Fig. 1b). The coastline within the study area consists of a 15-20 m thick exposure of poorly-sorted and uncemented matrix-supported outwash gravel, which is capped by up to 1 m of post-glacial loess and modern soil (Berger et al., 1996). The cliff face is punctuated by ~0.5 m thick lenses of sand or clean gravel.
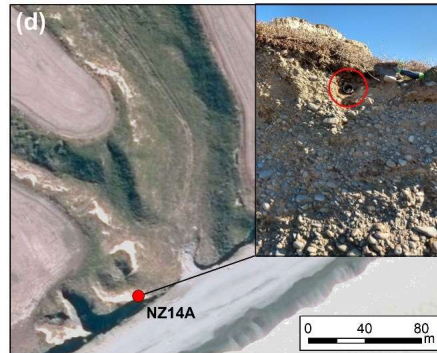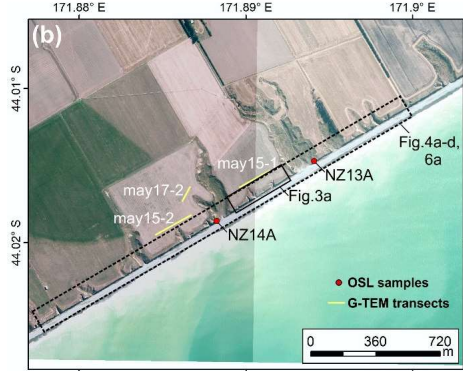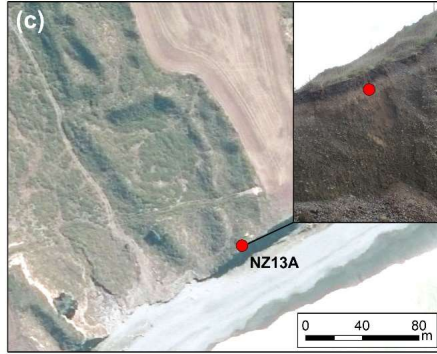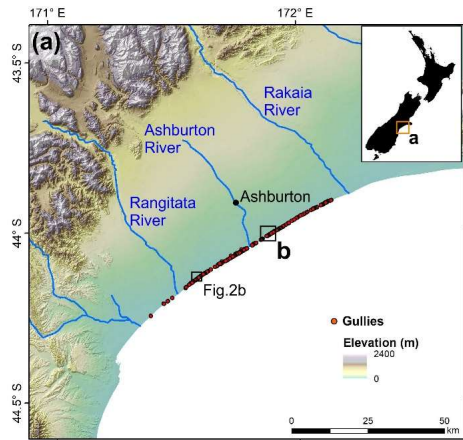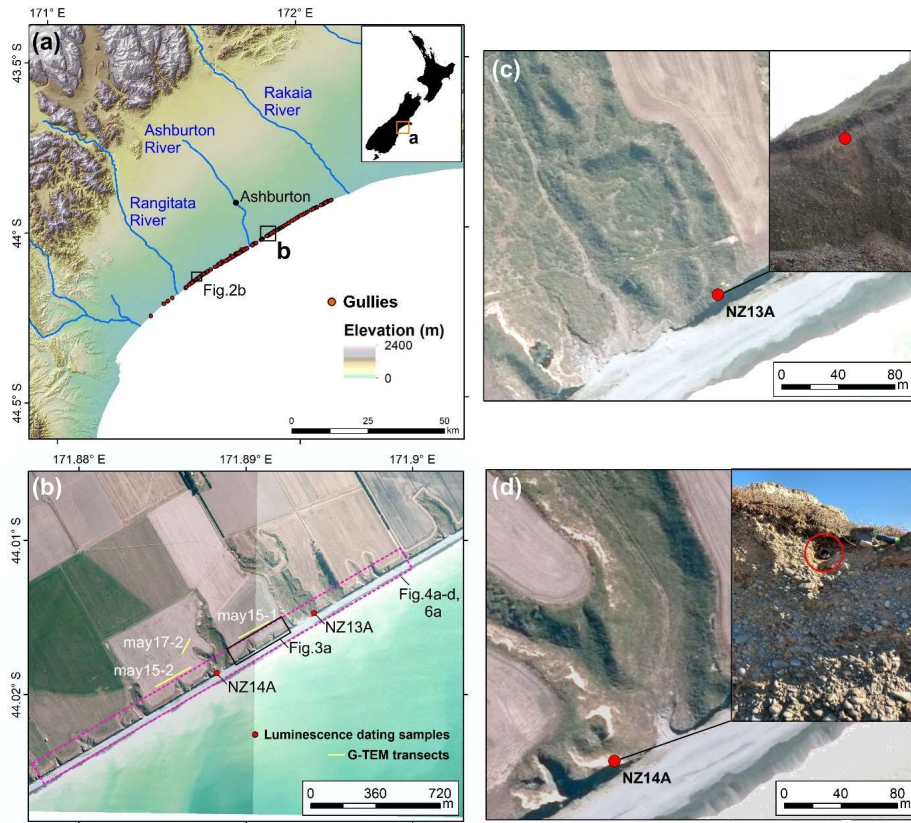
Figure 1: (a) Digital elevation model of the Canterbury Plains (source: Environment Canterbury), located along the eastern coast of the South Island of New Zealand, showing the location of mapped gullies. Location of figure is shown in inset. (b) Mosaic of aerial photographs of the study area (source: Environment Canterbury). Location in a. Location of ~~Optically Stimulated Luminescence~~**luminescence dating (OSL) samples, G-TEM transects, and other figures is shown. (c-d) Zoomed sections of the aerial photograph and site photographs of the** ~~OSL~~ **luminescence dating sampling sites NZ13A and NZ14A.**

3 Materials and Methods

3.1 Data

3.1.1 Field visits

Site visits were carried out in May 2017 and 2019. During these visits, geomorphic features of interest were noted and photographed, and samples collected. ~~The~~ Samples included outcropping sediment layers across the cliff face for grain size analyses, sediments with coating for geochemical analyses, and loess sediments for

14

410 geochronological analysis~~latter included outcropping sediment layers across the cliff face, sediments with coating, and loess sediments for geochronological analysis~~ (NZ13A, NZ14A; Fig. 1). The latter were collected from the base of the loess draping the flanks of the two largest gullies, above the boundary with the underlying gravels, by hammering stainless steel tubes into the sediment and ensuring that the material was not exposed to light.

415 ### 3.1.2 Unoccupied aerial vehicle (UAV) surveys

UAV surveys were carried out using DJI Phantom 4 Pro and DJI Mavic Pro drones. The surveys were carried out after rainfall events and on the following dates: 11th May, 19th June, 30th June, 11th July, 15th July, 23rd July, 29th July, 4th August, 26th August, 11th September, 23rd September, 6th October, 13th October and 30th October 2017.

420 The drones were flown at an altitude of 40-55 m, speed of 5 m s^{-1}, and side lap of 65-70%. Eight ground control points were selected and their location and elevation were determined by differential GPS with ~~centimetric~~ centimetre-scale horizontal and vertical accuracy. Orthophotos and digital elevation models with a horizontal resolution of 10 cm/pixel were generated from the UAV data using Drone Deploy. The mean distance between the ground control points and the generated orthophoto and model grid cell centres was 0.03 m. Root-mean square

425 and bias were used to estimate the vertical accuracy of the digital elevation models (equations in Laporte-Fauret et al., 2019). The root-mean square error and bias were 0.05 m and 0.03 m, respectively. The model elevations were slightly underestimated (0.1 m).

3.1.3 Near-surface geophysics

430

Time-domain electromagnetic (TEM) measurements were carried out in May 2019 using the Geonics (Canada) G-TEM system (Fig. 1b). The operating principles of the inductive TEM technique are described in Nabighian and Macnae (1991) and Fitterman (2015). The survey parameters included 4 turns, a 10×10 m^2 square TX loop, and a TX current output of 1 A. The G-TEM was operated in a fixed offset-sounding configuration, which is

435 termed "Slingram" mode, in which the RX coil was placed 30 m from the centre of the TX loop and the TX-RX pair moved together along a linear transect at 5 m station spacing, maintaining the 30 m offset. The maximum depth of investigation of the G-TEM system is given approximately by the formula:

$$d = 8.94L^{0.4}\rho^{0.25} \tag{1}$$

440

where L (m) is the TX loop size and ρ (Ωm) is the upper layer resistivity (Geonics, 2016). Setting ρ=100 Ωm yields a depth of investigation of d=71 m, whereas ρ=1000 Ωm yields d=126 m. Our investigation depth in New Zealand may be slightly greater than these values since the Geonics formula assumes a 1-turn TX loop carrying current 3 A, whereas we used a more powerful combination of 4 turns at 1.5 A. At each station, a consistent 1-D

445 smooth model of electrical resistivity vs. depth was performed based on the iterative Occam-regularised inversion method (Constable et al., 1987) and using IXG-TEM commercial software (Interpex, 2012). This is a standard 1-D TDEM inversion code that has previously been successfully used in coastal hydrogeophysical studies ~~been successfully used for coastal hydrogeophysical studies~~ (e.g. Pondthai et al., 2020).

3.1.4 Other data

Satellite images with a horizontal resolution of 1 m/pixel and dating back to 2004 were obtained from Google Earth. Precipitation records dating back to 1927 were provided by Environment Canterbury. The latter also provided a time series of water level data since 2015 from a 30 m deep well located 10 km to the north-east of the study area.

3.2 Methods

3.2.1 Sample analyses

Sediment samples were analysed for grain size distribution using sieves following the ASTM D0422 protocol. The composition of the coating on selected sediment outcrops within the gullies was determined using X-ray fluorescence.

3.2.2 ~~Optically Stimulated~~ Luminescence ~~(OSL)~~ dating

Luminescence dating is numerical-age technique that uses optically and thermally sensitive signals measured in the form of light emissions in the constituent minerals that form sediment deposits. Quartz and feldspars are among the most often used minerals. Sediment ages obtained via luminescence dating reflect the last exposure of the analysed mineral grains to daylight, when the resetting (called bleaching) of the previously incorporated luminescence signal occurs.

In order to obtain luminescence ages, two types of measurements were performed. The dose accrued by the crystal from natural radioactivity since its last exposure to daylight (called the palaeodose) was determined as an equivalent dose (D_e). This was done by measuring the light emission of the crystal upon optical stimulation, and matching this emission to signals generated by the exposure to a known dose of radiation given in the laboratory. This is expressed as the amount of absorbed energy per mass of mineral (1 J kg^{-1} = 1 Gy (Gray)). Radioactivity measurements were carried out on each sample in order to determine the annual dose (D_a), which represents the rate at which the environmental dose was delivered to the sample (Gy ka^{-1}). The age was obtained by dividing the two determined parameters. As low luminescence sensitivity and poor dosimetric characteristics were reported for quartz from sediments in New Zealand (see Preusser et al. (2009) and the references cited therein) we have used signals from feldspars by the application of infrared stimulation based on the post IR-IRSL$_{225}$ (Buylaert et al., 2009) and post IR-IRSL$_{290}$ (Thiel et al., 2011) protocols on polymineral fine (4-11µm) grains, as well as coarse (63-90 µm) potassium feldspars.

A detailed description of luminescence dating methodology, including sample preparation, equivalent dose determination, annual dose determination, luminescence properties (including residual doses, dose recovery tests and fading tests), is presented as Supplementary Materials.

3.2.3 Morphological change detection

The method used to measure gully aerial erosion in between surveys entailed the manual delineation of shapefiles around gully boundaries for each survey (using orthophotos, digital elevation models and slope gradient maps in the case of the UAV data, and satellite images in the case of the Google Earth data), the estimation of their areas, and the comparison of the latter in between surveys. The uncertainty inherent in this approach is related to the digitisation of the gully boundaries. We made sure that a vertex was added at least every 5 pixels for both the UAV (0.5 m) and Google Earth data (5 m). This ensures that a minimum erosion of 0.25 m^2 (in the case of the UAV data) and 25 m^2 (in the case of the Google Earth data) was detected.

3.2.4 Slope stability modelling

We developed a slope stability model based on the limit equilibrium and segmentation strategy of the Bishop method, where a soil mass is discretised into vertical slices. The factor of safety F_f is calculated using the following (Fredlund and Krahn, 1977; Fredlund et al., 1981):

$$F_f = \frac{\sum (c' \beta \cos\alpha + (N - u\beta) \tan\phi' \cos\alpha)}{\sum N \sin\alpha - \sum D \cos\omega} \tag{2}$$

where c' (in kPa) is effective cohesion, ϕ' (in °) is effective angle of friction, u (in kPa) is pore-water pressure, D (in kN) is concentrated point load, β (in m) represents the slice base length, ω (in °) is the angle between the top part of the slope and surface forces, and α (in °) is inclination of the slice base. N is the normal force acting on the slice base and can be computed by:

$$N = W \cos\alpha - kW \sin\alpha + [D \cos(\omega + \alpha - 90)] \tag{3}$$

where W (in kN) is slice weight (unit weight γ_s (in kN m^{-3}) × volume (in m^3)) and k is hydraulic conductivity (in m s^{-1}).

We also modelled the groundwater flow and pore pressure distribution within the soil using the Poisson equation, which is the generalised form of the Laplace equation (Whitaker, 1986):

$$k_x \frac{\partial^2 h}{\partial x^2} + k_y \frac{\partial^2 h}{\partial y^2} = q \tag{4}$$

where q is the total discharge (m^3 s^{-1}), k_x and k_y are equal to the hydraulic conductivity (m s^{-1}) in the horizontal and vertical directions, respectively, and h is the hydraulic head (m).

