Beyond 2D landslide inventories and their rollover: synoptic 3D inventories and volume from repeat LiDAR data

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Abstract.
Efficient and robust landslide mapping and volume estimation is essential to rapidly infer landslide spatial distribution, to quantify the role of triggering events on landscape changes and to assess direct and secondary landslide-related geomorphic hazards. Many efforts have been made to develop landslide mapping methods, based on 2D satellite or aerial images, and to constrain the empirical volume-area (V-A) relationship allowing in turn to offer indirect estimates of landslide volume. Despite these efforts, major issues remain including the uncertainty of the V-A scaling, landslide amalgamation and the under-detection of landslides. To address these issues, we propose a new semi-automatic 3D point cloud differencing method to detect geomorphic changes, obtain robust landslide inventories with an uncertainty metric and directly measure the volume and geometric properties of landslides. This method is based on the M3C2 algorithm and was applied to a multi-temporal airborne LiDAR dataset of the Kaikoura region, New Zealand, following the $M_w$ 7.8 earthquake of 14 November 2016.

In a 5 km² area, our 3D workflow detects 524 landslide sources and 304 deposits with a minimum size of 20 m² and a total volume of $752,616 \pm 154,165$ m³ and $949,742 \pm 150,014$ m³, respectively. Geometric properties of the 3D inventory, including the V-A relationship, are consistent with previous results, except for the lack of the classically observed rollover of the distribution of source area. A 2D inventory hand-crafted from aerial image comparison only identified 258 landslide scars, exhibits a rollover in the distribution of source area and severely underestimates the total area and volume of 3D detected sources by 75 % and 60 %, respectively. Detection and delimitation errors in 2D occurs in areas with limited texture change (bare rock surfaces, forests) and at the transition between sources and deposits that the 3D method accurately captures. Large rotational/translational landslides are missed in the 2D inventory owing to the dominant vertical topographic change. Our data show a systematic size-dependent under-detection in the 2D inventory below 200 m² that may explain all or part of the classical rollover observed in 2D landslide source area distribution. While the 3D segmentation of complex clustered landslides sources remains challenging, we demonstrate that 3D point cloud differencing offers a greater sensitivity to detect small changes than a classical difference of DEMs (digital elevation models). Our results underline the vast potential of 3D-derived inventories in quantifying exhaustively and objectively the impact of extreme events on topographic change in regions prone to landsliding and to explore in new ways the scaling properties of landslides.
1. Introduction

In mountain areas, extreme events such as large earthquakes and typhoons can trigger important topographic changes through landsliding. Landslides are a key agent of hillslope and landscape erosion (Keefer, 1994; Malamud et al., 2004) and represent a significant hazard for local populations. Efficient and rapid mapping of landslides is required to robustly infer their spatial distribution, their total volume and the induced landscape changes. Such information are crucial to understand the role of triggering events on landscape evolution and to manage direct and secondary landslide-related hazards (Guzzetti et al., 2012; Hovius et al., 1997; Marc et al., 2016; Parker et al., 2011). Following a triggering event, total landslide volume over a regional scale is classically determined in two steps: (i) individual landslide mapping using 2D satellite or aerial images (e.g. Behling et al., 2014; Fan et al., 2019; Guzzetti et al., 2012; Li et al., 2014; Malamud et al., 2004; Martha et al., 2010; Massey et al., 2018; Parker et al., 2011) and (ii) indirect volume estimation using a volume-area relationship (e.g. Simonett, 1967; Larsen et al., 2010):

\[ V = \alpha A^\gamma \]  

(1)

with \( V \) and \( A \) the volume and area of individual landslides, \( \alpha \) a prefactor and \( \gamma \) a scaling exponent ranging between 1.1 and 1.6 (e.g. Larsen et al., 2010; Massey et al., 2020).

A first source of error comes from the uncertainty on the values of \( \alpha \) and \( \gamma \) which tend to be site specific and potentially process specific (e.g. shallow versus bedrock landsliding). This uncertainty could lead to an order magnitude of difference in total estimated volume given the non-linearity of eq. (1) (Larsen et al., 2010). Two other sources of error arise from the detectability of individual landslides themselves and the ability to accurately measure the distribution of landslide areas due to landslide amalgamation and under-detection of landslides. Landslide amalgamation can produce up to 200 % error in the total volume estimation (Li et al., 2014; Marc and Hovius, 2015) and occurs because of landslide spatial clustering or incorrect mapping due, for instance, to automatic processing. Indeed, automatic landslide mapping (Behling et al., 2014; Marc et al., 2019; Martha et al., 2010; Pradhan et al., 2016) relies on the difference in texture, color and spectral properties such as NDVI (Normalized difference vegetation index) of multispectral 2D images between pre- and post-landslide images, assuming that landslides lead to vegetation removal or significant texture change. During this process, difficulties in automatic segmentation of landslide sources can result in incorrect estimate of individual landslide area, which propagates into a much larger estimate of volume owing to the non-linearity of eq. (1). Manual mapping and automatic algorithms based on geometrical and topographical inconsistencies can reduce the amalgamation effect on landslide volume estimation (Marc and Hovius, 2015), but it remains a source of error due to the inherent spatial clustering of landslides and the overlapping of landslide deposits and sources. Under-detection of landslides can occur because the spectral signature of images is not sufficiently altered by a new failure. Notably, under-detection of small landslides is one hypothesis put forward to explain the rollover classically observed in the distribution of landslide area (e.g., Stark and Hovius, 2001), even if the emergence of a rollover is predicted by mechanical models of landslide failures at the regional scale (e.g. Jeandet et al., 2019; Tanyas et al., 2019 and references therein). Under-detection can be particularly important in areas with thin soils and sparse or missing vegetation (Behling et al., 2014). It can
be further complicated when using different image sources with different resolution, spectral resolution, projected shadows and consequent ability to detect surface change. Yet, the level of under-detection of landslide in a given inventory remains generally largely unknown. The delimitation of landslides in areas with poor or total lack of vegetation is therefore critical to robustly infer landslide area distribution and total volume. To deal with poor vegetated areas, Behling et al. (2014, 2016) developed a method using temporal NDVI-trajectories which describes the temporal footprints of vegetation changes but cannot fully address complex cases when texture is not significantly changing such as bedrock landsliding on bare rock hillslopes.

Addressing these three sources of uncertainty - volume-area scaling uncertainty, landslide amalgamation and the under-detection of landslides - requires new approaches to obtain and analyse landslide inventories. In the last decade, the increasing availability of multi-temporal high resolution 3D point cloud data and digital elevation models (DEM), based on aerial or satellite photogrammetry and Light Detection and Ranging (LiDAR), has opened the possibility to better quantify landslide volume and displacement (Bull et al., 2010; Mouyen et al., 2019; Okyay et al., 2019; Passalacqua et al., 2015; Ventura et al., 2011).

The most commonly used technique is the difference of DEM (DoD) which computes the vertical elevation differences between two DEMs of different time (Corsini et al., 2009; Giordan et al., 2013; Mora et al., 2018; Wheaton et al., 2010). Even though this method is fast and works properly on planar surface, a vertical difference can be prone to strong errors when used to quantify changes on vertical or very steep surfaces where landsliding typically occurs (e.g., Lague et al., 2013). The “Multiscale model-to-model cloud comparison” (M3C2) algorithm implemented by Lague et al. (2013) rather considers a direct 3D point cloud comparison. This algorithm has three main advantages over a DoD: (i) it operates directly on 3D point clouds, avoiding a phase of DEM creation that is conducive to a loss of resolution imposed by the cell size and potential data interpolation, (ii) it computes 3D distances along the normal direction of the topographic surface, allowing better capture of subtle changes on steep surfaces, and (iii) it computes a spatially variable confidence interval that accounts for surface roughness, point density and uncertainties in data registration. Applicable to any type of 3D data to measure the orthogonal distance between two point clouds, this approach has generally been used for terrestrial lidar and UAV photogrammetry over sub-kilometer scales. In the context of landsliding, it has been used to infer the displacement and volume of individual landslides, using point clouds obtained by UAV photogrammetry (e.g., Esposito et al., 2017; Stumpf et al., 2015), as well as for rockfall studies (Benjamin et al., 2020; Williams et al., 2018) and sediment tracking in post-wildfire conditions (DiBiase and Lamb, 2020). To our knowledge, systematic detection and segmentation of hundreds of landslides from 3D point clouds have not yet been attempted.

Here, we produce an inventory map of landslide topographic changes using a semi-automatic 3D point cloud differencing (3D-PcD) method based on M3C2 and applied to multi-temporal airborne LiDAR data. We use the generic term of “landslide” to define the spatially coherent changes detected by our method on hillslopes that result in at least several decimeter of erosion (i.e., scars or sources) or deposition. This definition therefore includes all the types of mass wasting processes which involves the rapid displacement of soil, rocks and debris. The 3D landslide inventory is then compared to a traditional manually mapped
inventory of landslide scars based on aerial image comparison, hereafter called the 2D inventory. We apply our method to a complex topography located near Kaikoura, New Zealand, where the 2016 Mw 7.8 earthquake triggered nearly 30,000 landslides over a 10,000 km² area (Massey et al., 2020). A large part of these landslides have been mapped by Massey et al. (2020) providing a region based landslide distribution area and V-A scaling relationships. We choose a 5 km² area characterized by a high landslide spatial density along the Conway segment of the Hope fault, inactive during the earthquake, where pre- and post-earthquake LiDAR and aerial images were available (Fig. 1). This area has a variety of vegetation cover (e.g. forest, sparse or low vegetation, bare bedrock) and typically represents a challenge for conventional 2D landslide mapping. We illustrate the benefits of working directly on 3D data to generate landslide source and deposit inventories, and discuss the methodological advantages to operate directly on point clouds with M3C2 compared to DoD in terms of detection accuracy and error for total landslide volume.

The paper is organized as followed: first, the LiDAR dataset is presented followed by a detailed description of the 3D-PcD method. Second, results of the geomorphic change detection and identification of individual landslides in the studied area are presented. The remaining part of the paper focuses only on landslide sources. First, the comparison with conventional 2D landslide mapping is presented. Then, the statistical properties of the 3D and 2D landslide source inventories are investigated in terms of area and volume. Finally, current limitations of the method are discussed as well as knowledge gained on the importance of landslide under-detection on the co-seismic landslide inventory budget and landslide source geometry statistics.
2. Data description

In this study, we compare two 3D point clouds obtained from airborne LiDAR data collected before and after the November 14 2016 Kaikoura earthquake (Table. Error! Source of reference not found.). Both airborne LiDAR surveys were acquired during summer. Pre-earthquake (pre-EQ) LiDAR data were collated over six flights performed from March 13, 2014 to March 20, 2014 for a resulting ground point density of 3.8 ± 2.1 pts/m². The vertical accuracy of this dataset has been estimated at 0.068 m to 0.165 m as the standard deviation of the difference between the elevation of GPS points located on highways and the nearest neighbour LiDAR shot elevation (Dolan and Rhodes, 2016). The post-earthquake (post-EQ) LiDAR survey took place rapidly after the earthquake from December 3, 2016 to January 6, 2017 for an average ground point density of 11.5 ± 6.8 pts/m². The vertical accuracy of this dataset has been estimated following the same protocol than the pre-earthquake LiDAR data with a mean of 0.00 m and a standard deviation of 0.04 m (Aerial survey, 2017). The difference in acquisition dates represents a period of 2 years and 8 months. For both LiDAR point clouds, only ground points defined by the data provider are selected (see details of the classification in Dolan, 2014). Manual quality control showed that some points located on vegetation remained in the pre-EQ data. As these points are located a few meters above the ground, they can lead to false landslide detection. We thus reprocessed this dataset to remove incorrectly classified points (details in section S1 in the supplements). Removed points represent 0.3% of the pre-EQ original point cloud.

