



1 **Regularity of transportation for cohesive bank-collapsed**
2 **materials**

3 Guosheng Duan^{1,3}, Haifei Liu^{2,3,*}

4 ¹Faculty of Geographical Science, Beijing Normal University, Beijing 100875, China.

5 ²Key Laboratory of Hydro-Sediment Science and River Training, the Ministry of Water Resources,
6 China Institute of Water Resources and Hydropower Research, Beijing 100048, China.

7 ³School of Environment, Key Laboratory of Water and Sediment Sciences of MOE,
8 Beijing Normal University, Beijing 100875, China.

9 * Correspondence: haifei.liu@bnu.edu.cn

10 **Abstract:** The transportation of bank-collapsed materials is a key issue among river
11 evolution processes. In this study, a series of flume experiments were conducted to
12 monitor riverbank collapse processes and to explore the regularity of transportation for
13 cohesive collapsed materials. The collapsed materials, both the bed and suspended
14 loads, that transformed from collapsed materials were intensively evaluated under
15 experimental conditions. The results showed that the collapsed materials contributed to
16 12 ~ 20% sedimentation in situ, 8 ~ 14% suspended loads and 70 ~ 80% bed loads. In
17 addition, the bed load motion efficiency coefficient (e_b), suspended load motion
18 efficiency coefficient (e_s) and sediment carrying capacity factor ($U^3/gR\omega$) were
19 introduced to describe the transportation of collapsed materials in terms of energy
20 dissipation. This research provides theoretical and practical benefits for predicting
21 channel evolution processes.

22 **Keywords:** riverbank, collapsed materials, transformation, cohesive

23 **1. Introduction**

24 Riverbank collapse, which occurs in alluvial streams worldwide, has caused a
25 series of social, economic and environmental problems (Simon et al., 2009, Rinaldi and
26 Nardi, 2013, Hackney et al., 2015). Moreover, collapsed materials are also a major
27 stream sediment source, directly influencing sediment concentration and riverbed
28 evolution processes in both local and downstream areas (Motta et al., 2014). Thus, more
29 research has concentrated on the mechanisms and channel evolution processes
30 associated with riverbank collapse in recent years (Patsinghasanee et al., 2017; Arai et
31 al., 2018; Deng et al., 2019; Lopez & Lanzoni, 2019; Masoodi et al., 2019; Yu et al.,
32 2020; Zhao et al., 2020).



33 Riverbank collapse processes are usually decomposed into two steps: bank toe
34 erosion and upper riverbank failure (Thorne & Tovey, 1981; Lawler et al., 1997; Simon
35 et al., 2000). For cohesive riverbanks, bank toe erosion occurred through entrainment
36 of aggregates because of the electrochemical forces existing among the fine particles
37 (Wood et al., 2001; Langendoen & Simon, 2008). The collapse patterns can be classified
38 as plane, arch and cantilever collapse based on the shape of the collapse plane (Darby
39 et al., 2000). The roles of various influencing factors, mainly vegetation (Simon &
40 Collison., 2002; Yu et al., 2020), soil properties (Parker et al., 2008; Masoodi et al.,
41 2017), bank shape (Baker, 1981; Simon & Rinaldi, 2006), hydraulic conditions
42 (Visconti et al., 2010; Chiang et al., 2011; Chen et al., 2017) and underground water
43 level (Casagli et al., 1999; Dapporto et al., 2001; Rinaldi et al., 2004), were also
44 evaluated in detail in riverbank collapse processes. Based on these achievements,
45 several bank erosion models were set up to predict cohesive riverbank collapse, of
46 which the bank toe erosion rate was obtained by the difference between flow shear
47 stress and soil shear strength, while riverbank stability was estimated by a stability
48 coefficient (F_s) of the ratio of driving force to resistance (Hook, 1980; Osman & Thorne,
49 1988; Simon et al., 2009; Clark & Wynn, 2007). As the models took into accounting
50 the influencing factors, they were widely used to quantify riverbank collapse and
51 simulate the channel evolution process in collapsed reaches.

52 Many researchers have combined bank erosion models with water-sediment
53 mathematical models to simulate channel evolution processes (Nagata et al., 2000;
54 Darby et al., 2002; Chen & Duan, 2006; Rinaldi et al., 2008; 2013; Xu et al., 2011;
55 Motta et al., 2012). It is known that some collapsed materials were transported by flow
56 current instantaneously after the riverbank collapsed, while others accumulated at the
57 bank toe. Evaluating the deposition and further movement of the accumulated materials
58 remains a key problem to be solved. In previous simulations, various assumptions were
59 established: (1) collapsed materials were transported immediately by the water current
60 (Darby et al., 2007; Rinaldi et al., 2008); (2) 50% of the collapsed materials
61 accumulated at bank toe and then participated in riverbed evolution process (Xia et al.,
62 2016; Deng et al., 2019); (3) collapsed material particles that are coarser than 0.062 mm
63 would distribute uniformly across the bed area between bank toe and the boundary of
64 the near-bank sediment routing segment, from a distance equal to two bank heights
65 (Rijn and Leo, 1985); (4) the volume of collapsed materials accumulated at bank toe
66 was decided by sediment carrying capacity which equals the maximal sediment