17

Equation (4) applies to water flow under steady-state and homogeneous conditions, whereas the following equation is applicable to dynamic and inhomogeneous conditions:

$$\frac{\partial}{\partial_x}(k_x \frac{\partial h}{\partial x}) + \frac{\partial}{\partial_y}(k_y \frac{\partial h}{\partial y}) = q + \frac{\partial \theta}{\partial t}$$ (5)

where $\partial \theta / \partial t$ describes how the volumetric water content changes over the time.

The water transfer theory accounts for transient behaviour, which can be defined by the following equation (Domenico and Schwartz, 1997):

$$M_{st} = \frac{dM_{st}}{dt} = m_{in} - m_{out} + M_s$$ (6)

where m_{in} is the cumulative mass of water that enters the porous medium, m_{out} is equal to the mass of water that leaves the porous medium, and M_s is the mass source within the representative elementary volume. The rate of increase in the mass of water stored within the representative elementary volume is:

$$M_{st} = M_w + M_v$$ _____ (7)

where Mw and Mv represent the rate of change of liquid water and water vapour, respectively.

The relationship between water level and changes in pore water pressure can be expressed by:

$$u = \rho_w\, g\, h_w$$ (8)

where ρ_w is the water density, and h_w is the height of the water column.

Changes in vertical stress due to changes in pore water pressure can be represented by the pore water pressure coefficient $\bar{B}$ (Skempton, 1954), which is defined as:

$$\bar{B} = \Delta u / \Delta \sigma_1$$ (9)

where $\Delta \sigma_1$ is the change in the major principal stress, which is often assumed, for simplicity, to be equal to the change in vertical stress (σv). The coefficient then becomes:

$$\bar{B} = \Delta u / \Delta \sigma v$$ (10)

18

$\bar{B}$ is a general way of describing pore water conditions in a slope stability analysis.

565

The mechanical and hydraulic soil properties employed in this model are listed in Table 1 and were obtained from Dann et al. (2009) and Aqualinc Research Limited (2007). We modelled two scenarios, based on the available rainfall data (see Sect. 4.4). The first is a 3-day long intense rainfall event ((I-D)$_3$) covering the period

570   20th July – 22nd July 2017. The second is a 14-day period with occasional, low intensity rain ((I-D)$_{14}$) between the 21st June and 4th July 2017. Each scenario is modelled for two sandy gravel slopes with different permeabilities, one with a 0.5 m thick sand lens and the other with a 0.5 m thick gravel lens. Both lenses are located at a height of 5 m above sea-level. Lateral water inflow and surface water infiltration were estimated from the hydrological model in Micallef et al. (2020). Slope stability modelling and groundwater analyses was were carried out using

575   the Slide2 software package by Rocscience.

19

Table 21: Mechanical and hydraulic soil properties used in slope stability modelling.

| Soil type	Unit weight (kN m^{-3})	Cohesion (kPa)	Friction angle (°)	Saturated hydraulic conductivity (m/day)	Residual water content (m^3 m^{-3})	Saturated water content (m^3 m^{-3})
	γ_s	c	φ	k	θr	θs
Sand	20.5	7	34.5	3.216	0.01	0.078
Sandy gravel	23	8	37	0.64	0.01	0.128
Gravel	24	4	36.5	7.376	0.016	0.142

580 **4   Results**

4.1   Gullies along the Canterbury coast - distribution and morphology

We have mapped 315 gullies (locally also known as "dongas") along 70 km of the Canterbury coastline (mean of
585 4.5 gullies per km of coastline). The spatial distribution of the gullies is clustered (nearest neighbour ratio of 0.33
with a z-score of -22.67 and a p-value of 0); the majority of the gullies are located between Rakaia and Rangitata
Rivers (Fig. 1a), particularly in the vicinity of Ashburton River. The heads of many gullies connect to shallow,
relict meandering channels (Fig. 2a). Some of these channels are visible in aerial photographs, in spite of the
terrain having been worked by farmers (Fig. 2b).
590
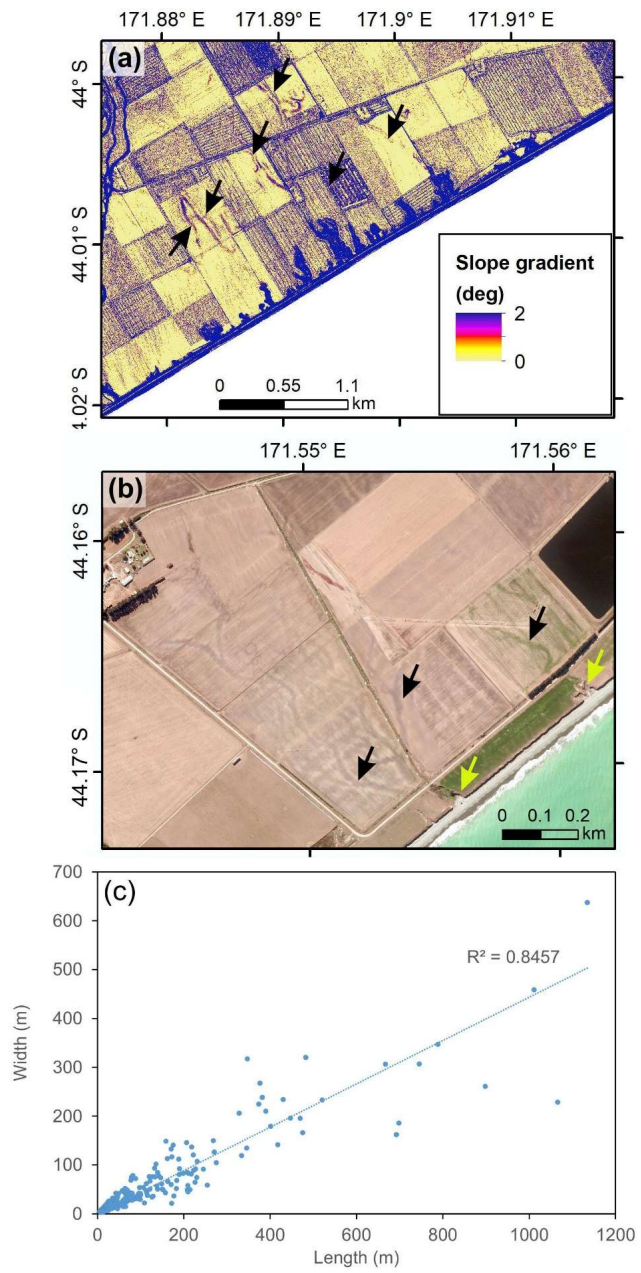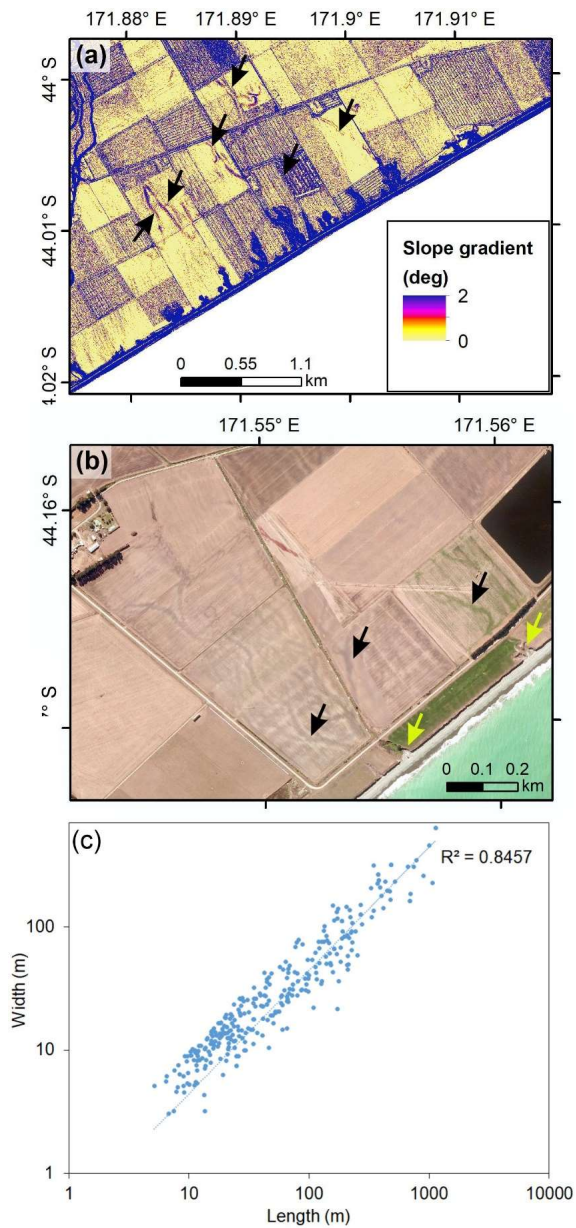
Figure 2: (a) Slope gradient map of the study area. Black arrows indicate relict, infilled channels. (b) Aerial
photograph of Coldstream, Canterbury coast (source: Environment Canterbury). Black arrows indicate
relict, infilled channels. Yellow arrows indicate gullies. Location in Fig. 1a. (c) Plot of length vs. width for
gullies mapped along the Canterbury coastline.

In ~~plan~~plan view, the gullies are predominantly linear to slightly sinuous (sinuosity of 1-1.3) and characterised by a concave head. In profile, the gullies have linear, gently sloping (2-10°) axes, with a concave break of slope separating the axis from a steep (up to 70°) head. In cross-section, the gullies are U-shaped with walls up to 70° in slope gradient. The gullies are between 5 and 1134 m long (mean of 116 m) and between 3 and 637 m wide (mean of 56 m). Gullies generally exhibit a constant width with distance upslope. They have a length to width ratio that varies between 1 and 7.9, with a mean of 2 (standard deviation of 0.89) (Fig. 2c).

4.2   Field site observations

In May 2017, our study area hosted 33 gullies that vary between 15 m and 600 m in length (Figs. 1b; 3a). During the site visits we did not encounter evidence of surface flow. However, the middle to lower sections of the gully walls and cliffs were consistently wet. These sections were also characterised by failure scars and alcoves, particularly above the sandy lenses. Alcoves were also encountered at the base of gully heads, where they were wet and up to 1 m deep (Fig. 3e). Some sandy layers outcropping across the cliff face hosted tunnels (Fig. 3c-d). Above these tunnels, theatre-shaped scars with a shallow and narrow gully at their base were observed (Fig. 3c). At the base of the scars, the gully heads and some gully mouths, we encountered mass movement debris that was occasionally intact and that predominantly consisted of gravel, sandy gravel and loess (Fig. 3c, h). Gullies have gravel-covered irregular floors. Whereas the smaller gullies have a U-shaped cross-section, the three longest gullies have gently sloping V-shaped cross-sections, with loess draping their walls (Fig. 3f). Sandy and clean gravel layers outcropping within the gullies were wet; the former appeared weathered, whereas the latter were coated by Fe and Mn (Fig. 3g). Fences were locally seen suspended across a number of gullies (Fig. 3b).
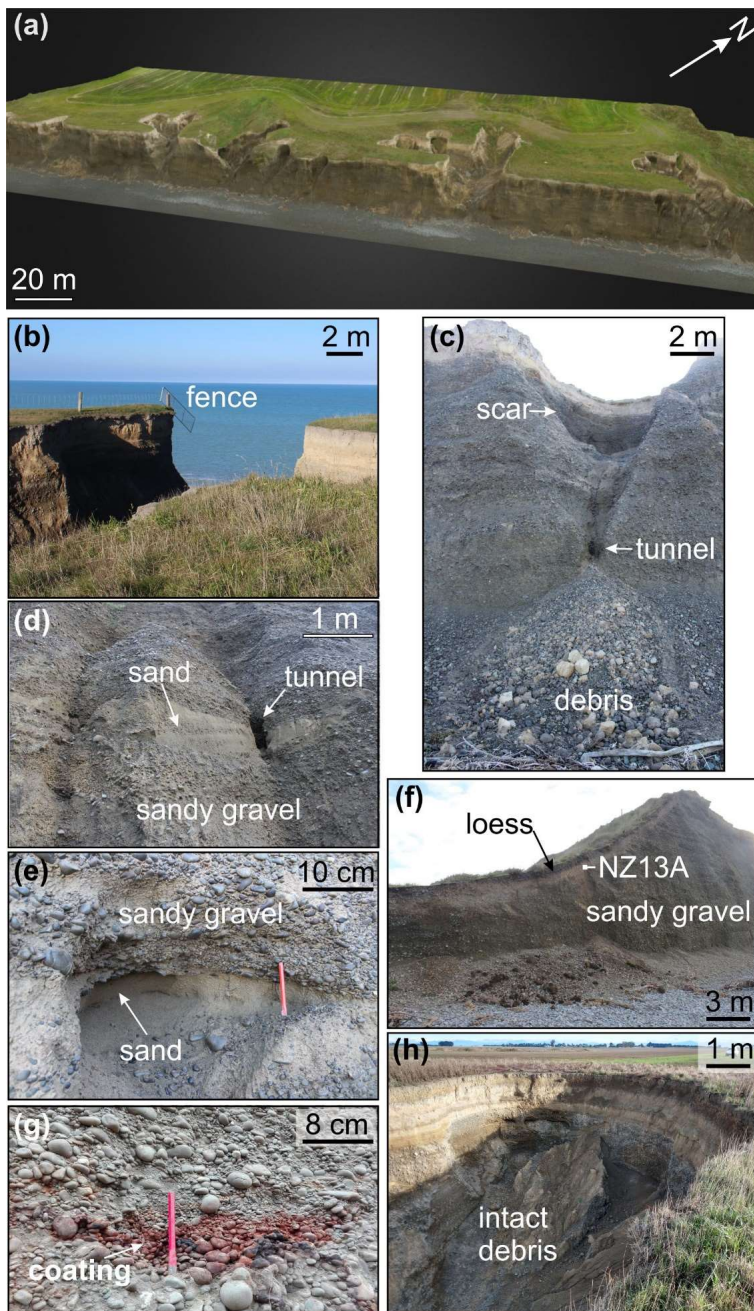
Figure 3: (a) Orthophoto map of part of the study area draped on a 3-D digital elevation model. Location in Fig. 1b. (b-h) Photographs of features of geomorphic interest taken at study area. The location of sample NZ13A is shown in f.