In addition, orthoimages were used to perform a manual mapping of landslides to compare the detection of landslides from the 3D approach and a more classical approach. The pre-EQ orthoimage was obtained on January 24 2015 (available at https://data.linz.govt.nz/layer/52602-canterbury-03m-rural-aerial-photos-2014-2015) and the post-EQ one on December 15 2016. The resolutions are 0.3 and 0.2 m, respectively.

Table 1: Information about LiDAR data used in this study

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<th>Pre-earthquake LiDAR</th>
<th>Post-earthquake LiDAR</th>
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<tr>
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<td>13/03/2014 – 20/03/2014</td>
<td>03/12/2016 – 06/01/2017</td>
</tr>
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<td>USC-UCLA-GNS science/NCALM</td>
<td>Land Information New Zealand/AAM NZ</td>
</tr>
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<td><strong>Availability</strong></td>
<td><a href="https://doi.org/10.5069/G9G44N75">https://doi.org/10.5069/G9G44N75</a></td>
<td>On request at gisbasemap.ecan.govt.nz</td>
</tr>
<tr>
<td><strong>Original point density (pts/m²)</strong></td>
<td>9.02</td>
<td>19.2 ± 11.7</td>
</tr>
</tbody>
</table>
### 3. Methods and parameter choice

#### 3.1. 3D point cloud differencing with M3C2

The method developed here to detect landslides consists of 3D point cloud differencing between two epochs using the M3C2 algorithm (Lague et al., 2013) available in the Cloudcompare software (Cloudcompare v2.11, 2020). This algorithm estimates orthogonal distances along the surface normal directly on 3D point clouds without the need for surface interpolation or gridding. While M3C2 can be applied on all points, the algorithm can use an accessory point cloud, called core points. In our case, core points constitute a regular grid with constant horizontal spacing generated by the rasterization of one of the two clouds. In the following, all the M3C2 calculations are done in 3D using the raw point clouds, but the results are “stored” on the core points. The use of a regular grid of core points has four advantages: (i) a regular sampling of the results allows computation of robust statistics of changes, unbiased by spatial variations in point density; (ii) it facilitates the volume calculation and the uncertainty assessment; (iii) it can be directly reused with 2D GIS as a raster (rather than a non-regular point cloud); and (iv) it speeds up calculations, although in the proposed workflow, computation time is not an issue and can be done on a regular laptop.

The first step of M3C2 consists in computing a 3D surface normal for each core point at a scale \( D \) (called the normal scale) by fitting a plane to the core points located within a radius of size \( D/2 \). Once the normal vectors are defined, the local distance between the two clouds is computed for each core point as the distance of the average positions of the two point clouds at a scale \( d \) (projection scale). This is done by defining a cylinder of radius \( d/2 \), oriented along the normal with a maximum length \( p_{\max} \). Distances are not computed if no intercept is found in the second point cloud. M3C2 also provides uncertainty on the computed distance at 95% of confidence based on local roughness, point density and registration error as follows:

\[
LoD_{95\%}(d) = \pm 1.96 \left( \sqrt{\frac{\sigma_1(d)^2}{n_1} + \frac{\sigma_2(d)^2}{n_2} + \text{reg}} \right)
\]

where \( LoD_{95\%} \) is the Level of Detection, \( \sigma_1(d) \) and \( \sigma_2(d) \) are the standard deviation of distances of each cloud, at scale \( d \), measured along the normal direction, \( n_1 \) and \( n_2 \) are the number of points and \( \text{reg} \) is the co-registration error between the two epochs. \( \text{Reg} \) is assumed to be spatially uniform and isotropic in our case, but could be spatially variable and anisotropic (James et al., 2017). Because point density and surface roughness are spatially variable, \( LoD_{95\%} \) is also spatially variable. For instance,
in forested steep hillslopes, points located under the canopy, with a lower point density, or vegetation points incorrectly filtered out creating locally high roughness, result into a higher LoD$_{95\%}$ and therefore require a larger topographic change to be detected as significant change. The M3C2 definition of the LoD$_{95\%}$ makes the conservative choice of adding the registration error to the combined standard error related to point cloud roughness, rather than taking the square root of the sum of squared standard error and squared registration. This choice is dictated by the simplistic hypothesis of using a spatially uniform and isotropic $reg$, while in reality $reg$ varies spatially due to intra-survey registration errors of flight lines, and inter-survey rigid registration (Passalacqua et al., 2015). M3C2 has the option to compute the distance vertically which bypasses the normal calculation, and we use this option several times in the workflow. We use the abbreviation vertical-M3C2 in that case and 3D-M3C2 otherwise.

3.2. The Same Surface Different Sampling test

Following the approach proposed in Lague et al. (2013), we use a test based on using different sampling of the same natural surface to tune parameters of the workflow and apply the entire workflow. To this end, we create two randomly sub-sampled versions of the post-earthquake LiDAR data (which has the largest point density) with an average point density equal to the pre-EQ data. The resulting point clouds corresponds exactly to the same surface (i.e., $reg=0$), with roughness characteristics typical of the studied area, but with different point sampling. Applying the entire workflow to these two point clouds, allows to evaluate the prevalence of false landslide sources and deposits only related to the difference in sampling of a rough surface. We subsequently refer to this type of approach as a Same Surface Different Sampling test (SSDS test).

3.3. Parameter selection and 3D point cloud differencing performance

In this section, we explain how to select the appropriate normal scale $D$ and projection scale $d$ to detect landslides using M3C2. The normal scale $D$ should be large enough to encompass enough points for a robust calculation, and smooth out small-scale point cloud roughness that results in normal orientation flickering and overestimation of the distance between surfaces (Lague et al., 2013). However, $D$ should also be small enough to track the large-scale variations in hillslope geometry. By studying roughness properties of various natural surface, Lague et al. (2013) proposed that the ratio of the normal scale and the surface roughness, measured at the same scale, should be larger than about 25. We thus set $D$ as the minimum scale for which a majority of core points verify this condition. As roughness is a scale and point density dependent measure, we explore a range for $D$ from 2 m to 15 m for the pre-EQ dataset, which has the lowest point density (Fig. 2.a). We found that $D \sim 10$ m represents a threshold scale below which the number of core points verifying this condition significantly drops.

The projection scale $d$ should be chosen such that it is large enough to compute robust statistics using enough points, but small enough to avoid spatial smoothing of the distance measurement. Following Lague et al. (2013), M3C2 computes eq. (2) only if 5 points are included in the cylinder of radius $d/2$ for each cloud. In our case, the pre-EQ data with the lowest point density will thus set the value of $d$. We use a SDDS test applying M3C2 with $D=10$ m and $d$ varying from 1 to 40 m. Results show
that (Fig. 2b): (i) when it can be computed the $\text{LoD}_{95\%}$ actually predicts no significant change for at least 95% of the time, indicating that the statistical model behind eq. (2) (Lague et al., 2013) is correct for this dataset; (ii) the fraction of core points for which the $\text{LoD}_{95\%}$ can be calculated rapidly increases between 1 and 8 m at which point it reaches 100%. We choose $d=5$ m as it represents a good balance between the ability to compute a $\text{LoD}_{95\%}$ on most core points (here, ~ 97%) and the smallest projection scale possible. To be able to generate M3C2 confidence intervals for as many points as possible, in particular on steep slopes below vegetation, we use a second pass of M3C2 with $d=10$ m using the core points for which no confidence interval was calculated at $d=5$ m. We note that $d$ could theoretically be set as a function of the lowest mean point density of the two LiDAR datasets, $res$, by $d \sim 25/\pi \times res$. In our case the pre-EQ dataset has $res = 3.8 \text{ pts}/\text{m}^2$ and would predict $d = 1.3$ m. However, the presence of vegetation significantly reduces the ground point density in some parts and the overlapping of flight lines creates localized high point density. Examining the mean ground point density of the entire dataset thus gives an incomplete picture of the strong spatial variations in point density. These changes in point density, critical to the correct evaluation of the $\text{LoD}_{95\%}$ (eq. (2)), are generally lost when working on raster of elevation (e.g., DEM). The spacing of the core point grid should be smaller than half the projection scale $d$ to ensure that all potential points are covered by at least one M3C2 measurement, while being larger than the typical point cloud spacing of the lowest resolution dataset. Because the ground point density on steep forested hillslope of the 2014 survey is of the order of 1 pt/m², we set a core point spacing of 1 m. Finally, the maximum cylinder length $p_{max}$ was set to 30 m as it encompassed the maximum change observed in the study area. This is generally obtained by trial and error. Setting $p_{max}$ too large increases computation time significantly and may result in two different surfaces of the same point cloud being averaged (e.g., near very steep divides or in narrow gorges).

Figure 2: Analysis of two main parameters of the M3C2 algorithm: the normal scale $D$ and the projection scale $d$. (a) Ratio between normal scale and mean roughness for different normal scale values, and fraction of the pre-earthquake core points for which the normal scale is 25 times larger than the local roughness. (b) Percentage of computed points with a confidence interval of 95% versus projection scale $d$. The percentage of non-significant points is represented as well as the percentage of points where the Level of Detection ($\text{LoD}_{95\%}$) was computed (i.e., with at least 5 points on each point cloud).
3.3. 3D landslide mapping workflow and parameter selection

Our 3D landslide mapping workflow is divided in five main steps (Fig. 3).

![Figure 3: Workflow of the 3D point cloud differencing method for landslide detection and volume estimation with schematic representations of the different steps (a,b,c).](image)

(a) 3D measurement step with the shadow zone effect, where the red lines show the normal orientation. (b) Vertical-M3C2 step. (c) Segmentation by connected component. The resulting sources and deposits are individual point clouds illustrated in the figure by different colours.

3.3.1. Registration of the datasets and registration error estimate

To detect geomorphic changes and landslides, the two datasets need to be co-registered as closely as possible and any large-scale tectonic deformation need to be corrected. The registration error to be used in eq. (2) must also be estimated.

First, a preliminary quality control is performed to evaluate the internal registration quality of each dataset. This is feasible if the individual flight lines can be isolated, by using for instance, the pointID information specific to each line and provided in the las file format. The intra-survey registration quality can be investigated with 3D-M3C2 measurements of overlapping flight lines using a 1 m regular grid of core points, from which we define the registration bias and error as the mean and standard deviation of the 3D-M3C2 distances, respectively. The point cloud of the pre-EQ dataset results from 12 flight lines (Fig S2 in supplements), while the post-EQ corresponds to 5 flight lines. Result shows that for each dataset, no significant bias is measured between lines (maximum of 3 cm for the pre-EQ survey and 1 cm for the post-EQ survey; Tab. S3 in the supplements), but the registration error ranges from 13 to 20 cm for the pre-EQ survey, and is typically around 6 cm, with one instance at 12 cm for the post-EQ survey. Hence, the internal registration quality of the pre-EQ is significantly worse than the post-EQ dataset, a likely consequence of differences in instrument precision and post-processing methods.

Second, the registration between the two surveys must be evaluated, and in general improved. As delivered, the LiDAR datasets have a vertical shift between 1 and 2 m. To correct for this shift, a grid of core points is first created by rasterizing the dataset with the largest point density with a 1 m grid spacing. Then, a vertical-M3C2 calculation is performed and the mode of the
resulting distribution is used to adjust the two datasets by a vertical shift of 1.36 m. This approach is valid only when the fraction of the surface affected by landsliding is small. A subsequent 3D-M3C2 calculation is performed to obtain a preliminary map of geomorphic change. At this stage, a visual inspection of the pre-EQ and post-EQ orthoimages and of the preliminary 3D-M3C2 distances allow us to determine that there is no significant internal tectonic displacement. Then, we manually define areas deemed stable, 25% of the studied area (Fig. 4a), to perform a cloud matching registration. The stable areas were defined as surfaces (1) with a 3D-M3C2 distance smaller than 1 m, (2) with no visual texture changes in orthoimages, and (3) away from mass-wasting processes and forested area. Attention has been paid to select areas uniformly distributed in terms of location and slopes in the studied region to maximize the registration quality.

An Iterative Closest Point (ICP) algorithm (Besl and McKay, 1992) is then performed on the stable areas, and the obtained rigid transformation is applied to the entire post-earthquake point cloud to align it with the pre-earthquake one (Tab. S4). The mean 3D-M3C2 distance on stable areas is -0.01 m, showing that there is almost no bias left in the registration, and the standard deviation of 3D-M3C2 distances is 0.17 m (Fig. 4b). At this stage, the two datasets are considered optimally registered for the stable areas but with an unknown registration error $reg$. We propose to define $reg$ as the maximum of the standard deviation of the intra-survey and inter-survey 3D-M3C2 distances. In the ideal case of two very high quality lidar datasets, $reg$ would be equal to the inter-survey registration error. In the studied case, the pre-EQ intra-survey registration error is locally worse (0.2 m) than the inter-survey registration error (0.17 m). We thus set $reg=0.2$ m. Consequently, and according to eq. (2), with $reg=0.2$ m, our workflow cannot detect a 3D change that is smaller than 0.39 m in the ideal case of negligible roughness surface. At this stage, a 3D map of topographic change is available, but the significant geomorphic changes and individual landslides have not been isolated.

Figure 4: Map of 3D-M3C2 distances on stable areas error and the associated histogram. Map is a point cloud colored with the post-earthquake orthoimage (Aerial survey, 2017).

3.3.2. Geomorphic change detection

The registration error $reg$ is then used in a first application of 3D-M3C2, using the pre-determined projection scale $d=5$ m, to estimate the spatially variable $LoD_{95\%}$ according to eq.(2). For problematic core points, where a confidence interval could not
be estimated due to insufficient points, a second application of 3D-M3C2 is performed at a larger projection scale \(d=10\). These problematic core points generally correspond to ground points under canopy on steep slopes and represent typically 9.5\% of the entire area and up to 12\% of steep slopes prone to landsliding. Significant geomorphic changes at the 95\% confidence interval are then obtained by considering core points associated to a 3D-M3C2 distance larger than the LoD_{95\%}. Significant geomorphic changes can be associated to any geomorphic processes, including landsliding, but also fluvial erosion and deposition. Changes located in the river bed, and specifically related to river dynamics and not to landslide deposits, are manually removed using the post-EQ orthoimage. With the selection of the stable area, this is the only manual phase of the workflow.

### 3.3.3. Landslide source and deposit segmentation

Core points with negative and positive significant changes are first separated into tow point clouds of sources and deposits, respectively. A vertical-M3C2 is performed on each of these point clouds to estimate the volume of landslide sources and deposits (see section 3.3.5). As for any 2D landslide inventory, a critical component of the workflow is to segment each point cloud into individual landslide sources and areas. Segmenting complex patterns of erosion and deposition in 3D, with a very wide range of sizes is still a challenge. Here, for the sake of simplicity we use a classical clustering approach by a 3D label connected component algorithm (Lumia et al., 1983), available in CloudCompare (Fig.3.c). The point cloud is segmented into individual clusters based on two criteria: a minimum number of points \(N_p\) defining a cluster and a minimum distance \(D_m\) below which neighbouring points, measured in a 3D euclidian sense, belong to the same cluster (Lumia et al., 1983). \(N_p\), or the minimum detectable landslide source or deposit area, was set to 20 m² to be consistent with the area of the projection cylinder used to average the point cloud position in the M3C2 distance calculation, \(\pi(d/2)^2 = 19.6\) m² with \(d=5\) m. \(D_m\) is an important parameter which, if chosen too large, will favour landslide amalgamation in identical clusters, and if is too small, in relation to the core point spacing, may over-segment landslides. In any case, \(D_m\) must be larger than the core point spacing. As there is no objective way to a priori choose \(D_m\), we explore various values and choose \(D_m=2\) m as an optimal value between landslide amalgamation and over-segmentation. The impact of \(D_m\) on the statistical distribution of landslide sources is addressed in the discussion.

We note that density based clustering algorithms based on DBSCAN (Martin Ester, Hans-Peter Kriegel, Jiirg Sander, 1996) have been used for 3D rockfall inventories segmentation (e.g., Benjamin et al., 2020; Tonini and Abellan, 2014). These algorithms separate dense clusters of points, considered as coherent topographic change, from areas of low point density, considered as noise. As shown in supplementary material (S5), density based clustering approaches do not yield a significantly better segmentation than a connected component. However, they have several drawbacks ranging from slow computation time, to less intuitive selection of parameters. We have therefore not used density based clustering in the following.
3.3.4. Definition of a confidence metric for each source and deposit: the SNR

Applying the previous workflow to an SSDS test results in 89 sources and deposits detected with an area between 20 and 37 m². This represents less than 1 % of the total surface, consistent with our definition of the \( LoD_{95\%} \). However, in a context of very low landslide activity, artefacts (either negative or positive false detection) may represent a large fraction of the final inventory. Moreover, despite attempts to minimize the source of errors, false detection of sources and deposits could occur due to the classification errors of the LiDAR data or to the large M3C2 cylinder length \( p_{\text{max}} \) required to detect deep landslides intercepting different part of the same cloud in narrow gorge. To minimize these potential errors, that a label connected component cannot detect, we compute for each segmented deposit or source an equivalent signal-to-noise (SNR) ratio measured as the mean of the ratio between the 3D-M3C2 distance and the associated \( LoD_{95\%} \) for each core point. The SNR can then be used to filter the landslide inventory. We propose to estimate an optimal SNR once the landslide mapping workflow is performed on the real dataset, by comparing it to the number of sources and deposits generated via a SSDS test. The optimal SNR is then chosen to minimize the number of artefacts compared to the number of real landslide.

3.3.5. Landslide area and volume estimation

While 3D normal computation is optimal to detect geomorphic changes, it is not suitable for volume estimation which requires to consider normals with parallel directions for a given landslide. Considering 3D normals can lead to “shadow zones”, due to surface roughness, which would result in a biased volume estimate (Fig. 2a). Therefore, distances and in turn volumes are computed by using a vertical-M3C2 on a grid of core points corresponding to the significant changes (Fig. 3b). As the core points are regularly spaced by 1 m, the landslide volume is simply the sum of the vertical-M3C2 distances estimated from the individualized landslides. While the distance uncertainty predicted by the vertical-M3C2 could be used as the volume uncertainty, it significantly overpredicts the true distance uncertainty due to non-optimal normal orientation for the estimation of point cloud roughness on steep slopes (i.e., the roughness is not the detrended roughness). For each landslide source and deposit, we thus compute the volume uncertainty from the sum of the 3D-M3C2 uncertainty measured at each core point, not the vertical-M3C2 uncertainty. The volume uncertainty is specific to each landslide sources and deposits and depends on the local surface properties such as roughness, the number of points considered and the global registration error, but not on the volume itself. For each individual landslide source, the area \( A \) was obtained by computing the number of core points inside the source region. This represents the vertically projected area, to be consistent with the existing literature based on 2D studies of landslide statistics. The difference between planimetric area and true surface area (i.e., measured parallel to the surface) is addressed in the discussion.

3.4. Comparison with a manually mapped inventory based on orthoimagery

To estimate the potential in terms of landslide topographic change detection between the 3D-PcD method (3D inventory) and a traditional approach, we created a second inventory (2D inventory) by manually delineating landslide sources based on a
visual interpretation of the pre- and post-EQ orthoimages. The 3D data was not used in the process, and the mapmaker did not have a detailed knowledge of the 3D inventory. Deposits were not mapped. The 2D and 3D landslide source inventories are then compared in terms of number of landslides and intersection of mapped surfaces in planimetric view using GIS software. For areas only detected by manual mapping, we define 4 classes: (1) areas located on deposit zone detected by the 3D-PcD method, (2) areas under the \( LoD_{95\%} \), (3) areas filtered by the minimum area of 20 m² and (4) areas filtered by the application of the SNR threshold. For areas only detected by the 3D-PcD method, we first distinguish landslide areas located on forested regions from those located in forest-free areas based on the number of laser returns of the post-EQ dataset (Fig. S9 and S10). We then separate the forest-free areas into 2 classes corresponding to typical textures found on the orthoimages, and delineate manually: (1) bare-rock areas and (2) sparse or low vegetation areas. We finally analyse the proportion of under-detected areas that are connected to a landslide source in the 2D inventory.

4. Results

4.1. Geomorphic change and 3D landslide sources and deposit inventory

The map of 3D-M3C2 distances (Fig. 5a) prior to statistically significant change analysis and segmentation provide a rare insight into topographic changes following large earthquakes. At first order, it highlights areas of coherent patterns of large (3D-M3C2 > 4 m) erosion (i.e. negative 3D distances) and deposition areas (i.e. positive 3D distances) located on hillslopes and corresponding to major landslides. Simple configurations with one major source area and a single deposit area can be easily recognized. A more complex pattern of intertwined landslides and rockfalls occur on a bare rock surface in the western part of the study area with a large variety of source sizes and aggregation of deposits. Most of the deposits are located on hillslopes while the deposits of three large landslides have reached the river and altered its geometry. At second order, a variety of patches of smaller amplitude (< 2 m) is visible on hillslopes. Erosion/deposition patterns in relation to fluvial activity can be documented on the river bed. The flight line mismatch, identified during the preliminary quality control, leads to low amplitude and long wavelength patterns of negative and positive 3D distances, notably visible on the central northern part of the studied area.