4.3 **Infrared stimulated ~~IL~~uminescence ages**

Four sets of infrared stimulated luminescence ages~~OSL ages~~ are presented in Table ~~3~~2. The pIRIR$_{290}$ ages are higher than the ages obtained by applying pIRIR$_{225}$ protocol. The cause of this difference is not yet fully understood, although it can partially be attributed to the results of the dose recovery test and the poor bleachability of the pIRIR$_{290}$ signals compared to pIRIR$_{225}$ signals (Buylaert et al., 2011). Considering that no anomalous behaviour of the investigated signals was observed (see Supplementary Materials), we are unable to explain the overestimation of the K-feldspar ages compared to the polymineral fine grain ages in the case of NZ13A, especially since the opposite behaviour is observed in the case of sample NZ14A. However, considering a 95% confidence level, infrared stimulated luminescence ages ~~ages~~ obtained using different methods broadly overlap, the only exception being the pIRIR$_{225}$ ages obtained on K-feldspars on sample NZ14A, which we regard as an outlier.

Table ~~2~~3: Summary of the pIRIR$_{225}$ and pIRIR$_{290}$ ages obtained on polymineral fine grains (4-11 µm) and coarse K-feldspars (63-90 µm). The infrared stimulated luminescence ages ~~ages~~ were determined considering 15% water content. Uncertainties are given at 1σ, 68% confidence level. Further details are available in the Supplementary Materials.

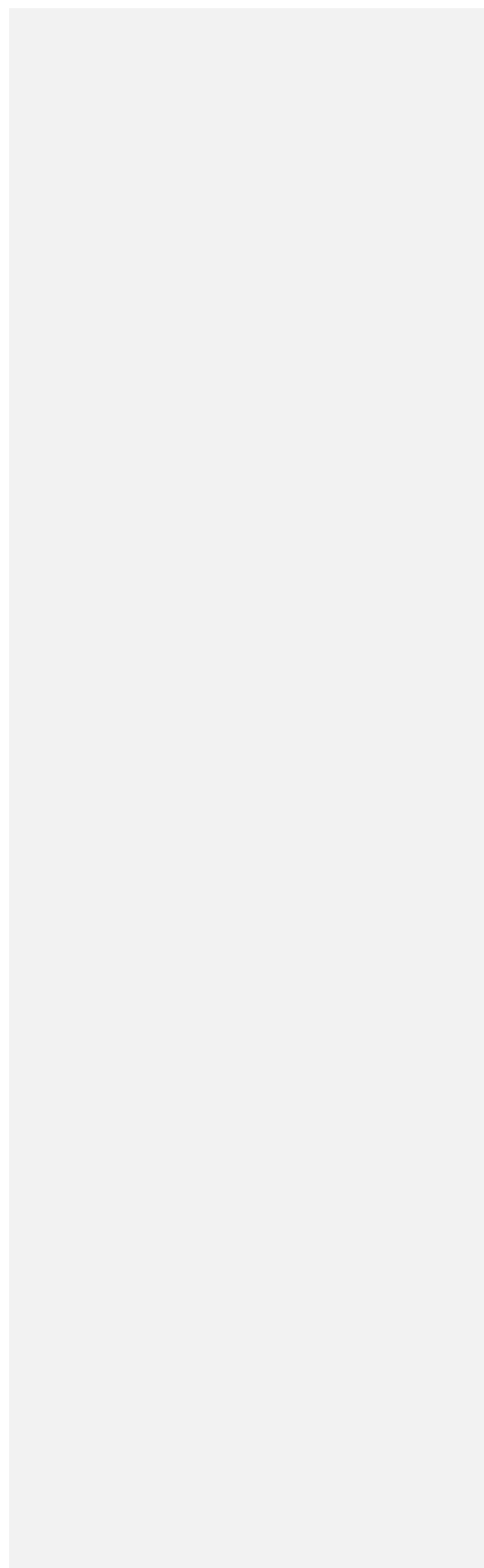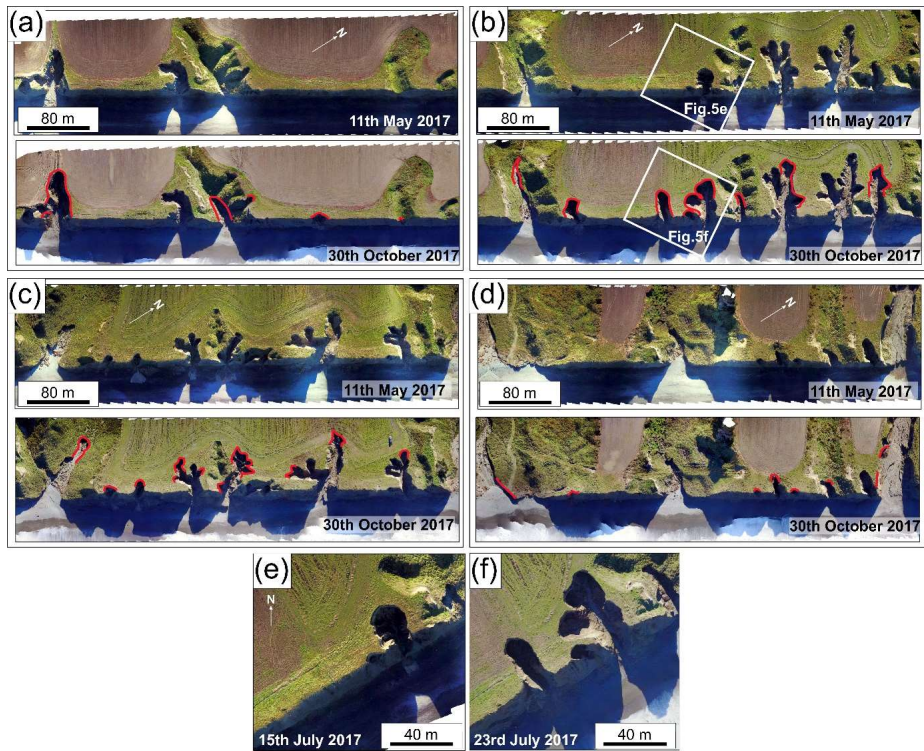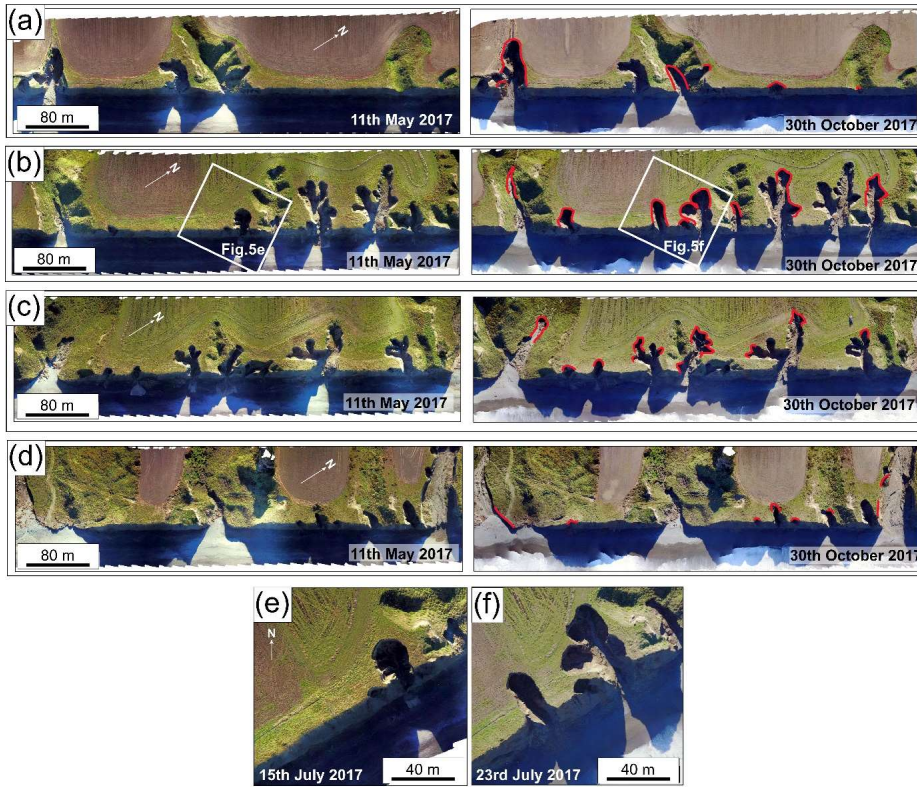|	Age (ka)-pIRIR$_{225}$		Age (ka)-pIRIR$_{290}$	
Sample code	Polymineral fine grains	K-feldspars (63-90 µm)	Polymineral fine grains	K-feldspars (63-90 µm)
NZ13A	16.0±1.4	20.1±1.5	20.9±2.0	26.2±2.1
NZ14A	4.6±0.4	1.9±0.1	6.0±0.7	3.1±0.3

4.4 Morphological changes

4.4.1 **Short term morphological changes**

By comparing the orthophotos and digital elevation models generated from the UAV data acquired during the various site visits between May and October 2017, we document the formation of 3 new gullies (up to 30 m long, Figs. 4e-f) and the enlargement of 30 gullies (primarily by elongation, and occasionally by widening and branching) (Figs. 4a-d). The new gullies formed at locations where there was a small landslide scar in the middle of the cliff. There was no change in form in 3 of the gullies. Figure 5 shows the total area eroded between surveys (which amounts to approximately 3273 m^2), the daily precipitation and the associated changes in water table height. Only three surveys recorded gully erosion. Two of these surveys happened soon after rainfall events of >40 mm in one day (Fig. 5). The most important of these covers the period between the 15th and 23rd July 2017, when 95% of the material was removed and the 3 new gullies were formed (Figs. 4-5). During this period, a total of 153 mm of rain fell (up to 120 mm on the 21st July 2017 alone, which was the most intense rainfall event since 1936), resulting in a 1.5 m rise in the water table. A third survey ~~happened~~ occurred six days after the 21st July 2017 storm, with 22 mm of rain falling in one day. The material eroded from the gullies was deposited at the base

660   of the cliffs as gravel cones, which were remodelled by debris flows during ensuing precipitation events and subsequently disappear from the orthophotos.

(a) 80 m | 11th May 2017 | 30th October 2017

(b) 80 m | Fig.5e | 11th May 2017 | Fig.5f | 30th October 2017

(c) 80 m | 11th May 2017 | 30th October 2017

(d) 80 m | 11th May 2017 | 30th October 2017

(e) N | 15th July 2017 | 40 m

(f) 23rd July 2017 | 40 m

665   **Figure 4: (a-d) Orthophotographs of the study area at the start and end of the UAV surveys, ordered from south-west to north-east. Red lines mark eroded areas. Location in Fig. 1b. Orthophographs from a part of the study area on the (e) 15th July 2017 and the (f) 23rd July 2017. Location in b.**
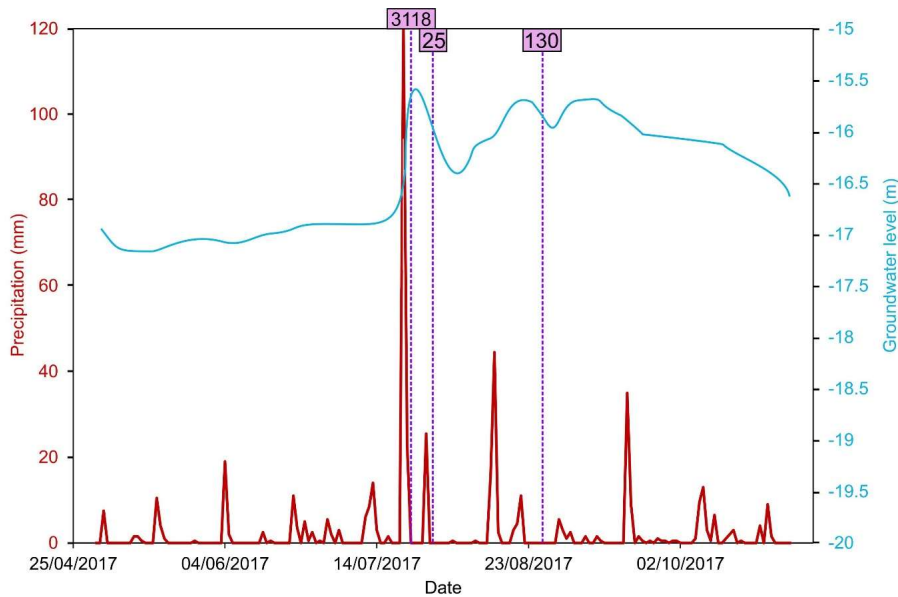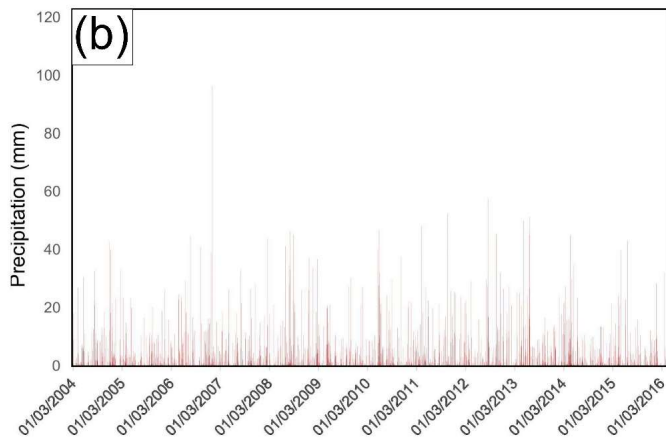
Figure 5: Daily precipitation (for Ashburton Council) and groundwater level records (from a well located 10 km north-east of the study area) for the period 1st May to 31st October 2017 (source: Environment Canterbury). The pink lines mark the surveys when gully erosion was observed (the value in the pink box corresponds to the eroded area in m^2; uncertainty is 0.25 m^2).

Formatted: Superscript

4.4.2   Long term morphological changes

For the period 2004-2015 we have used satellite imagery to map the formation of 6 new gullies and the elongation of 22 gullies. 18 of these erosion episodes are recorded in the image taken on 26th August 2013 (Fig. 6a). This follows a major rainfall event between the 16th and 23rd June 2013, when 171 mm of rain fell in 7 days (with up to 51 mm falling in one day) (Fig. 6b). The other erosion episodes include the 5 gullies eroded by the 28th March 2009, after a storm of 46 mm per day on the 31st July 2008, and the 5 gullies eroded by the 19th October 2015, after a storm of 43 mm per day on the 19th June 2015.

(a)

27th March 2004 — 180 m
24th February 2007
28th March 2009
7th April 2010
9th October 2010
24th February 2012
22nd March 2013
26th August 2013
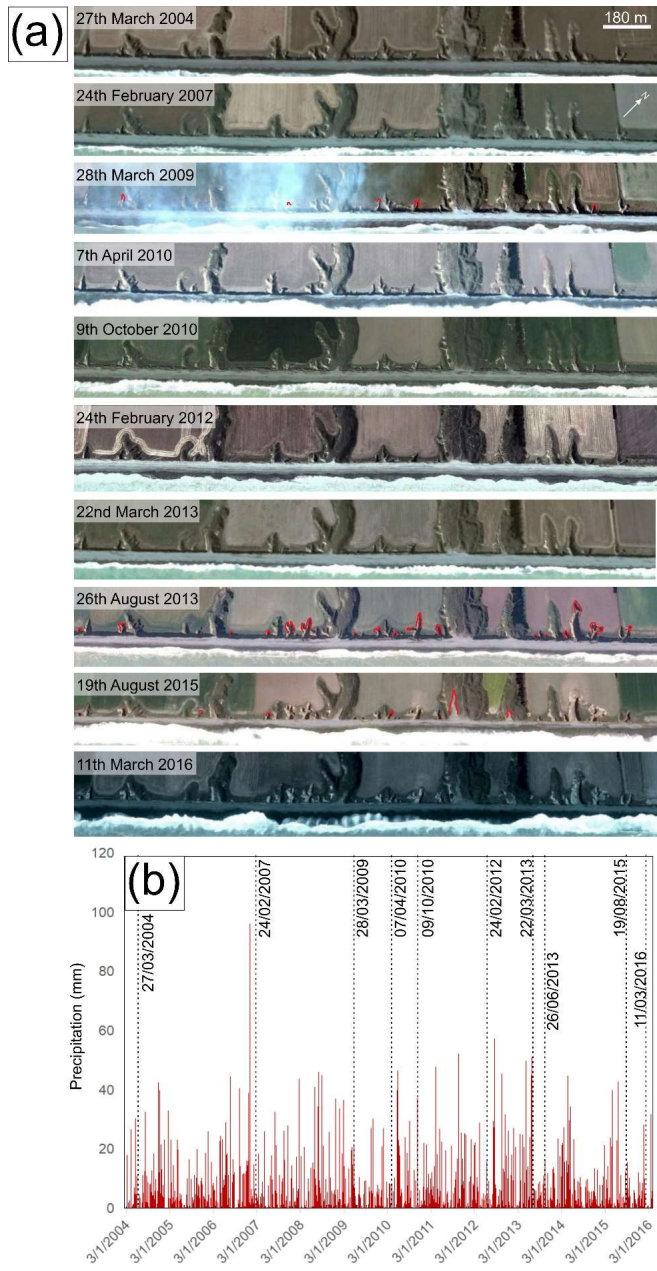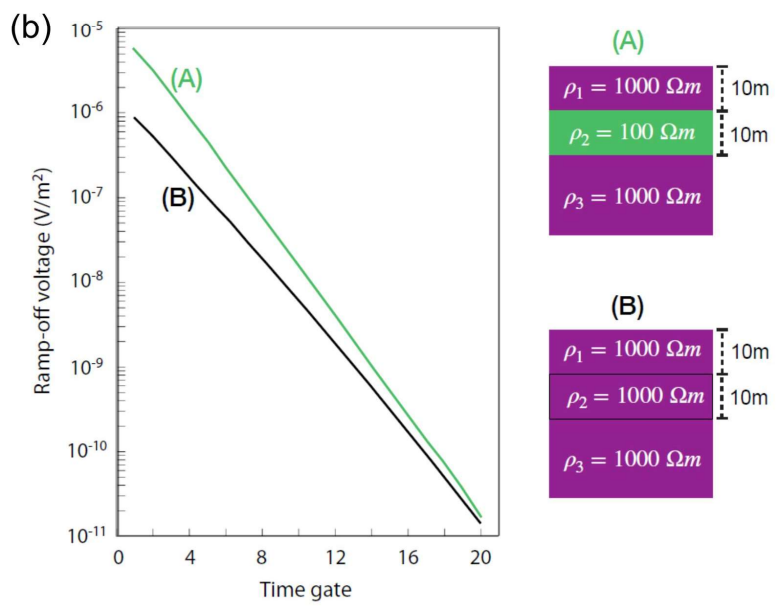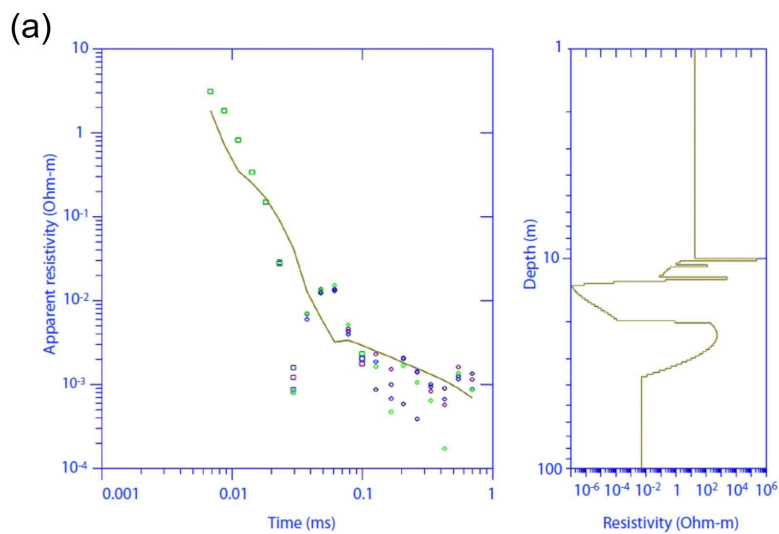19th August 2015
11th March 2016

(b)

685

Figure 6: (a) Satellite imagery of the study area between the 27th March 2004 and 11th March 2016 (source: Google, Maxar Technologies). Eroded areas are marked by red lines. (b) Daily precipitation record for this period for Ashburton Council (source: Environment Canterbury). The dates on which the satellite imagery was collected are denoted.

4.5 Geophysical data

The location of the G-TEM transects is shown in Fig. 1b. An attempt was made to invert the G-TEM slingram-mode responses with 30-m TX-RX offset using 1-D Occam inversion. A representative inversion result is shown in Fig. 7. ~~A representative inversion result is shown in Fig. 7a.~~ The resistivity model is presented in the right panel, whereas the corresponding model-response with the actual data points is shown on the left. The best calculated smooth depth profile clearly does not fit well with the measured signal and there is excessive structure in the ~10-20 m depth range, including the very low resistivity layer (~10^{-4} Ωm) at depths in excess of ~12-15 m. The resistivity values between 40 and 100 m depth are lower than sea water resistivity (0.3 Ωm), which is not reasonable. The inability to fit a 1-D model to the slingram responses suggests that the geoelectrical sub-surface structure is strongly heterogeneous within the footprint of the G-TEM transmitter. As a result, we cannot trust 1-D inversions of the slingram-mode data in such a 3-D geological environment. We did not try to use the 1-D inversion software to further analyse and interpret the G-TEM data. However, even though the individual slingram-mode responses cannot be fit reliably by a 1-D model, we can still analyse lateral changes in the observed response curves along the slingram profiles to reveal information about subsurface heterogeneity; this is elaborated below.

32

(a)

(b)

(A)

$\rho_1 = 1000\ \Omega m$ 10m
$\rho_2 = 100\ \Omega m$ 10m
$\rho_3 = 1000\ \Omega m$

(B)

$\rho_1 = 1000\ \Omega m$ 10m
$\rho_2 = 1000\ \Omega m$ 10m
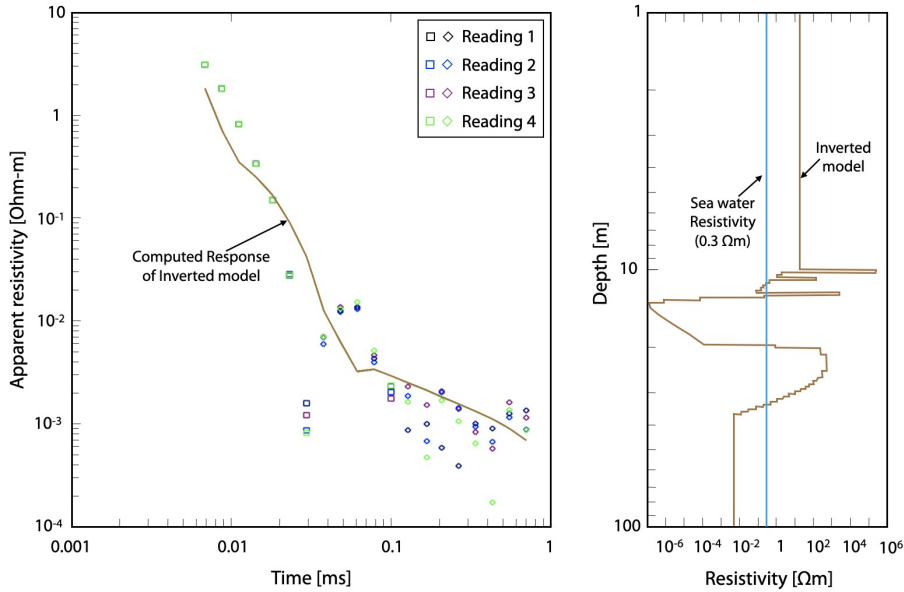$\rho_3 = 1000\ \Omega m$

710

33

Figure 7: 1-D inversion result for G-TEM data shown as square and diamond symbols (representing positive and negative responses, respectively) at a station located 6 m from start of Profile May15-1. (left) The computed resistivity depth profile displayed as a curve passing through data points; (right) the best-fitted model is marked as the brown line while the light blue is the inferred seawater resistivity.

~~Figure 7: (a) 1-D inversion result for data at a station located 6 m from start of Profile May15-1 (location in Fig. 1b). (b) G-TEM slingram responses for model (A) containing a conductive zone at a depth of 10-20 m, and for model (B) without the conductive zone.~~

Instead of performing 1-D inversions, we present time-gate plots for all three transects. A time-gate plot is defined as a graph of the observed G-TEM voltage response, evaluated at a particular time-gate, as a function of position along a profile. Time-gate plots are a useful alternative to explore the lateral variability of the G-TEM response along a profile in the event that the sounding curves at individual stations cannot be fit with 1-D models. It is presumed that variability in a time-gate plot is correlated with lateral heterogeneity in the subsurface geoelectrical structure, since a 1-D Earth structure would yield no spatial variability in a time-gate plot. In general, due to lengthy signal-averaging times, ambient electromagnetic noise from the environment adds very small contribution to TDEM responses such that any along-profile variations are likely caused by geological heterogeneity. However, there is not a straightforward relationship between the magnitude of the TDEM voltage at any given time-gate and the resistivity within a particular subsurface volume. The situation becomes more complicated since the true Earth is characterised by multiscale heterogeneity, such that spatial variations in the geology at all length scales superimpose their individual responses on one another to produce the final overall TDEM response that is measured. Thus, any analysis of the spatial variability of a time-gate plot, while informative, is largely qualitative and indicates only a first-order spatial distribution of causative subsurface

34

structures.