The area extent of significant changes, where the absolute amplitude of change is greater than \( LoD_{95\%} \), represents 15 % of the study area (Fig 5.b). After the manual removal of changes in the fluvial domain related to fluvial processes, the minimum and maximum 3D-M3C2 distances on significant change areas are 0.40 \( \pm \) 0.40 m and 29.97 \( \pm \) 0.67 m, respectively (Fig.5.b). Due to surface roughness, the minimum \( LoD_{95\%} \) observed is thus 0.40 m.

The point cloud of significant changes was segmented to identify the landslide sources (i.e. net erosion) and deposits (i.e. net deposition). During this step, clusters smaller than the detection limit of 20 m² are removed. They account for an area of 29,823 m², that is 4.2 % of the total area of significant change. Before application of a SNR threshold, the 3D inventory contained 1270 sources and 748 deposits. Applying the workflow to evaluate the optimal threshold SNR, we found that for a SNR = 1.5, the percentage of false detection in the inventory is expected to be minimum, equal to 2.1 % (Fig.6). Applying a SNR threshold
of 1.5 removes 746 sources and 442 deposits, characterized by a mean area and standard deviation of $88.6 \pm 98$ m$^2$ and $234 \pm 198$ m$^2$, respectively. Hence, the SNR filtering removed about 59% in number of the sources and deposits, but only 17.6% and 27.6% of their total surface, respectively. This latter highlights the small individual area of the sources and deposits filtered. A large fraction of small patches in steep forested hillslopes are removed by the SNR filtering (Fig. 5b). The pre- and post-EQ raw point clouds of 20 patches with SNR < 1.5 were visually inspected in detail. It was difficult for a human expert to confirm a topographic change with high confidence owing to the very low point density and the rough topography of steep forested hillslopes. On the contrary, the final filtered dataset shows coherent patterns of upslope erosion and downslope deposition in forested areas, indicative of landslides or large rockfalls. The orthoimagery cannot however help in confirming this due to the dense canopy cover and/or the pronounced projected shadows. The SNR filtering also removed large patches of very low amplitude topographic changes on open ground (< 0.5 m, either positive or negative), located in the pre-EQ data flight line mismatch, and did not correspond to a visible change in the orthoimagery (e.g., in the central-northern part of the studied area, Fig. 5b). While the SNR filtering removes more than half of the initial number of sources and deposits, these patches are of small size, close to the LoD$_{95\%}$ and only correspond to 5.96% and 3.4% of the total source and deposit volumes, respectively.

The final landslide inventory (3D inventory) contains a total of 524 sources and 304 deposits (Fig. 5c and 7a), with many sources sharing the same deposits at the toe of hillslopes. For sources, the mean absolute vertical-M3C2 distance is 2.69 m, the standard deviation 2.91 m and the maximum absolute value 23.06 ± 0.53 m. For deposits, the mean absolute vertical-M3C2 distance is 3.40 m, the standard deviation 3.68 m and the maximum absolute value is 27.9 ± 0.49 m. The area of detected landslides ranges from 20 to 40,679 m$^2$ for sources and from 20 to 28,037 m$^2$ for deposits, and the total source and deposit areas are 286,445 and 283,661 m$^2$, respectively. The resulting individual landslide volume ranges from 0.56 ± 41.5 m$^3$ to 169,890 ± 20,188 m$^3$ for source areas, with a total of 752,616 ± 154,165 m$^3$, and from 3.5 ± 19.5 m$^3$ to 151,706 ± 15,082 m$^3$ for deposits, with a total of 949,742 ± 150,014 m$^3$. The uncertainty on total volume estimation represents 20% for sources and 16% for deposits.
Figure 5: Map of the different steps of the workflow to generate the final landslide inventory. A) 3D-M3C2 distances from the geomorphic change detection step. B) Significant changes (>LoD95%) with indication of areas filtered by the SNR threshold. C)
Final map of vertical-M3C2 distances after application of a minimum area of 20 m² and a minimum SNR =1.5. Data is overlaid on the post-earthquake orthoimagery (12-15-2016, Aerial survey, 2017). Landslide sources are in blue and landslide deposits are in red.

![Image](image.png)

**Figure 6:** Percentage of the number of artefacts compared to the total number of landslides as a function of the signal-to-noise ratio.

### 4.2. 3D vs 2D landslide source inventory

In the following analysis we separate two types of errors: detection errors, corresponding to landslides present in only one of the 2D and 3D inventories, and delimitation errors, corresponding to differences in the planimetric contours of landslides. 258 landslide sources, called hereafter 2D-sources as opposed to 3D-sources derived from 3D-PcD, were mapped from visual inspection of pre-EQ and post-EQ orthoimages (Fig. 7b). The 2D-sources represent a total area of 147,039 m² (Tab.2) with a minimum area of 7.2 m² and a maximum of 40,679 m². The minimum area detected shows that the resolution capability of the 2D inventory is finer than the 3D-PcD workflow. From the 258 2D-sources, 171 intersect 3D-sources and 87 are not detected by the 3D-PcD method. These 87 2D-sources range from 14 m² to 599 m² with 63% smaller than 100 m². However, 22 are actual deposits in the 3D inventory, highlighting detection errors in the 2D inventory. These detection errors represent 16 % of the surface of the 2D inventory and are removed in the following, leading to 65 2D-sources not detected by the 3D-PcD method. The 3D-PcD method thus detects 72.4 % of the 2D-sources, and 57.4 % of the total surface of the 2D inventory (Tab.2). The 65 2D-sources not detected by the 3D-PcD method correspond to 32 2D-sources located in areas with no statistically significant change (i.e., 3D-M3C2 distance < LoD95%), 29 2D-sources filtered by the SNR threshold and 4 2D-sources below the minimum detectable size of 20 m². In terms of planimetric surface however, the area not captured by 3D-PcD is overwhelming dominated by non-statistically significant change (40.9 % of the total 2D-sources surface are < LoD95%), as opposed to SNR filtering (1.5%) or the minimum detectable size (0.2%). The surface of non-statistically significant change corresponds to delimitation errors located on the edges of sources and deposits, owing to the averaging effect of the M3C2 approach, and the transition between landslide sources and deposits (Fig. 7c). The volume missed in 3D-sources was computed...
by using the intersection between the contours of the 2D-sources not shared in 3D and the vertical M3C2 field of the core points. We find that the volume that would be missed in the 3D inventory is 0.6% of the total volume of 3D-sources. While 171 2D-sources are common to 3D-sources, this corresponds to 144 3D-sources owing to the difference in landslide segmentation in the two inventories (Fig. 7a). The 2D inventory misses 72% (380) of the landslide sources detected in 3D, including landslides as large as 12,928 m² (blue polygon in the frame of figure 7a). The detection errors are predominantly in forest (222, 58% of detection errors) and bare rock (88, 23% of detection errors). They also occur on sparse or low vegetation (70, 18% of detection errors) as is the case of two large landslides where pronounced shadows in the post-EQ, and where the topographic change is mostly vertical (Fig. 7c). 75% of the total surface of 3D-sources, is not detected in the 2D inventory, with 26% under forest, 34% on bare rock and 40% on sparse or low vegetation areas (Tab. 2 and Fig. S11). The landslide scars in this latter domain should be generally visible owing to strong spectral contrast between pre-EQ vegetation and post-EQ rock surface. However, the large source of error is explained by the incorrect delimitation of upslope topographic subsidence related to large scars (Fig. 7c), as well as the under-detection of vertical subsidence related to translational and rotational landslides (Fig. 10b). These vertical movements of metric amplitude or less do not correspond to a clear change of orthoimagery texture, or create scarps that are too small or not easily detectable if they do not generate a shadow. Detection and delimitation errors contribute roughly equally to the 2D area under-detection (47% detection error, 53% delimitation error). The 2D-sources misses 60% of the total volume of the 3D-sources. In contrast to the missed planimetric surface, the volume missed is predominantly on bare rock (32.8%), nearly three times larger than in forest (13.9%) or sparse/low vegetation (13.4%).
Figure 7: Comparison between landslide source inventories from a) the 3D point cloud detection workflow and b) a manual mapping based on 2D orthoimage comparison. Each landslide source is shown as a single colored polygon. c) Detailed comparison of typical

Table 2: Summary of the comparison between 2D and 3D landslide source inventories. For the 2D inventory, the percentages are calculated with respect to the corrected total in which the 2D sources corresponding to 3D deposits are removed.

<table>
<thead>
<tr>
<th>Category</th>
<th>landslide sources</th>
<th>Area</th>
<th>Volume*</th>
<th>% of 3D total</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>2D inventory</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Total</td>
<td>258</td>
<td>147,039</td>
<td>NA</td>
<td></td>
</tr>
<tr>
<td>On 3D deposit</td>
<td>22</td>
<td>23,497</td>
<td>16</td>
<td>40.5</td>
</tr>
<tr>
<td>Corrected total</td>
<td>236</td>
<td>123,542</td>
<td>100</td>
<td>30</td>
</tr>
<tr>
<td>Shared</td>
<td>171</td>
<td>70,936</td>
<td>57.4</td>
<td>39.9</td>
</tr>
<tr>
<td>&lt; min area (20 m²)</td>
<td>4</td>
<td>295</td>
<td>0.2</td>
<td>179</td>
</tr>
<tr>
<td>&lt; SNR threshold</td>
<td>29</td>
<td>1848</td>
<td>1.5</td>
<td>1,790</td>
</tr>
<tr>
<td>&lt; LoD$_{95%}$</td>
<td>32</td>
<td>50,463</td>
<td>40.9</td>
<td>2,877</td>
</tr>
<tr>
<td><strong>3D inventory</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Total</td>
<td>524</td>
<td>286,445</td>
<td>100</td>
<td>100</td>
</tr>
<tr>
<td>Shared</td>
<td>144</td>
<td>70,936</td>
<td>24.7</td>
<td>39.9</td>
</tr>
<tr>
<td>Forest</td>
<td>222</td>
<td>56,288</td>
<td>19.7</td>
<td>13.9</td>
</tr>
<tr>
<td>Bare rock</td>
<td>88</td>
<td>73,191</td>
<td>25.5</td>
<td>32.8</td>
</tr>
<tr>
<td>Sparse or low vegetation</td>
<td>70</td>
<td>86,124</td>
<td>30.1</td>
<td>13.4</td>
</tr>
</tbody>
</table>

*: volumes for the 2D inventory are computed from the vertical-M3C2 of core points located within the sources delimitations

4.3. Landslide sources area, depth and volume analysis

The area distribution of landslide sources is computed as follow (Hovius et al., 1997; Malamud et al., 2004):

\[
p(A) = \frac{1}{N_{LT}} \times \frac{\delta N_L}{\delta A} \tag{3}
\]

where \( p(A) \) is the probability density of a given area range within a landslide inventory, \( N_{LT} \) is the total number of landslides and \( A \) is the landslide source area. \( \delta N_L/\delta A \) corresponds to the number of landslides with areas between \( A \) and \( A + \delta A \). The landslide area bin widths \( \delta A \) are equal in logarithmic space.