735

Specifically, the amplitude of the G-TEM slingram response (in units of 10^{-10} V/m^2) at the first time-gate is plotted as a function of station number along a profile. Figure 8a displays a 1-D model (I) that contains a conductive layer of 200 Ωm between 10-20 m depths in a homogeneous 1000 Ωm background. The 1-D model (I) is motivated by the inversion results of deep-penetrating 40 × 40 m TX loop TDEM soundings carried out on

740 top of the cliffs several tens of metres inland ~~Figure 7b displays a 1-D model (A) that contains a conductive layer of 100 Ωm between 10-20 m depths in a homogeneous 1000 Ωm background. The 1-D model (A) in Fig. 7b is motivated by the inversion results of deep-penetrating 40 × 40 m TX loop TDEM soundings carried out on top of the cliffs several tens of metres inland~~ (Weymer et al., in review), which revealed such a conductive zone at these depths. Unlike the slingram profiles, the deeper-penetrating, larger-loop sounding curves are readily fit by

745 a 1-D model. This model generates a G-TEM slingram response that has a substantially larger ramp-off voltage amplitude at all time gates than does the model (~~B~~II) without the conductive layer, as shown in Fig. ~~7b~~8a. Thus we regard an enhancement of response at the first time gate as indicative of a conductive zone at depth beneath the slingram station. The spatial analysis of time-gate plots is not a conventional approach in time-domain electromagnetics, but it is somewhat analogous to the spatial analysis of apparent resistivity profiles in

750 frequency-domain electromagnetics using terrain conductivity meters (e.g. Weymer et al., 2016). This is based on the idea that the G-TEM response at a fixed time-gate carries information similar to that of a terrain conductivity meter response at a fixed frequency.
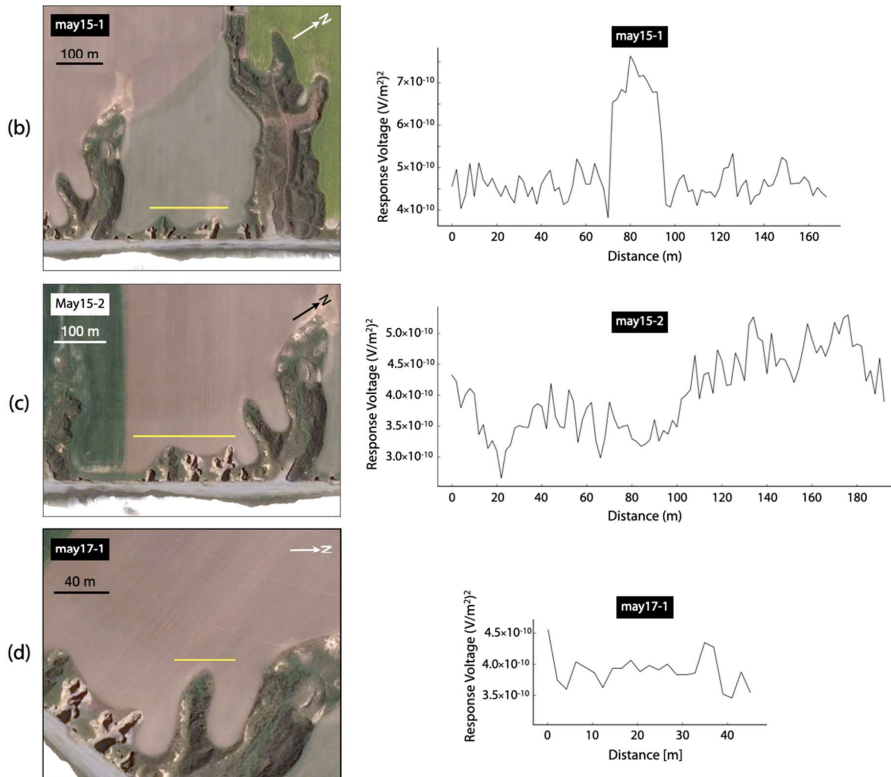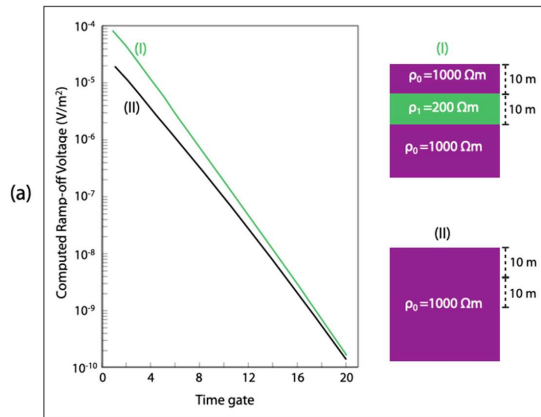
35

Figure 8: (a) G-TEM slingram response for electrical model (I) containing a conductive zone at a depth of 10-20 m, and for model (II) without the conductive zone. First-time-gate profiles of G-TEM slingram transects of (b) May15-1, (c) May 15-2, and (d) May17-2. The yellow line marks a slingram transect, the length of which can be determined from the scale bar. Source of background imagery: Google, Maxar Technologies.

760

The first-time-gate profile of transect May15-1 is located upslope of small but recently eroded gullies (Fig. ~~8a~~8b). In this figure, the 'first-time-gate profile' is a plot as a function of distance along the transect of the G-TEM ramp-off voltage at time gate number 1 ~~(as shown, for example, in Fig. 7b)~~, at the first sampled point of the transient response immediately after the TX current has been switched off. Near the middle of this transect there is a

765 distinctive peak that is much higher than the background. The peak is ~20-30 m wide and it appears in a similar fashion on each of the gates 1 through 7 (not shown here), although it cannot be clearly observed after gate 7. Transect May 15-2 is located upslope of recently eroded gullies in the south-west and relatively less active gullies in the north-east of the investigated area (Fig. ~~8b~~8c). Lateral variations are evident along the 192 m length of the profile. The high amplitude response at the start of the profile (going from the south-west to north-east) is

770 followed by a drop in amplitude near the midpoint of the profile, following which there is continuous fluctuation at a lower amplitude until the end of the profile. The time-gate plots for gates 2 to 7 remain similar in shape to that of the time-gate-1 plot and hence are not shown. After time-gate 7, the time-gate plots start to lose coherence due to the low signal-to-noise ratio of the decaying RX voltage at late times after TX ramp-off. G-TEM slingram profile May17-2 was acquired upslope of the tributary of a large gully covered by mature vegetation (Fig. ~~8c~~8d).

775 As shown in Sect. 4.4, the size and location of this gully have been persistent over recent years, in contrast to the neighbouring, smaller gullies that are under active development. Transect May 17-2 shows a lower amplitude response in comparison to the previous two transects (Fig. ~~8c~~8).
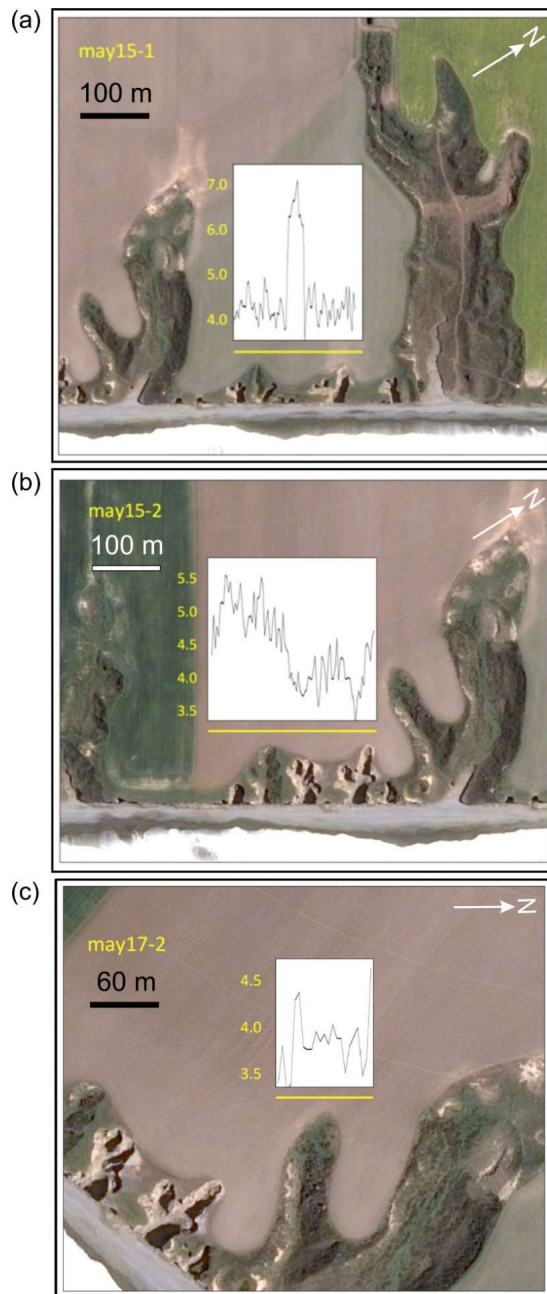
780

Figure 8: First-time-gate profiles of G-TEM slingram transects (a) May15-1, (b) May 15-2, and (c) May17-2 (units in yellow are 10^{-10} V m^{-2}). Source of background imagery: Google, Maxar Technologies. A yellow line marks a slingram transect, the length of which can be determined from the scale bar.

785

Based on all three profiles, a general observation that can be made is that the first-time-gate amplitude of the slingram response is higher upslope of the more recently active gullies.

790   **4.6 Slope stability modelling**

4.6.1   Slope with sand lens

The factory of safety of the slope prior to any rainfall event was 2.514. During the first scenario ((I-D)₃), the factor
795   of safety decreased to 1.371 due to undermining by tunnelling associated to high pore pressures within the sand
lens, and then to 0.614 as a result of a decrease in the shear strength of the lower slope material due to an increase
in pore pressure (Figs. 9a, 10a-b). A rainfall intensity of 40 mm per day is required to bring the factor of safety
below 1 (Fig. 10c9e), and .up to 4.4 m³ of water are estimated to have seeped out of the cliff face to erode 1650
m³ of material. In the case of the second scenario ((I-D)₁₄), changes in pore-water pressure did not result in either
800   tunnelling or slope failure. This only resulted in a decrease in the effective stress and in the factor of safety (1.216)
(Figs. 9b,9c-d 10b).

(a)

(b)
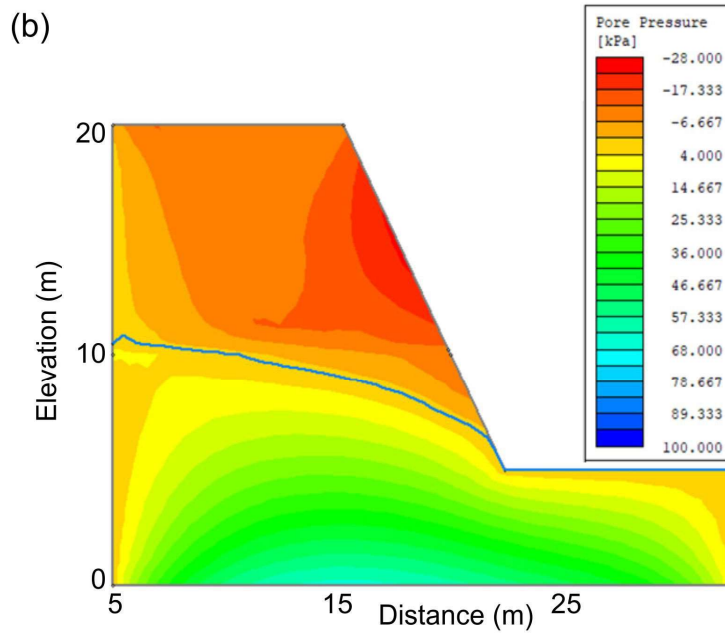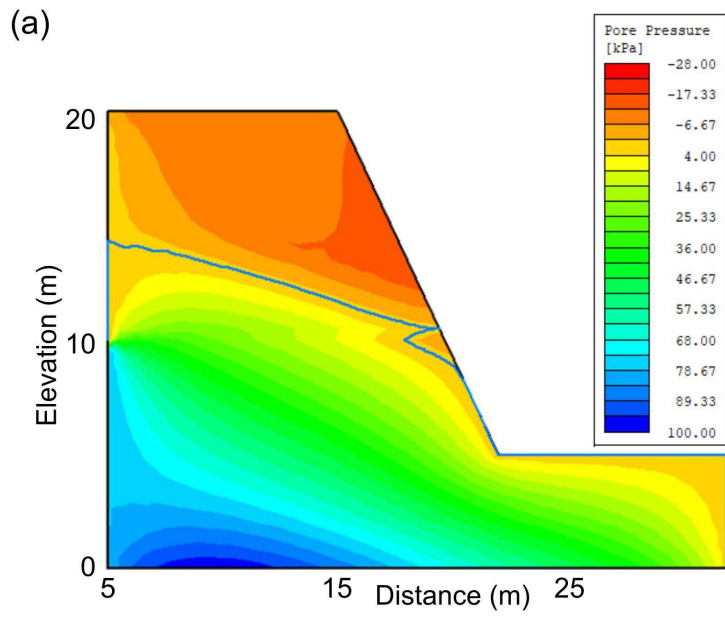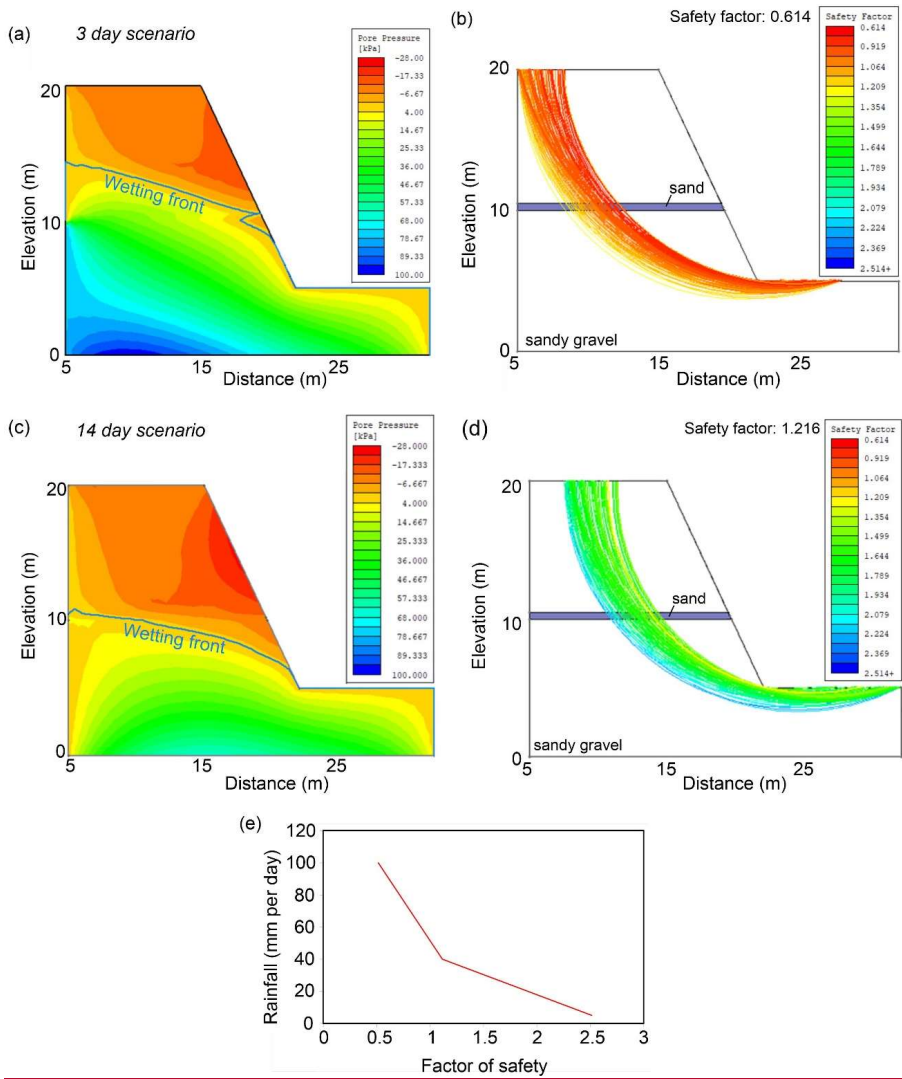
Figure 9: Model results for sandy gravel slope with sand lens. Estimated pore water pressure and factor of safety after (a) 3 days for first scenario ((I-D)$_3$) (a-b) and (b) 14 days for second scenario ((I-D)$_{14}$) (c-d). (e) Plot of rainfall intensity vs. factor of safety for the for first scenario ((I-D)$_3$ for the slope with sand lens. The results shown are for the end of the simulation for each scenario. Blue line denotes wetting front.
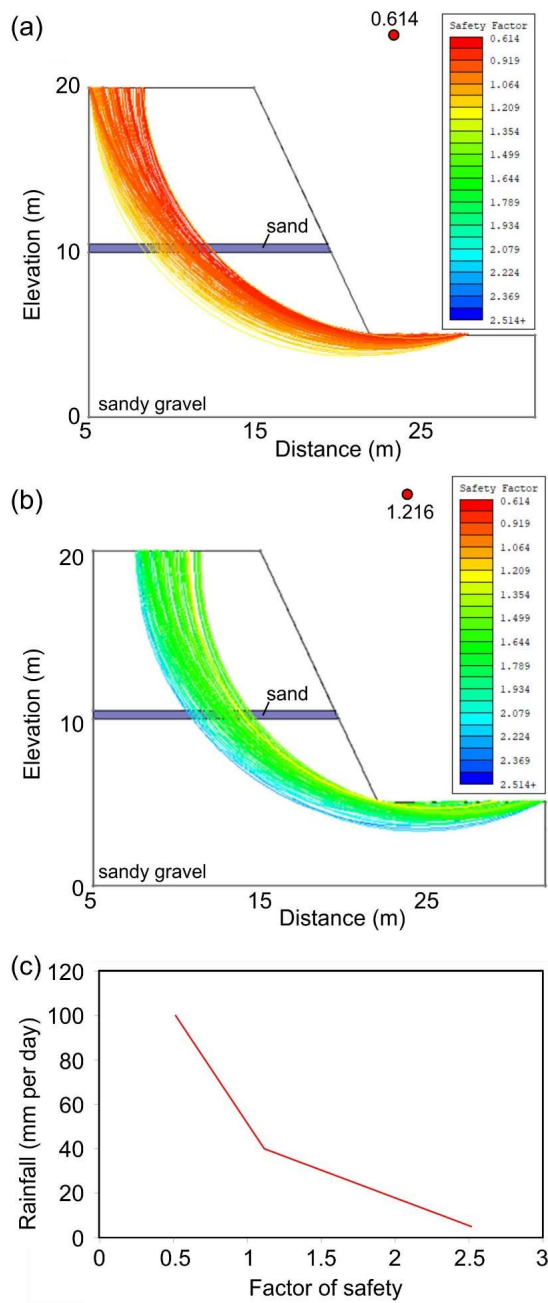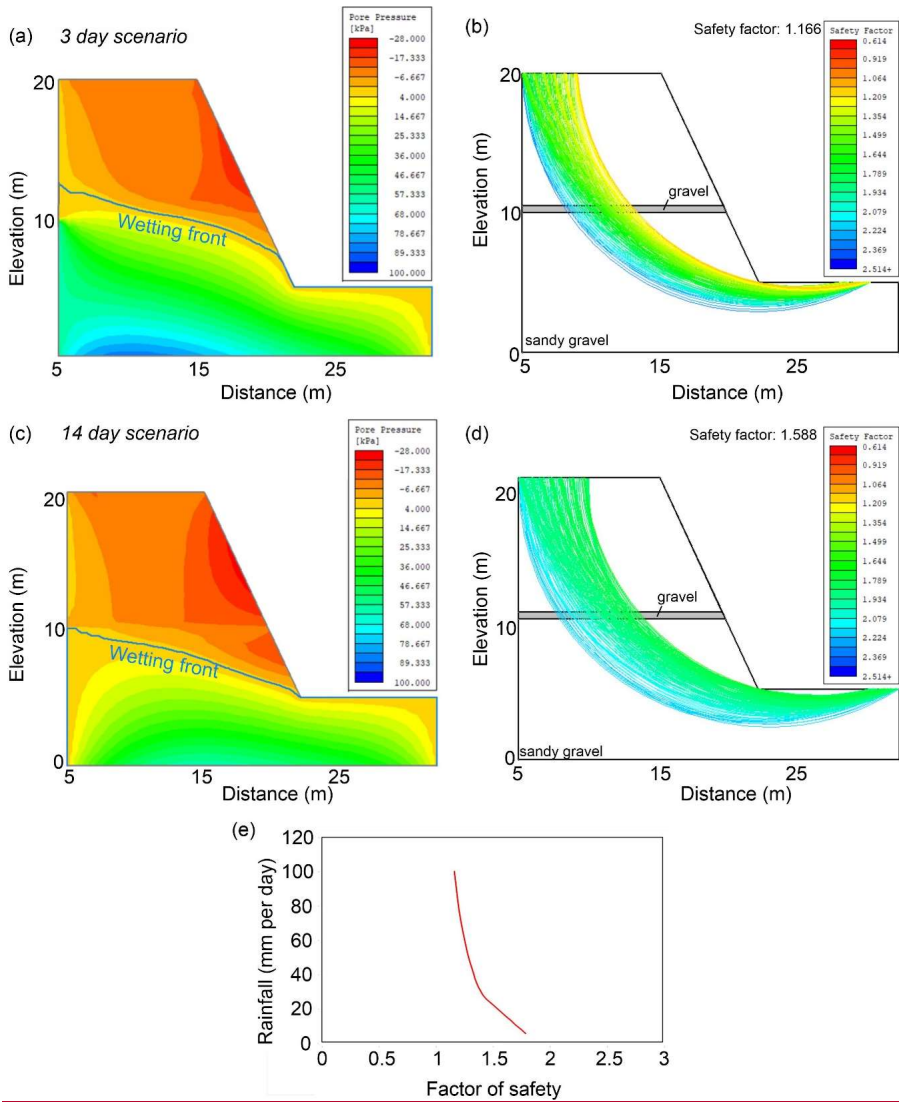
41

810

Figure 10: Model results for sandy gravel slope with sand lens. (a) Estimated factor of safety after 3 days for first scenario ((I-D)$_3$). (b) Estimated factor of safety after 14 days for second scenario ((I-D)$_{14}$). (c) Plot of rainfall intensity vs. factor of safety for the for first scenario ((I-D)$_3$ for the slope with sand lens.

4.6.2 Slope with gravel lens

815

The factor of safety of the slope prior to any rainfall event is 1.793. For the first scenario ((I-D)$_3$), the factor of safety decreased to 1.166, and neither tunnelling nor slope failure occurred (Figs. ~~11a~~10a-b). In the case of the second scenario ((I-D)$_{14}$), the outcome is the same, with the factor of safety decreasing to just 1.588 (Figs. ~~11c~~10c-d). The factor of safety does not reach a value lower than 1 for rainfall intensities of up to 120 mm per day (Fig.

820   10e).

(a) *3 day scenario*

(b) Safety factor: 1.166

(c) *14 day scenario*

(d) Safety factor: 1.588

(e)

5   Discussion

Gullies are characteristic landforms along the Canterbury coast (Fig. 1a). They are an important driver of coastal geomorphic change as well as loss of agricultural land. In the following sections we integrate field observations

45

with the modelling results to infer how coastal gullies are formed by groundwater erosion, the role that lithology and permeability play in gully initiation and evolution, and the temporal scale of gully formation.

5.1 Coastal gully formation by groundwater-related processes

The Canterbury gullies initiate and evolve via two types of groundwater-related processes. The first process is seepage erosion of sand, which leads to the formation of alcoves and tunnels. This inference is based on the exclusive occurrence of tunnels in sandy layers at the study site (Figs. 3c-e). Seepage erosion lowers the overall factor of safety of the slope, as demonstrated by slope stability model results for the slope with sand lens scenario, and is a precursor to the second process, which is slope failure (Fig. 3c). Site observations (Fig. 3h), the UAV data (Fig. 4) and satellite imagery (Fig. 5) show that gullies primarily evolve by retrogressive slope failure, which results in the elongation of the gullies and, to a lesser extent, in widening and branching along the gully walls. According to the slope stability model in Fig. 9a, up to 4.4 m³ of ~~seepage~~ water ~~are~~is required to ~~estimated to have seeped out of the cliff face to~~ erode 1650 m³ of ~~material~~sediments, which contrasts with the inference by Howard (1988) that 100-1000 times more water than volume of eroded sediment must be discharged in order to create a sapping valley. We infer that wave erosion is responsible for the removal of the failed material at the gully mouths and the base of the cliff. Isotropic scaling of length with width (Fig. 2c) suggests that gully planform shape is generally geometrically similar at consecutive stages of evolution.

5.2 Influence of geological/permeability heterogeneity on gully formation

Two factors control the location of gullies. The first factor is the occurrence of sand lenses across a sandy gravel cliff face. This geological framework is conducive to alcove formation, tunnelling and slope failure (Figs. 3c-e). The higher permeability of the sand and clean gravel lenses, in comparison to the surrounding sandy gravel (Table 12), facilitates faster water transfer to the cliff face; this is also corroborated by the weathering in the sandy layers and Fe and Mn deposits in the clean gravel layers (Fig. 3g). Alcoves and tunnels only form in the sand lenses, however, because the latter develop higher pore pressures, and sand is easier to entrain and remove in comparison to clean gravel in view of its lower shear strength (Table 12). Slope failure only occurs in sandy gravel slopes with sand lenses (Figs. 9-1110). The higher pore pressure developed in the sand lenses is transferred to the sandy gravel slopes, resulting in a larger decrease in the shear strength and higher water table in comparison to the sandy gravel slope with gravel lens.

The second factor is a hydraulically-conductive zone upslope of the gully. This inference is supported by the following observations: (i) Braided river channel infills, which tend to comprise highly permeable, coarse grained materials (Moreton et al., 2002), lead into the gullies' heads (Figs. 2a-b); (ii) Clustered distribution of gullies between the two braided rivers with the highest flow rates (Rakaia and Rangitata Rivers (Environment Canterbury, 2019)) (Fig. 1a); (iii) Geophysical observations (Fig. 8). With regards to the G-TEM slingram time-gate plots (Fig. 8), we interpret the higher-amplitude responses on the time-gate-1 plots that are preferentially located upslope of recently active gullies as zones of relatively high electrical conductivity in the subsurface at depths of ~10 m. These zones are suggestive of buried groundwater conduits made up of gravel and/or sandy units (e.g.

Weymer et al., in review), or tunnels formed by sub-surface groundwater flow in sand units. Further analysis of the G-TEM data, including 2-D modelling and inversion, is required to ascertain the sub-surface hydraulic geometry responsible for the along-profile amplitude variations. This is elaborated further in the Supplementary Materials. The above observations confirm the importance of spatial variations in hydrogeological properties as a factor controlling the location of a gully. This had initially been suggested by Dunne (1990) and has been documented for gullies in bedrock environments (Laity and Malin, 1985; Newell, 1970). Development of gullies downslope of permeable conduits may also explain why most of the erosion entails elongation of existing gullies, rather than formation of new ones (Figs. 4, 6). It also agrees with the results of experimental modelling by Berhanu et al. (2012), which suggest that channels grow preferentially at their tip when the groundwater flow is driven by an upstream flow. If seaward-directed groundwater conduits are responsible for the location of gullies, the G-TEM results predict that, along the Canterbury coast, we should generally observe active gully development downslope of peaks in slingram time-gate plots. If this is the case, G-TEM could be used to identify locations of incipient and even future gully development.