First, the area distribution of landslide sources inventories obeys a power-law scaling relationship consistent with previous studies (e.g., Hovius et al., 1997; Malamud et al., 2004). The exponents are respectively \( c = -1.78 \pm 0.07 \) and \( c = -1.72 \pm 0.04 \) for the 2D and 3D inventory, respectively (Fig. 8a). The landslide area distribution of the 2D inventory shows a cut-off around 100 m² and a roll-over, characteristic of landslide distributions, around 20 m² (Guzzetti et al., 2002; Malamud et al., 2004; Malamud and Turcotte, 1999; Tanyaş et al., 2019). The landslide area distribution of the 3D inventory does not exhibit a
rollover but a cut-off of the power-law behaviour around 40 m². This behaviour differs from the one observed from the landslide area distribution from Massey et al. (2020) in the broader Kaikoura region for which a cut-off appears around 1000 m² with a rollover at 100 m².

The volume distribution of the landslide sources of the 3D inventory was defined using equation (3), replacing $A$ by the volume $V$, and also exhibits a typical negative power-law scaling (Fig.8b) of the form: $p(V) = dV^e$. The exponent of the power-law relationship is $e = -1.61 \pm 0.08$. A roll-over is visible on the landslide volume distribution around 20 m³. Considering that the minimum $LoD_{95\%}$ observed in 3D is 0.40 m, and that the minimum landslide area is 20 m², the minimum volume that we can confidently measure should be 8 m³, a value close to the observed rollover. 10 landslides are smaller than 8 m³ in our inventory. They correspond to peculiar cases of very small landslides where negative 3D distances close to the $LoD_{95\%}$ are positive when measured vertically and thus reduce the apparent volume of eroded material.

With a direct measurement of landslide volume, it is possible to compute the volume-area relationship (eq. (1); Simonett, 1967; Larsen et al., 2010) and to compare it with previous results in New Zealand (Larsen et al., 2010, Massey et al., 2020). Here we determine V-A scaling coefficients using two methods: by fitting a linear model (1) on log-transformed data and (2) on averaged log-binned data. While the first method leads to a V-A relationship best describing the volume of each landslide, the second one is not affected by the varying number of landslides in each range of landslide area and leads to a V-A relationship that best matches the total landslide volume. Using the first approach, we find a volume-area scaling exponent of $\gamma = 1.16 \pm 0.02$ and an intercept log $\alpha = -0.28 \pm 0.04$ m$^{0.7}$ with a determination coefficient $R^2 = 0.88$ (Fig.8.c). Using the second method, we find $\gamma = 1.17 \pm 0.02$, an intercept log $\alpha = -0.26 \pm 0.08$ m$^{0.7}$ and a determination coefficient $R^2 = 0.99$. We also obtain a good correlation $R^2$ of 0.83 and 0.79 with the Larsen et al. (2010) relationships derived from soil landslides and from mixed soil landslides and bedrock landslides, respectively (Tab.333). $R^2$ of 0.85 is obtained when considering the parameters of the V-A relationships of the Kaikoura region, derived by Massey et al. (2020), including all their mapped landslides. At first order, the V-A relationships we obtained are thus consistent with previous studies. Yet, if the relationships from Larsen et al. (2010) and Massey et al. (2020) were applied to our landslide area inventory, the total volume would vary from $0.376\times10^6$ m³ to $1.005\times10^6$ m³ (Tab.3), compared to $0.753\times10^6 \pm 0.154\times10^6$ m³ that we estimate directly. The closest evaluation of the total volume is based on the Massey et al. (2020) V-A relationship, that predicts a total volume of $0.653\times10^6$ m³. The farthest evaluation of the total volume is the V-A relationship from Larsen et al. (2010) for all landslides ($1.005\times10^6$ m³), while their soil-dominated landslide relationship only predicts half of the total volume.

We presented the V-A relationship as it classically used in co-seismic volumes estimate from 2D inventories, however the volume being the product of mean depth and area, the V-A relationship hides an indirect correlation with area which may hinder subtle variations of depth with landslide size. Fig 8c shows that mean depth increases on average with area as a power law with an exponent $0.16 \pm 0.03$ consistent with the V-A relationships we derived. However, the binned data suggests potentially two different trends: one for landslides smaller than 1000 m² in which, mean depth is nearly constant and exhibits a factor 4 of variation for given area ($\sim 0.7$ m to $\sim 3$ m), while depth increases with area for sources larger than 1000 m².
However, the limited number of landslides in our inventory is insufficient to be conclusive on the existence of two different regimes.

Figure 8: Landslide sources inventory analysis of the study area. (a) Landslide area distribution of both 3D and 2D inventory and Massey et al. (2020). (b) Landslide volume distribution of the 3D inventory. (c) Volume-area scaling relationships with uncertainty on volume and comparison with Larsen et al. (2010) and Massey et al. (2020) relationships obtained in New Zealand. The landslide mean depth vs area is also presented in inset. All scaling parameter values are summarized in Table 3.

Table 3: Power-law scaling parameter values of the relations shown in Figure 8. Log $\alpha$ and $\gamma$ are scaling parameters from the landslide area-volume relationship. Unit of $\alpha$ is $[L(3-2\gamma)]$ with $L$ in meters. Landslide source area and volume distribution coefficients are $b$ and $d$ while exponents are $c$ and $e$ respectively. The coefficient of determination $R^2$ is also given for each power-law fit function. The total volume refers to the application of the V-A relationship to the landslide areas of the 3D inventory.

<table>
<thead>
<tr>
<th></th>
<th>$\log b$, $\log d$ or $\log \alpha$</th>
<th>$c$, $e$ or $\gamma$</th>
<th>$R^2$</th>
<th>Total Volume ($m^3$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Landslide area distribution (3D inventory)</td>
<td>0.70 ± 0.12</td>
<td>-1.72 ± 0.04</td>
<td>0.99</td>
<td>-</td>
</tr>
<tr>
<td>Landslide area distribution (2D inventory)</td>
<td>1.07 ± 0.20</td>
<td>-1.78 ± 0.07</td>
<td>0.99</td>
<td>-</td>
</tr>
<tr>
<td>Landslide volume distribution</td>
<td>0.39 ± 0.26</td>
<td>-1.61 ± 0.08</td>
<td>0.98</td>
<td>$0.753 \times 10^6$ (direct measurement)</td>
</tr>
<tr>
<td>V-A relationship from averaged log-binned data (this study)</td>
<td>-0.26 ± 0.08</td>
<td>1.17 ± 0.02</td>
<td>0.99</td>
<td>$0.643 \times 10^6$</td>
</tr>
<tr>
<td>V-A relationship from log-transformed data (this study)</td>
<td>-0.28 ± 0.04</td>
<td>1.16 ± 0.02</td>
<td>0.86</td>
<td>$0.524 \times 10^6$</td>
</tr>
<tr>
<td>V-A relationship for soil landslides</td>
<td>-0.37 ± 0.06</td>
<td>1.13 ± 0.03</td>
<td>0.83</td>
<td>$0.376 \times 10^6$</td>
</tr>
</tbody>
</table>
5. Discussion

The aim of this paper is to present a semi-automatic workflow, called 3D-PcD, for the detection and geometric characterization of landslide sources and deposits from repeated airborne LiDAR data. We specifically aim to overcome issues such as under-detection of landslides in inventories based on imagery analysis, landslide amalgamation and V-A relationship biases on total volume calculation. In the following, we discuss 1) the benefits and limits of the 3D-PcD method, 2) the benefits of 3D change detection to create landslide inventories, and 3) how 3D landslide inventories shed new light on the scaling properties of landslide sources.

5.1. 3D point cloud differencing and landslide detection

5.1.1 Vertical versus 3D change detection capability, and the M3C2 algorithm

The importance of detecting changes in 3D (3D-M3C2), as opposed to vertically (vertical-M3C2), in steep slopes can be illustrated by a SSDS test applied to the post-EQ point cloud (Fig. 9). Typical of change measurement methods on rough surfaces with random point sampling (e.g., Lague et al., 2013), a non-null mean distance is often measured, even though the two point clouds are samples of exactly the same surface. The distribution of measured distances is centred near zero, with a means of $-2.10^{-4}$ and $1.10^{-4}$ m, for the vertical and 3D approach respectively. However, the 3D approach results in a standard deviation, $\sigma=0.05$ m, four times smaller than using a vertical differencing, $\sigma= 0.20$ m. The map of distance shows that vertical differencing systematically results in much larger distances on steep slopes than the 3D approach, while they both yield similar low distances on horizontal surfaces.

We thus find that the 3D-PcD method offers a greater sensitivity to detect changes compared to classical vertical DoD. This difference is particularly important as it propagates into a lower level of detection and uncertainty on volume calculations. Using the M3C2 algorithm in 3D (Lague et al., 2013) also offers the benefit of accounting for spatially variable point density and roughness in estimating a distance uncertainty for each core point, that can be subsequently used in volume uncertainty calculation. For instance, 3D-M3C2 reduces the sensibility of change detection in vegetated areas to a lower ground point density and potentially to a higher roughness due to vegetation misclassification. In turn, this advantage prevents in part the detection of false sources or deposits by using 3D-M3C2. By using a regular grid of core points as in Wagner et al. (2017), our workflow combines the benefits of working directly with the raw unorganized 3D data, as opposed to DoD where the relationship with the underlying higher point density data is lost. This approach also produces results with a regular sampling
that can easily be used for unbiased spatial statistics, volume calculation and easy integration into 2D GIS software. Compared to DoD, if an interpolation is needed, it is performed on the results rather than on the original DEM which can lead to uncontrolled error budget management.

Figure 9: Comparison between vertical differencing (vertical-M3C2) and 3D differencing (3D-M3C2) on the post-EQ point cloud, sub-sampled randomly two times to generate two point clouds of the same surface with a different sampling (Same Surface Different Sampling test). A) Resulting change detection maps of the two different techniques. B) Histogram of the computed distances with the two techniques.