5.3   Temporal scale of gully formation

Morphological changes derived from time-series of UAV data (Figs. 4-5) and satellite imagery (Fig. 6), as well as the observations of suspended fences across gullies (Fig. 3b), suggest that gully formation is rapid (daily timescales) and recent (<3 years ago). It is an episodic process that occurs after a threshold is exceeded. This threshold entails a rainfall intensity of >40 mm/day, which occurs once every 227 days, on average. The threshold value is based on UAV and satellite imagery observations, which show that gullies form after rainfall events with an intensity higher than 40 mm per day (Figs. 5, 6), and the plot of factor of safety with rainfall intensity from the slope stability model for the first scenario ((I-D)$_3$ for the slope with sand lens (Fig. 9). These values are derived from the comparison of daily precipitation with the area of gullies eroded (Figs. 5, 6), and the plot of factor of safety with rainfall intensity from the slope stability model for the first scenario ((I-D)$_3$ for the slope with sand lens (Fig. 10). The erosion rate documented in our study area is up to 30 m per day (Figs. 4e-f), which is the highest rate documented for gullies formed by groundwater so far.

The majority of the gullies in our study area have shown evidence of erosion in the past 11 years (Figs. 4, 6). The OSL luminescence dating results (Table 23), however, suggest that the two largest gullies have largely been inactive during at least the last 2 ka; recent erosion is only documented in small gullies located in the central section of their mouths (Figs. 4, 6). This contrasts with the inference by Schumm and Phillips (1986) that they were formed by spillage of water from swamps behind the cliffs in the 19th century. We therefore propose that the short gullies (<200 m in length) are recently active features, whereas the largest gullies are relict features that formed as a result of higher groundwater flow, and possibly surface erosion, in the past. The age of sample NZ13A suggests that this may have occurred during the Last Glacial Maximum. Such difference in age, and possibly formation process, between gullies of different length may explain the different cross-sectional shape and higher scatter in the plot of length vs. width for the longer gullies (Fig. 2c).

6   Conclusions

Gully erosion is a prevalent process shaping the Canterbury coast of the South Island of New Zealand. In this study we have integrated field observations, ~~OSL~~ luminescence dating, multi-temporal UAV and satellite data, time-domain electromagnetic surveying, and slope stability modelling to constrain the controlling factors and temporal scales of gully formation. Our results indicate that gully development in sandy gravel cliffs is a groundwater-related, episodic process that occurs when rain falls at intensities of >40 mm per day. At the study area, such rainfall events occur at a mean frequency of once every 227 days. Gullies have been developing, primarily by elongation, in the last 11 years, with the latest episode dating to 3 years ago. Gullies form within days and erosion rates can reach values of up to 30 m per day. Gullies longer than 200 m, on the other hand, appear to be relict features that formed by higher groundwater flow and surface erosion >2 ka ago. The key processes responsible for gully development are the formation of alcoves and tunnels in sandy lenses by groundwater seepage erosion, followed by retrogressive slope failure. The latter is a result of undermining and a decrease in shear strength due to excess pore pressure development in the lower part of the slope. The location of the gullies is controlled by the occurrence of hydraulically-conductive zones, which comprise relict braided river channels and possibly tunnels, and sand lenses exposed across the sandy gravel cliff. We also show that gully planform shape is generally geometrically similar at consecutive stages of evolution. The outcomes of our study can improve reconstruction and prediction of an overlooked geohazard along the Canterbury coastline.

7   Code and data availability

We used Drone Deploy (https://www.dronedeploy.com/), IXG-TEM (http://www.interpex.com/) and Slide2 (https://www.rocscience.com/software/slide2) in this paper. All data from this study appear in the tables, figures, main text and supplementary materials.

8   Author contribution

A.M. designed the study and drafted the manuscript, which was revised by all co-authors. A.M., R.M, P.P., M.E. B.A.W. and P.W. participated in the fieldwork. R.M. and R.P.T. interpreted the UAV data and satellite imagery. N.S., and D.C. carried out the slope stability modelling. P.P. and M.E. processed the geophysical data. A.A. and A.T.G. were in charge of the ~~optically stimulated luminescence dating~~luminescence dating.

9   Competing interests

The authors declare that they have no conflict of interest.

10   Acknowledgments

References

Abotalib, A. Z., Sultan, M., and Elkadiri, R.: Groundwater processes in Saharan Africa: Implications for landscape
    evolution in arid environments, Earth-Science Reviews, 156, 108-136, 2016.

Abrams, D. M., Lobkovsky, A. E., Petroff, A. P., Straub, K. M., McElroy, B., Mohrig, D., Kudrolli, A., and
    Rothman, D. H.: Growth laws for channel networks incised by groundwater flow, Nature Geoscience, 2, 193-
    196, 2009.

Aqualinc Research Limited: Canterbury groundwater model 2. Christchurch (NZ), Aqualinc Research Limited,
    2007.

Bal, A. A.: Valley fills and coastal cliff s buried beneath an alluvial plain: Evidence from variation of
    permeabilities in gravel aquifers, Canterbury Plains, New Zealand, Journal of Hydrology (New Zealand), 35, 1-
    27, 1996.

Berger, G. W., Tonkin, P. J., and Pillans, B.: Thermo-luminescence ages of post-glacial loess, Rakaia River, South
    Island, New Zealand, Quaternary International, 35/36, 177-182, 1996.

Berhanu, M., Petroff, A. P., Devauchelle, O., Kudrolli, A., and Rothman, D. H.: Shape and dynamics of seepage
    erosion in a horiztonal granular bed, Physical Review E, 86, 041304, 2012.

Browne, G. H., and Naish, T. R.: Facies development and sequence architecture of a late Quaternary fluvial-
    marine transition, Canterbury Plains and shelf, New Zealand: implications for forced regressive deposits,
    Sedimentary Geology, 158, 57-86, 2003.

Buylaert, J.-P., Murray, A. S., and Thomsen, K. J.: Testing the potential of an elevated temperature IRSL signal
    from K-feldspar, Radio Measurements, 44, 560-565, 2009.

Buylaert, J. P., Thiel, C., Murray, A. S., D., V., Yi, S., and Lu, H.: IRSL and post-IR IRSL residual doses recorded
    in modern dust samples from the Chinese Loess Plateau, Geochronometria, 38, 432-440, 2011.

Chu-Agor, M. L., Fox, G. A., Cancienne, R. M., and Wilson, G. V.: Seepage caused tension failures and erosion
    undercutting of hillslopes, Journal of Hydrology, 359, 247-259, 2008.

Coelho Netto, A. L., Fernandes, N. F., and Edegard de Deus, C.: Gullying in the southeastern Brazilian Plateau,
    Bananal, SP, Porto Alegre Symposium, Porto Alegre, 1988, 35-42,

Collins, B. D., and Sitar, N.: Geotechnical properties of weakly and moderately cemented sands in steep slopes,
    Journal of Geotechnical and Geoenvironmental Engineering, 135, 1359-1366, 2009.

Collins, B. D., and Sitar, N.: Stability of steep slopes in cemented sands, Journal of Geotechnical and
    Geoenvironmental Engineering, 137, 43-51, 2011.

Constable, S. C., Parker, R. L., and Constable, C. G.: Occam's inversion: Apractical algorithm for generating
    smooth models from EM sounding data, Geophysics, 52, 289-300, 1987.

49

Dann, R., Close, M., Flinto, M., Hector, R., Barlow, H., Thomas, S., and Francis, G.: Characterization and estimation of hydraulic properties in an alluvial gravel vadose zone, Vadose Zone Journal, 8, 651-663, 2009.

Davey, G.: Definition of the Canterbury Plains Aquifers, Environmental Canterbury, 2006.

Devauchelle, O., Petroff, A. P., Seybold, H. F., and Rothman, D. H.: Ramification of stream networks,
1005   Proceedings of the National Academy of Sciences of the United States of America, 109, 20832-20836, 2012.

Domenico, P. A., and Schwartz, F. W.: Physical and Chemical Hydrogeology, John Wiley, Chichester, 528 pp., 1997.

Dunne, T.: Hydrology, mechanics, and geomorphic implications of erosion by subsurface flow, in: Groundwater Geomorphology: The Role of Subsurface Water in Earth-Surface Processes and Landforms, edited by: Higgins,
1010   C. G., and Coates, D. R., Special Paper Geological Society of America, 1-25, 1990.

Environment Canterbury: River flow data, www.ecan.govt.nz/data/riverflow, 2019.

Fitterman, D. V.: Tools and techniques: Active-source electromagnetic methods, in: Resources in the Near-Surface Earth, Treatise on Geophysics, edited by: Slater, L., Elsevier, 295-333, 2015.

Fox, G. A., Wilson, G. V., Periketi, R. K., and Cullum, R. F.: Sediment transport model for seepage erosion of
1015   streambank erosion, Journal of Hydrologic Engineering, 11, 603-611, 2006.

Fredlund, D. G., and Krahn, J.: Comparison of slope stability methods of analysis, Canadian Geotechnical Journal, 14, 429-439.

Fredlund, D. G., Krahn, J., and Pufahl, D.: The relationship between limit equilibrium slope stability methods, 10th International Conference on Soil Mechanics and Foundation Engineering, Stockholm, Sweden, 1981,
1020 Geonics: G-TEM Operating Manual, Geonics Ltd., Mississauga, Canada, 2016.

Gibb, J. G.: Rates of coastal erosion and accretion in New Zealand, New Zealand Journal of Marine and Freshwater Research, 12, 429-456, 1978.

Harrison, K. P., and Grimm, R. E.: Groundwater-controlled valley networks and the decline of surface runoff on early Mars, Journal of Geophysical Research, 110, E12S16, 2005.
1025 Higgins, C. G.: Drainage systems developed by sapping on Earth and Mars, Geology, 10, 147-152, 1982.

Howard, A. D.: Groundwater sapping on Earth and Mars, in: Sapping Features of the Colorado Plateau, edited by: Howard, A. D., Kochel, R. C., and Holt, H. R., NASA, 1-4, 1988.

Howard, A. D., and McLane, C. F.: Erosion of cohesionless sediment by groundwater seepage, Water Resources Research, 24, 1659-1674, 1988.
1030 Howard, A. D.: Case study: Model studies of ground-water sapping, in: Geological Society of America Special Paper, edited by: Higgins, C. G., and Coates, D. R., 257-264, 1990.

Howard, A. D.: Simulation modeling and statistical classification of escarpment planforms, Geomorphology, 12, 187-214, 1995.

Interpex: IXG-TEM Instruction Manual, Interpex Ltd., Golden, USA, 2012.
1035 Kirk, R. M.: River-beach interaction on mixed sand and gravel coasts: A geomorphic model for water resource planning, Applied Geography, 11, 267-287, 1991.

Kline, S. W., Adams, P. N., and Limber, P. W.: The unsteady nature of sea cliff retreat due to mechanical abrasion, failure and comminution feedbacks, Geomorphology, 219, 53-67, 2014.

Kochel, R. C., Howard, A. D., and McLane, C. F.: Channel networks developed by groundwater sapping in fine-grained sediments: Analogs to some Martian valleys, in: Models in Geomorphology, edited by: Woldenberg, M., Allen and Unwin, St Leonards, Australia, 313-341, 1985.

Kochel, R. C., and Piper, J. F.: Morphology of large valleys on Hawaii - Evidence for groundwater sapping and comparisons with Martian valleys, Journal of Geophysical Research, 91, E175-E192, 1986.

Laity, J. E., and Malin, M. C.: Sapping processes and the development of theater-headed valley networks in the Colorado Plateau, Geological Society of America Bulletin, 96, 203-217, 1985.

Lamb, M. P., Howard, A. D., Johnson, J., Whipple, K. X., Dietrich, W. E., and Perron, J. T.: Can springs cut canyons into rock?, Journal of Geophysical Research, 111, E07002, 2006.

Laporte-Fauret, Q., Marieu, V., Castelle, B., Michalet, R., Bujan, S., and Rosebery, D.: Low-Cost UAV for High-Resolution and Large-Scale Coastal Dune Change Monitoring Using Photogrammetry, Journal of Marine Science and Engineering, 7, 63, 2019.

Lapotre, M. G. A., and Lamb, M. P.: Substrate control on valley formation by groundwater on Earth and Mars, Geology, 46, 531-534, 2018.

Leckie, D. A.: Modern environments of the Canterbury Plains and adjacent offshore areas, New Zealand — an analog for ancient conglomeratic depositional systems in nonmarine and coastal zone settings, Bullettin of Canadian Petroleum Geology, 51, 389-425, 2003.

Leyland, J., and Darby, S. E.: An empirical–conceptual gully evolution model for channelled sea cliffs, Geomorphology, 102, 419-434, 2008.

Leyland, J., and Darby, S. E.: Effects of Holocene climate and sea-level changes on coastal gully evolution: insights from numerical modelling, Earth Surface Processes and Landforms, 34, 1878-1893, 2009.

Limber, P. W., and Barnard, P. L.: Coastal knickpoints and the competition between fluvial and wave-driven erosion on rocky coastlines, Geomorphology, 306, 1-12, 2018.

Lobkovsky, A. E., Jensen, B., Kudrolli, A., and Rothman, D. H.: Threshold phenomena in erosion driven by subsurface flow, Journal of Geophysical Research, 109, F04010, 2004.

Mackey, B. H., Scheingross, J. S., Lamb, M. P., and Farley, K. A.: Knickpoint formation, rapid propagation, and landscape response following coastal cliff retreat at the last interglacial sea-level highstand: Kaua'i, Hawai'i, Geological Society of America Bulletin, 126, 925-942, 2014.

Malin, M. C., and Carr, M. H.: Groundwater formation of Martian valleys, Nature, 397, 589-591, 1999.

Micallef, A., Person, M., Haroon, A., Weymer, B. A., Jegen, M., Schwalenberg, K., Faghih, Z., Duan, S., Cohen, D., Mountjoy, J. J., Woelz, S., Gable, C. W., Averes, T., and Tiwari, A. K.: 3D characterisation and quantification of an offshore freshened groundwater system in the Canterbury Bight, Nature Communications, 11, 1372, 2020.