5.1.2. Current limits of the method

Registration: A critical aspect of the comparison of 3D point clouds is their co-registration, in particular in the context of co-seismic landsliding. In this study, a rigid transformation is applied to the entire datasets using an ICP algorithm (Besl and McKay, 1992), assuming that internal deformation induced by the earthquake is negligible. The 3D-M3C2 map does not exhibit any systematic horizontal shift either north or south of the Hope fault. We thus conclude that internal deformation, if any, was below the typical registration error in our study area. For larger studied regions with internal deformation and in the absence of a 3D co-seismic deformation model that could be applied to the post-EQ point cloud (e.g., Massey et al., 2020), our workflow should be applied in a piecewise manner with boundaries corresponding to the main identified faults or deformation zones. For landslide inventories following climatic events, the application to large datasets should be straightforward as no significant internal deformation is expected. Similarly, we also note internal flight line height mismatches of 0.13-0.20 m in the pre-EQ survey that are difficult to correct after data delivery and generate some apparent large scale low amplitude topographic changes (Fig. 4, Tab. S3 and section S2 in supplements). Interestingly, in the M3C2 calculation, flight line mismatches are averaged out in the distance measurement but leads to a higher local point cloud standard deviation, and thus to an increase of the LoD95% and to a lower probability of incorrect topographic change detection. Despite some significant flight line mismatches in the pre-EQ dataset, using a SNR filtering approach efficiently removes the few false positive sources related to this issue. This highlights 1) the need for a detailed quality control (e.g., by applying M3C2 on overlapping lines) to
ensure the highest accuracy of the LiDAR data, 2) the importance of the statistical significance tests performed at the core point scale, and 3) the need for confidence metrics at the landslide scale, such as the SNR, to filter out a variety of potential false landslides. Ideally, a spatially variable model for point cloud errors and registration should be developed for each survey and combined into a more accurate and complete form of LoD than what the M3C2 approach currently offers (e.g., Glennie, 2008; Passalacqua et al., 2015). However, the position and attitude information of the sensor (e.g., Smoothed Best Estimate of Trajectory file) and raw LiDAR data area rarely available on LiDAR data repositories. Additionally, a dense network of ground control points is hard to get in mountainous environment. It is thus frequently impossible either to reprocess the LiDAR data to improve its quality (e.g., Glennie et al., 2014), or to create a spatially variable registration and point cloud error model.

**Landslide segmentation:** The connected component segmentation is a simple, objective and rapid way to separate landslides in 3D that can be scaled up to much larger datasets. However, given the complexity of the 3D data, and in particular the very large range of landslide sizes (i.e., 4 orders of magnitude in the studied case), it inevitably exhibits some drawbacks and is subject to improvement. In particular, landslide amalgamation occurs, between two sources or deposits, if two of their core points are closer than $D_m$. Hence, landslides occurring on the two sides of a collapsed divide can be connected. This is the case for the largest landslide of our database located on the rock cliffs on the western part of the study area (Fig. 7a and Fig. 10a). In this example, the landslide source could reasonably be segmented in at least 5 smaller landslides. However, there does not seem to be a unique way to segment such a complex set of amalgamated events, even manually, underlining that landslide segmentation, can never be fully objective. We have explored the use of fast implementations of density based spatial clustering algorithm derived from DBSCAN (Martin Ester, Hans-Peter Kriegel, Jiirg Sander, 1996), an algorithm used for segmentation of 3D point clouds of rockfalls and removal of noisy points (e.g., Benjamin et al., 2020; Tonini and Abellan, 2014; details in section S5 in supplements). We applied OPTICS (Ankerst et al., 1999), recently used for rockfall segmentation of 3D lidar data (Carrea et al., 2021) and HDBSCAN (McInnes et al., 2017) which has a better ability to detect clusters of various sizes compared to DBSCAN, and is much faster. However, none managed to provide a significantly better segmentation of the largest landslides of our database, and the density probability of source area they produce is very similar to the one generated by a connected component. These approaches are however significantly longer to run than a connected component in Cloudcompare (S5 in supplementary material), and have parameters which are less intuitive to set than $D_m$, which is a distance directly comparable to core point spacing. New segmentation approaches accounting for normal direction, divide organization and 3D depth maps of amalgamated sources are needed to improve the segmentation of complex cases. We note however that segmentation issues do not affect the total landslide volume calculation in our study and that a sensitivity analysis of the impact of $D_m$ shows that landslide source statistics are not severely affected by this parameter as long as it is close to the value we have used (see section 5.2).

**Landslide volume calculation:** Landslide volume is computed using a vertical-M3C2 on regular core points. This facilitates volume calculation on potentially complex 2D landslide geometry, but may lead to incorrect volume estimates on very steep slopes. Yet, the median slope distribution of the source core points (measured on the pre-EQ surface, Fig S12) is 34.6°, and only 0.74% of the core points have slopes higher than 60°. We thus expect this effect to affect a very small fraction of our
inventory. Measuring landslide volume in 3D would be preferable, for instance along a constant surface normal direction defined for each source or deposits, but such simple approach is not better than a vertical measurement for the complex surface geometry of large landslides observed in the dataset and which are properly segmented (e.g., Fig. 7c). New approaches based on 3D mesh reconstruction have been used recently for rockfall volume estimation (Benjamin et al., 2020) and represent a future improvement of our workflow.

**Landslide surface area:** Another simplification of our approach is the calculation of planimetric surface areas, rather than true surface area. This choice was made to be consistent with previous results based on 2D inventories and to facilitate the comparison with our image based inventory. Measuring surface parallel area with 3D data would potentially help unravel new relationships between normal depth and area that are independent of topographic slope. Yet, this calculation is not trivial for complex landslide geometries in which assuming a unique normal orientation to get a surface parallel area measurement could result in a strong bias (e.g., Fig. 7c). Approaches based on 3D mesh surface calculation could help resolve this. Given that the median of the slope distribution of our landslide source inventory is 34.1°, a back of the envelope estimate of the true area gives a total landslide source area of 356,876 m² rather than 286,445 m².

**Translational landslides:** The 3D-PcD workflow we have designed is not designed for the measurement of translational landslides for which the dominant movement is parallel to the topographic surface. As in figure 10b, these landslides will appear as negative surface elevation in the source area and positive in the downslope accumulation area with little or non-significant 3D-M3C2 distance over much of the landslide body. These landslides can be detected with the 3D-PcD workflow, but the corresponding volume and area of sources may not be fully relevant to the bulk of the landslide inventory for which the source material has travelled further downslope exposing a large part of the slip surface. For mostly translational landslides, the surface parallel component of the deformation may be evaluated with feature tracking approaches as long as there are features to track (e.g., Aryal et al., 2012; Teza et al., 2007). The only elements that could be easily tracked in the 3D-PcD workflow are the barycenter of the source and associated deposit of each landslide, to explore runout dynamics, but we have not investigated this option yet.

**Significant changes and geomorphic processes:** While not a limitation per se, the 3D-PcD workflow detect changes, but cannot classify the nature of this change into various types of geomorphic processes. Given the current LoD95% (i.e., > 0.40 m) only large topographic changes, correspond to landslide type processes on hillslopes and fluvial processes, are detected. Debris-flow processes could be detected, and may actually be part of the processes that remobilize landslide debris, however, they potentially create erosion in narrow steep channels that are likely below our spatial resolution capability, or will generate very small sources. They could however contribute to generate very large deposits. Fluvial processes are removed by the only manual operation performed in 3D-PcD, deemed necessary to preserve landslide deposits that have reached the river. While we do not have independent field constraints for all our detected sources, we are confident that the strict handling of error and SNR filtering approach filters out artefacts, and that our inventory of sources only contains landslide processes. Our approach does not directly resolve the typology of the landslides, including their failure mechanism (sliding, flow, fall), the failed materials (rock, soil, debris) and the velocity of the displacement (Hungr et al., 2014). Yet, combining the 3D-M3C2 distance
field with orthoimages (Fig. 10), we have identified the presence of rock avalanches, slumps (rotational failures), debris slides (translational failure) and we suspect the occurrence of some large rockfalls, although pre-EQ slopes steeper than 60° are extremely rare in the detected sources. We did not try to separate these as: (1) we were primarily interested in co-seismic volumes rather than detailed landslide mechanics which would have required field data; (2) there is no way to univocally identify, for the vast majority of our sources, the dominant landslide mechanism with either the 3D-M3C2 distance field and/or the orthoimages; (3) large landslides for which a dominant mechanism can be identified are too few in our inventory to draw a robust inference on scaling properties and geometry.

5.1.3. Landslide topographic change detection compared to manual passive imagery mapping

We presented for the first time a comparison between a classical handcrafted inventory of landslide sources from 2D orthoimagery comparison, and a 3D inventory based on LiDAR change detection where landslides are detected according to the topographic change they produce, not a change in optical passive imagery. Results show how different two landslide inventories of the same region, constructed from fundamentally different data sources (passive vs active remote sensing), can be. While the 3D inventory cannot be considered exhaustive, as it has a non-null LoD$_{95\%}$, it nonetheless detects roughly 3 times more landslides than the 2D imagery and a planimetric area affected by landsliding nearly two times larger. Most importantly, the 3D-PcD workflow knows its detection limit as one of its outcome is a spatially variable confidence interval (LoD$_{95\%}$) and confidence metrics (SNR) for each segmented source and deposit. While the resolution capability of 2D image analysis can be evaluated based on pixel size and is better than the LiDAR based approach in our study case, the detection capability is much more difficult to quantify, especially if the inventory is manually handcrafted.

Both detection and delimitation errors equally contribute to under-detection of the total area in the 2D inventory. They are, as expected (Zhong et al., 2020), frequent in areas with poor spectral contrasts between successive orthoimages such as bare rock surfaces or forests. But under-detection also occurs in sparse or low vegetation zones where some very large areas corresponding to vertical subsidence at the top of rotational or translational landslides were not detected (e.g., Fig. 10b) or incorrectly mapped (e.g., Fig. 7c). We note that under-detection in forest, while very significant (58 % of all detection errors), only corresponds to 19.7% of total area and 13.9% of the total volume. This is explained by the small size of missed landslides, as large ones strip out vegetation and are easily detectable. Hence, we do not expect that under-detection on forested area represent a large contribution in previously published co-seismic landslide volume estimates. However, it may limit the detection of subsidence area associated to new retrogressive slip planes (Fig 7c) which may prove important for subsequent landslide hazard management. Delimitation and detection errors are dominant on sparse and bare rock surfaces corresponding to 55.6% of the total landslide area. In particular, it is extremely difficult to map the transition between sources and deposits, especially on large and amalgamated landslides (e.g., Fig 7c). Here the ability of the 3D-PcD approach to not only detect sources but also deposits is essential. Our results thus indicate that existing landslide inventories, manually mapped from 2D images, may significantly suffer from under-detection of landslide area at least in regions dominated by sparse or absent vegetation cover.
We show that the main reason the 3D-PcD method did not detect surfaces mapped on the 2D inventory is that these surfaces are located in areas where the 3D-M3C2 distance is below the $LoD_{95\%}$. The detection limits of the 3D-PcD will improve in future years, by using the latest generation of LiDAR instrument generating dense (> 10 pts/m²) and more accurate 3D point clouds (< 5 cm Z error). With such data, the registration error could become of the order of 5 cm or less, further improving the detection capability of 3D-PCD both in terms of spatial resolution and $LoD_{95\%}$.

![Figure 10: Two different points of interest of the 3D inventory illustrating various type of landslide mechanisms.](image)

Figure 10: Two different points of interest of the 3D inventory illustrating various type of landslide mechanisms. a) Area mostly dominated by rock avalanche, where large rockfalls are also expected. b) Debris slide with mostly translational movement (A) and slump with likely rotational to translational displacement (B). The post-earthquake orthoimage is overlaid on the point cloud (December 15, 2016; Aerial survey, 2017)

5.1.4. Toward a limitation of amalgamation and under-detection biases on total landslide volume estimation

By a direct measurement from topographic data, the amalgamation effect is no longer an issue for total landslide volume estimation of an inventory even though our segmentation approach cannot resolve the amalgamation of individual landslides perfectly. Bypassing the use of a non-linear V-A relationship also avoid uncertainty inherent to the choice of the best suited scaling parameters. As we show, the total landslide volume vary significantly (from $0.376 \times 10^6$ m$^3$ to $1.005 \times 10^6$ m$^3$ ; Tab.3) depending on the V-A scaling relationship applied to our landslide inventory. For instance, we observe a difference of 18% in total volume estimation only due to the method used to fit data (i.e. on log-transformed or on averaged log-binned data). We also note that total landslide volume estimation from such relationship can get close to the volume estimated from the 3D-PcD for wrong reasons. As instance, applying our V-A relationship to both versions of the 2D inventory with and without deposit areas (Tab.2) lead to a difference of 17% in total volume. These results highlight the overarching sensitivity of the total volume of eroded material to the V-A relationship biases (Li et al., 2014; Marc and Hovius, 2015).

Our 3D-PcD approach also allows to estimate total landslide volume without the issue of under-detection of landslides. Due to the difference in the type of under-detection and delimitation errors between both 2D and 3D inventories, these issues do not propagate into total landslide volume estimate in similar ways. The area not detected by the 3D-PcD method in the 2D inventory represents only 0.6 % of the total volume. This is a negligible component owing to the fact that only very shallow
landsides, or shallow parts of very large landslides are missed. On the contrary, the area not detected by the 2D inventory represents 60% of the total volume, highlighting the pronounced underestimation of total volume estimate if one uses image based detection followed by volume calculation. Most of this missed volume is due to the landslide delimitation errors on bare rock and sparse vegetation cover surfaces which represent 42% of the total volume while the under-detection of entire landslides only represents 18%. We also note that a third of the total volume is missed on bare rock surfaces. Our study area was chosen based on LiDAR data availability and contains a particularly high proportion of under-detected landslides in the 2D inventory due to the presence of actively eroding bare bedrock hillslopes. We expect this proportion to significantly vary when considering other landscapes with potentially varying proportions of vegetation cover, vegetation density and type (e.g. grass, shrubs, trees), lithology and ground shaking intensity. Nonetheless, our finding represents a first approach to the issue of considering the under-detection of landslides in total landslide volume estimates. We show that extreme caution should be put on co-seismic volumes estimated on landscapes where a large fraction of bare rock surfaces and sparse vegetation cover are present before earthquake, such as the Kaikoura ranges.

5.2. Landslide source scaling properties

The use of 3D data opens up a very large range of new geometric analysis of landslide sources and deposits. Here, we revisit traditional size-distributions and scaling relationships of landslide sources generated from 2D inventories. We systematically perform sensitivity analysis of these relations to the main parameters of the 3D-PcD workflow: the registration error \( \text{reg} \), the minimum distance for segmentation \( D_m \) and the SNR threshold for removing landslides with limited confidence (See Fig.11, Appendix A, S13 and S14 in supplementary materials).

5.2.1. Total volume of landslide sources and deposits

Over the studied area of ~5 km\(^2\), 524 landslide sources and 304 landslide deposits were detected with the 3D point cloud processing workflow. The scaling of pdf(V), with an exponent of -1.61 ± 0.08, indicates a slight tendency for the overall eroded volume to be dominated by the largest landslide (151,706 m\(^3\), that is 20% of the total volume). The uncertainty on total landslide volume, 16% to 20% for deposits and sources, respectively, might appear large, as it is based on a conservative 95% confidence interval that we use throughout our analysis. These uncertainties are dominated by the registration error (\( \text{reg} = 0.2 \) m) and by the lower point cloud density of the pre-earthquake LiDAR data (Table). Within these uncertainties, the total volume of sources (752,616 ± 154,165 m\(^3\)) and deposits (949,742 ± 150,014 m\(^3\)) are not statistically different. The larger volume of deposit is however consistent with rock decompaction during landsliding, which could be constrained by using a joint gravity survey in future studies (Mouyen et al., 2020). On top of this effect, we also expect an increased likelihood for sources to be more systematically filtered out than deposits as they are thinner (mean 3D-M3C2 distance are 2.69 m for sources and 3.4 m for deposits). This is consistent with the tendency for debris deposits, located on convergent parts of the landscape (e.g., hillslope hollows, debris flow channels), to collect different upslope sources in thicker patches than the initial individual sources (e.g., Fig. 10a)
5.2.2. Distribution of landslide source area and lack of rollover

We obtain a range of landslide area over 3 to 4 orders of magnitude (20 to 42,679 m²) which obey a clear power-law relationship for A > 40 m² with an exponent c = -1.72 ± 0.04 (Fig. 8a). The negative power law behaviour for landslide area is generally observed for 2D landslide inventories, although only for source areas typically larger than 500- 5000 m² (Guzzetti et al., 2002; Malamud et al., 2004; Malamud and Turcotte, 1999; Medwedeff et al., 2020). Our exponent is roughly consistent with the exponents obtained over the entire Kaikoura coseismic landslide inventory of -1.88 (N_LT = 10,195; Massey et al., 2018) but differs significantly from the most recent estimate of -2.10 (N_LT = 29,557; Massey et al., 2020, Fig. 7a) for which the power-law scaling is expressed for A > 500 m². A sensitivity analysis of the impact of the workflow parameters (Fig. 11), in particular D_m which affects the level of amalgamation in the dataset, does not yield values of c smaller than -1.85 and cannot reconcile our results with Massey and co-authors (2020). Either, our limited study area overemphasizes, by chance, the occurrence of large landslides generating a smaller value of c, the manual inventory of Massey et al., 2020 may miss a large fraction of intermediate and small landslides, especially in bare rock hillslopes which are frequent in the high mountains of the Kaikoura range.

Most importantly, the landslide area distribution that we derive does not exhibit a rollover classically observed in 2D landslide inventories. Only a small deviation of the power-law behaviour appears for A < 40 m². Varying reg or D_m does not change this behaviour (Fig. 11a and 11b), nor using a density based clustering approach (Fig. S8). Increasing the SNR threshold to 2 (Fig. 11c), and thus censoring a larger number of small/intermediate landslides with small depth, increases the deviation from the power-law behaviour, but never creates a rollover. Hence, we are confident that our probability density of source area, generated by a purely objective and automatic approach, does not exhibit a rollover. If there is any, it would occur for sizes much smaller than 20 m².

![Figure 11](image.png)

Figure 11: Landslide source area distributions for different (a) registration error reg, (b) minimum segmentation distance D_m and (c) signal-to-noise (SNR) values. All plots share the same y-axis. Value of the parameters used for this study are colored in red.

Several hypotheses, related to landslide mechanics or to landslide detection capabilities, have been put forward to explain the rollover behaviour for small landslide area. These include the transition to a cohesion dominated regime reducing the likelihood of rupture (Frattini and Crosta, 2013; Jeandet et al., 2019; Stark and Guzzetti, 2009), a cohesion gradient with depth (Frattini...
landslide amalgamation (Tanyas et al., 2019) or the under-detection of small landslides (Hovius et al., 1997; Stark and Hovius, 2001). Our segmentation approach tends to amalgamate landslides rather than over-segment large ones and cannot explain the lack of rollover. On the contrary, this would create or accentuate a rollover by suppressing small landslides through amalgamation. The lack of rollover may also hint at a transition towards a different landsliding process, where rockfall dominates for instance. However, core points in sources with slopes > 60° represent only 0.74 % of the source area, pointing at an extremely limited contribution of rockfall processes originating from near-vertical cliffs.

To evaluate the degree of under-detection as a function of landslide size, we can leverage the two inventories we have created. For this, we compute a completeness ratio as the number of detected sources in 2D over the number detected in 3D, per range of source area. Fig.12 shows that the completeness ratio is around 0.25 for areas ~20-40 m² and systematically increases with landslide size up to 0.8-0.9 for sizes larger than 200-500 m². The behaviour above 500 m² suggests a slight increase of the completeness ratio which would asymptotically tend towards 1 for very large landslide source that cannot be missed both in 2D and 3D. However, we caution that our inventories contain too few landslides above 1000 m² (~ 20 each) to draw robust conclusions on this behaviour or derive a functional relationship. As some very shallow landslides detected in 2D are not detected in 3D, we cannot consider the 3D inventory as complete for small sizes and the true completeness ratio may actually be slightly overestimated at very small sizes. Yet, the 3D inventory is however far more complete than the 2D inventory. As such, our results demonstrate that in this study area, the rollover behaviour of the 2D inventory is caused by a size-dependent under-detection of small landslides below 500 m², existing even when using high resolution imagery with a better resolving capability than our 3D-PcD workflow (7 m² vs 20 m²) (Hovius et al., 1997; Stark and Hovius, 2001). This size-dependent under-detection of small landslides is expected to be systematically present in other image-based landslide inventories, even if carefully hand-crafted. Whether this effect systematically explains all the rollovers observed in past landslide inventories, or if other hypothesis such as a transition to cohesion dominated regime also contribute or are only expressed at even smaller scales remain to be explored. In any case, the number of landslides potentially missed in previous studies can be important given the level of under-detection that we report for small sizes. For instance, we note that in the first manual inventory of the Kaikoura EQ landslides (Massey et al., 2018), only 27 landslides were detected in our study area. The volume corresponding to under-detected small landslides may actually not matter in terms of total volume produced by earthquake derived landsliding. However, the presence or not of a rollover significantly matters in terms of hazards management (i.e. impact on the exposed population, infrastructure damage etc.) owing to the very large differences in the probability of small landslides.
5.2.3. Distribution of landslide volume

We present here one of the first co-seismic landslide volume distribution derived directly from 3D topographic data (Fig. 8b), rather than inferred from the combination of the landslide area distribution, based on 2D data, and an estimated \( V-A \) relationship. Our direct measurements show that the landslide volume distribution indeed obeys a power-law relationship for \( V > 30 \text{ m}^3 \) with an exponent \( e = -1.61 \pm 0.08 \), consistent with the very broad range of exponents estimated in previous studies of \( -1.0 \leq e \leq -1.9 \) and \( -1.5 \leq e \leq -1.9 \) for rock and soil landslides, respectively (e.g., Brunetti et al., 2009; Malamud et al., 2004). The sensitivity analysis to the workflow parameters (Fig. S13 and Appendix A), shows that the exponent \( e \) will decrease with \( \text{reg} \) and the SNR threshold as these parameters will censor progressively thinner landslides which are statistically the smallest ones. A SNR threshold of 2 strongly reduces the size of the inventory, in favour of larger landslides, and \( e = -1.38 \). While a SNR =1, results in \( e = -1.69 \) and a complete lack of a rollover above the minimum detectable volume. Contrary to the distribution of source area, the segmentation distance \( D_m \) has little impact on \( e \).