Moreton, D. J., Ashworth, P. J., and Best, J. L.: The physical scale modelling of braided alluvial architecture and estimation of subsurface permeability, Basin Research, 14, 265-285, 2002.

Nabighian, M. N., and Macnae, J. C.: 6. Time Domain Electromagnetic Prospecting Methods, in: Electromagnetic Methods in Applied Geophysics: Volume 2, Application, Parts A and B, 427-520, 1991.

Nash, D. J., Shaw, P. A., and Thomas, D. S. G.: Duricrust development and valley evolution: Process-landforms links in the Kalahari, Earth Surface Processes and Landforms, 19, 299-317, 1994.

51

Nash, D. J.: Groundwater sapping and valley development in the Hackness Hills, North Yorkshire, England, Earth Surface Processes and Landforms, 21, 781-795, 1996.

1080 Newell, M.: Canyonlands - modern history, Naturalist, 21, 40-47, 1970.

Onda, Y.: Seepage erosion and its implications to the formation of amphitheatre valley heads: A case study at Obara, Japan, Earth Surface Processes and Landforms, 19, 624-640, 1994.

Pelletier, J. D., and Baker, V. R.: The role of weathering in the formation of bedrock valleys on Earth and Mars: A numerical modeling investigation, Journal of Geophysical Research, 116, E11007, 2011.

1085 Petroff, A. P., Devauchelle, O., Abrams, D. M., Lobkovsky, A. E., Kudrolli, A., and Rothman, D. H.: Geometry of valley growth, Journal of Fluid Mechanics, 673, 245-254, 2011.

Pillans, B.: Drainage initiation by subsurface flow in South Taranaki, New Zealand, Geology, 13, 262-265, 1985.

Pondthai, P., Everett, M. E., Micallef, A., Weymer, B. A., Faghih, Z., Haroon, A., and Jegen, M.: 3D characterization of a coastal freshwater aquifer in SE Malta (Mediterranean Sea) by time-domain
1090 electromagnetics, Water, 12, 1566, 2020.

Preusser, F., Chithambo, M. L., Götte, T., Martini, M., Ramseyer, K., Sendezera, E. J., Susino, G. J., and Wintle, A. G.: Quartz as a natural luminescence dosimeter, Earth Science Reviews, 97, 184-214, 2009.

Salese, F., Pondrelli, M., Neeseman, A., Schmidt, G., and Ori, G. G.: Geological evidence of planet-wide groundwater system on Mars, Journal of Geophysical Research, 124, 374-395, 2019.

1095 Schorghofer, N., Jensen, B., Kudrolli, A., and Rothman, D. H.: Spontaneous channelization in permeable ground: Theory, experiment, and observation, Journal of Fluid Mechanics, 503, 357-374, 2004.

Schumm, S. A., and Phillips, L.: Composite channels of the Canterbury Plain, New Zealand: A Martian analog?, Geology, 14, 326-329, 1986.

Schumm, S. A., Boyd, K. F., Wolff, C. G., and Spitz, W. J.: A groundwater sapping landscape in the Florida
1100 panhandle, Geomorphology, 12, 281-297, 1995.

Scott, G. L.: Near-surface hydraulic stratigraphy of the Canterbury Plains between Ashburton and Rakaia rivers, New Zealand, Journal of Hydrology (New Zealand), 19, 68-74, 1980.

Skempton. A.W.: The pore-pressure coefficients A and B, Géotechnique 4(4), 143-147. 1954.

Sunderlin, D., Trop, J. M., Idleman, D., Brannick, A., White, J. G., and Grande, L.: Paleoenvironment and
1105 paleoecology of a Late Paleocene high-latitude terrestrial succession, Arkose Ridge Formation at Box Canyon, southern Talkeetna Mountains, Alaska, Palaeogeography, Palaeoclimatology, Palaeoecology, 401, 57-80, 2014.

Thiel, C., Buylaert, J.-P., Murray, A., Terhorst, B., Hofer, I., Tsukamoto, S., and Frechen, M.: Luminescence dating of the Stratzig loess profile (Austria) – Testing the potential of an elevated temperature post-IR IRSL protocol, Quaternary International, 234, 23-31, 2011.

1110 Uchupi, E., and Oldale, R. N.: Spring sapping origin of the enigmatic relict valleys of Cape Cod and Martha's Vineyard and Nantucket Islands, Massachussets, Geomorphology, 9, 83-95, 1994.

Weymer, B. A., Everett, M. E., Houser, C., Wernette, P., and Barrineau, P.: Differentiating tidal and seasonal effects on barrier island hydrogeology: Testing the utility of portable multi-frequency EMI profilers, Geophysics, 81, E347-361, 2016.

1115 Weymer, B. A., Wernette, P., Everett, M. E., Pondthai, P., Jegen, M., and Micallef, A.: Multilayered high-permeability conduits connecting onshore and offshore coastal groundwater aquifers, Frontiers in Marine Science – Coastal Ocean Processes, in review.

Whitaker, S.: Flow in Porous-Media I: a theoretical derivation of Darcy's-Law, Transport in Porous Media, 1, 3-25, 1986.

1120 Wilson, G. V., Periketi, R., Fox, G. A., Dabney, S., Shields, D., and Cullum, R. F.: Seepage erosion properties contributing to streambank failure, Earth Surface Processes and Landforms, 32, 447-459, 2007.

Ye, F.-Y., Barriot, J.-P., and Carretier, S.: Initiation and recession of the fluvial knickpoints of the Island of Tahiti (French Polynesia), Geomorphology, 186, 162-173, 2013.

Yi, R., Cohen, Y., Devauchelle, O., Gibbins, G., Seybold, H. F., and Rothman, D. H.: Symmetric rearrangement

1125 of groundwater-fed streams, Proceedings of the Royal Society of London, Series A, 473, 20170539., 2017.

Page 18: [1] Change	Unknown	

Field Code Changed

Page 18: [2] Formatted	ABC	10/25/2020 9:54:00 PM

Font: (Default) +Headings CS (Times New Roman), Complex Script Font: +Headings CS (Times New Roman)

Page 18: [3] Formatted	ABC	10/25/2020 9:54:00 PM

Font: 10 pt, Complex Script Font: 10 pt

Page 18: [4] Formatted	ABC	10/25/2020 9:56:00 PM

Space After: 0 pt, Line spacing: 1.5 lines

Page 18: [5] Formatted	ABC	10/25/2020 9:54:00 PM

Font: (Default) +Headings CS (Times New Roman), 10 pt, Complex Script Font: +Headings CS (Times New Roman), 10 pt

Page 18: [6] Formatted	ABC	10/25/2020 9:54:00 PM

Font: 10 pt, Complex Script Font: 10 pt

Page 18: [7] Formatted	ABC	10/25/2020 9:54:00 PM

Font: (Default) +Headings CS (Times New Roman), 10 pt, Complex Script Font: +Headings CS (Times New Roman), 10 pt

Page 18: [8] Formatted	ABC	10/25/2020 9:54:00 PM

Font: 10 pt, Complex Script Font: 10 pt

Page 18: [9] Formatted	ABC	10/25/2020 9:54:00 PM

Font: (Default) +Headings CS (Times New Roman), 10 pt, Complex Script Font: +Headings CS (Times New Roman), 10 pt

Page 18: [10] Formatted	ABC	10/25/2020 9:56:00 PM

Font: (Default) +Headings CS (Times New Roman), Complex Script Font: +Headings CS (Times New Roman)

Page 18: [11] Formatted	ABC	10/25/2020 9:56:00 PM

Right, Space After: 0 pt, Line spacing: 1.5 lines

Page 18: [12] Formatted	ABC	10/25/2020 9:56:00 PM

Font: (Default) +Headings CS (Times New Roman), Complex Script Font: +Headings CS (Times New Roman)

Page 18: [13] Formatted	ABC	10/25/2020 9:56:00 PM

Font: (Default) +Headings CS (Times New Roman), Complex Script Font: +Headings CS (Times New Roman)

Page 18: [14] Formatted	ABC	10/25/2020 9:56:00 PM

Font: 12 pt, Complex Script Font: 12 pt, Not Superscript/ Subscript

Page 18: [15] Formatted	ABC	10/25/2020 9:56:00 PM

Font: 12 pt, Complex Script Font: 12 pt

Page 18: [16] Formatted	ABC	10/25/2020 9:56:00 PM

Font: 10 pt, Complex Script Font: 10 pt

Page 18: [17] Formatted	ABC	10/25/2020 9:54:00 PM

Font: 10 pt, Complex Script Font: 10 pt, Not Superscript/ Subscript

Page 18: [18] Formatted	ABC	10/25/2020 9:54:00 PM

Font: (Default) +Headings CS (Times New Roman), 10 pt, Complex Script Font: +Headings CS (Times New Roman), 10 pt

Page 18: [19] Formatted	ABC	10/25/2020 9:56:00 PM

Space Before: 0 pt, After: 0 pt, Line spacing: 1.5 lines

Page 18: [20] Formatted	ABC	10/25/2020 9:54:00 PM

Font: (Default) +Headings CS (Times New Roman), 10 pt, Complex Script Font: +Headings CS (Times New Roman), 10 pt

Page 18: [21] Formatted	ABC	10/25/2020 9:59:00 PM

Space Before: 0 pt, After: 0 pt, Line spacing: 1.5 lines

Page 18: [22] Formatted	ABC	10/25/2020 9:54:00 PM

Font: 10 pt, Complex Script Font: 10 pt

Page 18: [23] Formatted	ABC	10/25/2020 9:54:00 PM

Font: (Default) +Headings CS (Times New Roman), 10 pt, Complex Script Font: +Headings CS (Times New Roman), 10 pt

Page 18: [24] Formatted	ABC	10/25/2020 9:54:00 PM

Font: (Default) +Headings CS (Times New Roman), 10 pt, Complex Script Font: +Headings CS (Times New Roman), 10 pt

Page 18: [25] Formatted	ABC	10/25/2020 9:54:00 PM

Font: (Default) +Headings CS (Times New Roman), 10 pt, Complex Script Font: +Headings CS (Times New Roman), 10 pt

Page 18: [26] Formatted	ABC	10/25/2020 9:54:00 PM

Font: 10 pt, Complex Script Font: 10 pt

Page 18: [27] Formatted	ABC	10/25/2020 9:54:00 PM

Font: 10 pt, Complex Script Font: 10 pt

Page 18: [28] Formatted	ABC	10/25/2020 9:54:00 PM

Font: (Default) +Headings CS (Times New Roman), 10 pt, Complex Script Font: +Headings CS (Times New Roman), 10 pt

Page 18: [29] Formatted	ABC	10/25/2020 9:54:00 PM

Font: (Default) +Headings CS (Times New Roman), 10 pt, Complex Script Font: +Headings CS (Times New Roman), 10 pt

Page 18: [30] Formatted	ABC	10/25/2020 9:56:00 PM

Right, Space Before: 0 pt, After: 0 pt, Line spacing: 1.5 lines

Page 18: [31] Formatted	ABC	10/25/2020 9:56:00 PM

Font: (Default) +Headings CS (Times New Roman), Complex Script Font: +Headings CS (Times New Roman)

Page 18: [32] Formatted	ABC	10/25/2020 9:56:00 PM

Font: (Default) +Headings CS (Times New Roman), Complex Script Font: +Headings CS (Times New Roman)

Page 18: [33] Formatted	ABC	10/25/2020 9:56:00 PM

Font: (Default) +Headings CS (Times New Roman), Complex Script Font: +Headings CS (Times New Roman)

Page 18: [34] Formatted	ABC	10/25/2020 9:56:00 PM

Font: 12 pt, Complex Script Font: 12 pt

Page 18: [35] Formatted	ABC	10/25/2020 9:56:00 PM

Font: 10 pt, Complex Script Font: 10 pt

Page 18: [36] Formatted	ABC	10/25/2020 9:54:00 PM

Font: (Default) +Headings CS (Times New Roman), 10 pt, Complex Script Font: +Headings CS (Times New Roman), 10 pt

Page 18: [37] Formatted	ABC	10/25/2020 9:56:00 PM

Space Before: 0 pt, After: 0 pt, Line spacing: 1.5 lines

Page 18: [38] Formatted   ABC   10/25/2020 9:54:00 PM

Font: (Default) +Headings CS (Times New Roman), 10 pt, Complex Script Font: +Headings CS (Times New Roman), 10 pt

Page 18: [39] Formatted   ABC   10/25/2020 9:56:00 PM

Right, Space Before: 0 pt, After: 0 pt, Line spacing: 1.5 lines

Page 18: [40] Formatted   ABC   10/25/2020 9:57:00 PM

Font: (Default) +Headings CS (Times New Roman), Complex Script Font: +Headings CS (Times New Roman)

Page 18: [41] Formatted   ABC   10/25/2020 9:57:00 PM

Font: (Default) +Headings CS (Times New Roman), Complex Script Font: +Headings CS (Times New Roman)

Page 18: [42] Formatted   ABC   10/25/2020 9:54:00 PM

Font: 10 pt, Complex Script Font: 10 pt

Page 18: [43] Formatted   ABC   10/25/2020 9:54:00 PM

Font: (Default) +Headings CS (Times New Roman), 10 pt, Complex Script Font: +Headings CS (Times New Roman), 10 pt

Page 18: [44] Formatted   ABC   10/25/2020 9:54:00 PM

Font: 10 pt, Complex Script Font: 10 pt

Page 18: [45] Formatted   ABC   10/25/2020 9:54:00 PM

Font: (Default) +Headings CS (Times New Roman), 10 pt, Complex Script Font: +Headings CS (Times New Roman), 10 pt