The lack of a pronounced rollover above the minimum volume that we can theoretically detect (\( \sim 8 \text{ m}^3 \)), makes the comparison with rockfall volume statistics relevant. The probability distribution of rockfall volume generally obeys a power-law relationship with an exponent \( e_R \) ranging from -1 to -2.2 (e.g., Malamud et al., 2004; Benjamin et al., 2020). If we restrict existing inventories to those having at least 500 rockfalls and the largest rockfall at least of 20 \( \text{m}^3 \), the range of exponent \( e_R \) narrows to -1.5/-2 with a majority of inventories around -1.6 \( \pm 0.1 \) (Benjamin et al., 2020). Although, we do not expect rockfalls to be a dominant mechanism in our database given the lack of very steep slopes and given that rupture mechanisms (e.g., fragmentation, sliding, slumping…), rock heterogeneity and topographic constraints (e.g., hillslope size) are not expected to be similar (Dussauge et al., 2003), the consistency of the exponent we find is striking. This may suggest a much large range of scales over which the volume of landslides, encompassing rockfalls in this definition, obeys a unique scaling behavior. Dataset
specifically acquired to bridge the gap between large scale airborne lidar and terrestrial lidar are needed to get a better handle on the volume distribution of landslides, a critical information with respect to risk analysis and landslide erosion calculation.

5.2.4. Landslide depth and volume-area relationship

Our 3D-PcD approach opens the possibility to directly quantify the variations of landslide depth with size. We show that landslide mean depth does not vary for landslide area smaller than 1000 m². The same behaviour has been observed by Larsen et al. (2010) for soil failures suggesting that our landslide inventory may be relevant to shallow landslide. This is consistent with the fact that 50% of the landslide thicknesses are lower than 1.2 m and that the landslide volume-area (V-A) scaling relationships obtained in this study are close to that of Massey et al. (2020) and Larsen et al. (2010) for soil landslides. Moreover, for bedrock failures, Larsen et al. (2010) did observe an increase of landslide depth with size. Our landslide inventory may exhibit a slight increase of landslide depth for landslide area larger than 1000 m² that may hint at the transition from shallow to deeper bedrock landslide. However, the limited number of large landslides in our inventory does not allow to draw robust conclusions on this point.

The sensitivity analyses to the workflow parameters show that the V-A exponent γ is not significantly affected by the variations of the reg and SNR values we explored. Respectively, γ vary from 1.16 ± 0.03 to 1.19 ± 0.01 with the explored range of reg and varies from 1.17 ± 0.02 to 1.21 ± 0.02 with the SNR threshold (Fig S14, Appendix A). It is also not affected by the segmentation distance for \( D_m < 4 \) m, beyond which landslide amalgamation becomes significant and γ decreases to 1.1 for \( D_m=6 \) m.

6. Conclusion

In this paper, we introduce a new workflow for semi-automated landslide sources and deposit detection using 3D differencing based on high resolution topographic point cloud data. This method uses the M3C2 algorithm developed by Lague et al. (2013) for accurate change detection based on the 3D distance normal to the local surface. Landslide sources and deposits are segmented, using a 3D connected component approach, and their volumes are computed by a vertical-M3C2. Spatially variable uncertainties on distance and volume are provided by the calculation and used in the workflow to evaluate if a change is statistically significant or not, for volume uncertainty estimation and to define a confidence metric per source or deposit (Signal to Noise Ratio). The SNR is used to filter out potentially remaining artefacts. We provide various tests and recipes to estimate the registration error and to choose the parameters of the M3C2 algorithm as function of the point cloud density to ensure the lowest level of change detection, and the best resolution of the 3D map of change. Applied to a 5 km² area located in the Kaikoura region in New Zealand with pre- and post-earthquake LiDAR, we generate the first automatic inventory of landslide sources and deposits based on repeat 3D airborne LiDAR data. We show that:

- A minimum level of 3D change detection at 95% confidence of 0.40 m can be reached with airborne LiDAR data, which is largely set by the registration error. In our case, the limited quality of flight line alignment of the pre-EQ
data was the dominant source of registration uncertainty. Because it operates on raw data, M3C2 accounts for subpixel characteristics such as point density and roughness that are not accounted for when working on DEMs, and results in more robust statistics when it comes to evaluate if a change is significant or not. 3D point cloud differencing is critical on steep slopes and allows a lower level of change detection compared to the traditional DoD.

- Considering 3D topographic change for landslide detection removes the amalgamation effect on the total landslide volume by directly measuring it in 3D rather than considering an ad hoc V-A relationship. Amalgamation in 3D is still an issue when exploring individual landslide area and volume statistics given the simplistic segmentation approach that we have used. However, our approach has the benefits of more systematically capturing small landslides than traditional approaches based on 2D imagery with manual landslide mapping.

- Landslides on surfaces with low or no vegetation cover are classically missed with 2D imagery processing due to the lack of texture or spectral change. In our study case, 75% of surface area was missed when considering a 2D inventory, corresponding to 60% of the total volume determined with the 3D inventory. Missing area both correspond to detection error (landslide fully missed) and delimitation error (uncertainty in contours). Our method also shows the ability to detect subsidence related to slip failure propagation and the initiation or displacement of translational and rotational large landslides, which cannot be detected with 2D imagery.

- As this method provides direct 3D measurement, landslide geometry properties such as volume, area, depth and their distribution can be explored. Our results are broadly consistent with the V-A relationship scaling parameters determined by Larsen et al. (2010) for soil landslides and Massey et al. (2020), with a scaling exponent of 1.17.

- No rollover is observed in the landslide area distribution down to 20 m², our conservative resolution limit, using the 3D landslide inventory. However, we demonstrate, for the first time, a size-based under-detection in landslide mapped from repeat 2D images, which in turn results in a rollover of the landslide source area distribution for the 2D inventory. This result lends credit to the hypothesis that the rollover systematically observed in landslide area distributions generated from 2D images is entirely or partially related to an under-detection of small landslides (Stark and Hovius, 2001).

Our 3D processing workflow is a first step towards harnessing the full potential of repeated 3D high resolution topographic surveys to automatically create complete and accurate landslide inventories. However, high density LiDAR flights are not always available in landslide-prone regions for which a 2D image-based approach remains the most suited approach. Nevertheless, we recommend to systematically perform a 3D-PcD approach where repeat LiDAR data exist. This is critically needed to improve landslide science and managing the cascade of hazards following large earthquakes or storm events, by automatically identifying landslide deposits, and subtle features such as subsidence developing around landslides missed in 2D inventories. Current bottlenecks to apply this workflow over larger scales, beyond the availability of high-quality 3D data itself, are the registration of pre- and post-EQ data when complex co-seismic deformation patterns occur, and limitations of the segmentation method in high landslide density areas. While airborne LiDAR is best suited to vegetated environments and
currently results in the best precision compared to aerial or spatial photogrammetry, the workflow operates for any kind of 3D data.

Appendix A: Table of the result of the sensitivity analyses to the workflow parameters: \( \text{reg} \), \( D_m \) and \( \text{SNR} \). Unit for the registration error \( \text{reg} \) and the minimum segmentation distance \( D_m \) is in meter and \( \text{SNR} \) has no unit.

<table>
<thead>
<tr>
<th>Workflow parameter</th>
<th>Value</th>
<th>( N_{LT} )</th>
<th>Landslide area distribution</th>
<th>Landslide volume distribution</th>
<th>V-A relationship</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \text{reg} )</td>
<td>0.2*</td>
<td>524</td>
<td>0.70 ± 0.12</td>
<td>-1.72 ± 0.04</td>
<td>0.99</td>
</tr>
<tr>
<td></td>
<td>0.3</td>
<td>329</td>
<td>0.50 ± 0.12</td>
<td>-1.64 ± 0.04</td>
<td>0.99</td>
</tr>
<tr>
<td></td>
<td>0.4</td>
<td>200</td>
<td>0.28 ± 0.27</td>
<td>-1.55 ± 0.09</td>
<td>0.96</td>
</tr>
<tr>
<td></td>
<td>0.5</td>
<td>234</td>
<td>0.11 ± 0.19</td>
<td>-1.49 ± 0.07</td>
<td>0.98</td>
</tr>
<tr>
<td>( D_m )</td>
<td>1.5</td>
<td>550</td>
<td>0.70 ± 0.12</td>
<td>-1.73 ± 0.04</td>
<td>0.99</td>
</tr>
<tr>
<td></td>
<td>2*</td>
<td>524</td>
<td>0.70 ± 0.12</td>
<td>-1.72 ± 0.04</td>
<td>0.99</td>
</tr>
<tr>
<td></td>
<td>3</td>
<td>443</td>
<td>0.61 ± 0.16</td>
<td>-1.68 ± 0.05</td>
<td>0.99</td>
</tr>
<tr>
<td></td>
<td>4</td>
<td>373</td>
<td>0.42 ± 0.18</td>
<td>-1.59 ± 0.06</td>
<td>0.98</td>
</tr>
<tr>
<td></td>
<td>6</td>
<td>259</td>
<td>0.13 ± 0.14</td>
<td>-1.45 ± 0.04</td>
<td>0.99</td>
</tr>
<tr>
<td>( \text{SNR} )</td>
<td>1.5*</td>
<td>524</td>
<td>0.69 ± 0.12</td>
<td>-1.72 ± 0.04</td>
<td>0.99</td>
</tr>
<tr>
<td></td>
<td>2</td>
<td>166</td>
<td>0.22 ± 0.14</td>
<td>-1.49 ± 0.04</td>
<td>0.99</td>
</tr>
</tbody>
</table>

*: reference case used in the study.

Code availability

The code producing the landslide inventory in this study is available as a jupyter notebook at https://github.com/Thomas-Brd/3D_landslide_detection, and is also archived in Zenodo: http://doi.org/10.5281/zenodo.4010806.

Data availability

The landslide source and deposit information supporting the findings of this paper can be found in Zenodo: 10.5281/zenodo.4558905

Supplement link

The supplement related to this article is available online at: .
Author contribution

D.L. and T.B. designed the landslide detection workflow. T.B. and all co-authors participated to the discussion, writing and reviewing of this paper. T.B produced the figures and the code.

Competing interests

The authors declare that they have no conflict of interest.

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