67 concentration for nonequilibrium transportation of the suspended load (Jia et al., 2010;
68 Duan et al., 2018; Shu et al., 2019). Although a number of relatively accurate simulation
69 results were obtained based on these assumptions, there has been no direct evidence to
70 expound the distribution and transportation of collapsed materials in detail. Certain
71 advantages have been provided through water flume experiments, such as the
72 distribution of cohesive collapsed materials along noncohesive riverbeds, the mixture
73 of collapsed and bed sediments, and the relationship between sediment distribution and
74 velocities (Yu et al., 2013; 2014; 2016). These results mainly focused on qualitatively
75 describing the phenomenon. However, the quantity of sediment transportation was not
76 involved, especially in collapsed materials. Thus, one object of this study is to quantify
77 the transportation of collapsed materials, which is a key issue when predicting the
78 riverbed evolution process.

79 In addition, collapsed materials that accumulate at the bank toe will initiate first
80 and then transform into bed and suspended load in the following river evolution
81 processes. From the point of energy dissipation, the energy of bed load motion comes
82 from water potential energy, while sediment suspension energy comes from the
83 turbulent kinetic energy of water flow (Huang et al., 2005). The transportation of
84 accumulated sediments depends not only on the relationship between sediment gravity
85 and current shear stress but also on the ratio between the energy expended in motion
86 and the water potential energy available (Qian & Wan, 1983). To describe the
87 transportation of collapsed materials in detail, the energy dissipation of sediment
88 transportation was investigated in this study.

89 Overall, a series of flume experiments were conducted to simulate cohesive
90 riverbank collapse processes and characterize the transportation of collapsed materials.
91 The major objectives of this study are as follows: (1) to quantify the sediment
92 transformation due to riverbank collapse, especially the collapsed materials
93 transforming into bed and suspended loads, and (2) to analyze the transportation of
94 collapsed materials in terms of energy dissipation.

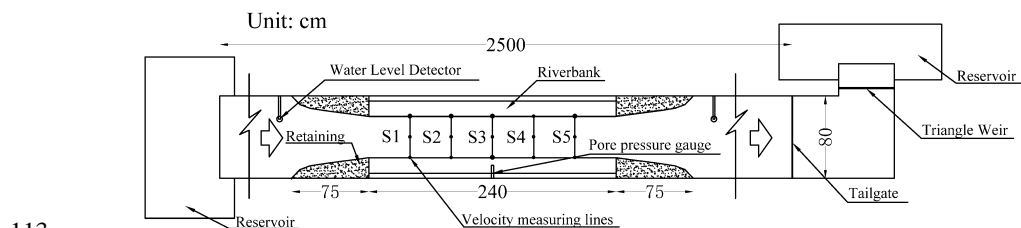
95 **2. Experimental Methods**

96 **2.1 Experimental setup and materials**

97 Experiments were performed in a 25 m long rectangular flume with a width and
98 depth of 0.8 m (Figure 1), located at the Key Laboratory of Water and Sediment Science

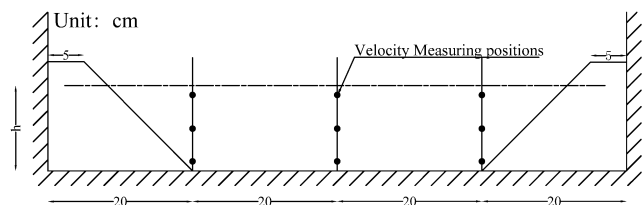


99 of MOE (Ministry of Education), Beijing Normal University, China. The experiments
100 consisted of four groups with different bank slopes (45° , 60° , 75° , 90°). For each group,
101 a 2.4 m long, 0.15 m deep symmetric trapezoidal channel with a 0.4 m bottom width
102 was built within the flume, while the width of the channel top was determined by bank
103 slopes, as listed in Table 1. Riverbanks of both sides were made of the selected materials
104 collected from a natural bank at the Dengkou reach of the Yellow River (Shu et al.,
105 2019). The gravel was laid up and downstream of the recreated banks to enable constant
106 boundary conditions (Figure 1). Five typical sections (S1-S5) were also set up at 40 cm
107 intervals to monitor the relevant parameters, and three measuring lines were set in each
108 section to monitor the velocities (Figure 1). Multiple locations within measuring lines
109 of typical sections were selected to ensure the accuracy of velocities by using a
110 propeller (Figure 2). Figure 3 shows the top view of the actual experimental setup, with
111 water level gauges and pore-water pressure gauges fitted in the flume to monitor the
112 water level and pore water pressure, respectively.



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Figure 1. Schematic diagram of the test flume (not to scale) (Unit: cm).



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Figure 2. Example of one cross section and corresponding monitoring positions for the velocity.

118 Before each experiment, the particle size distribution (Figure 4) and physical
119 properties of experimental materials taken from typical sections were tested. At the
120 preparatory stage, the tailgate was kept closed, and the water level rose slowly to the
121 designed level. Then, the initiation of experiment began by adjusting the designed flow
122 conditions (Table 1). Water samples containing materials were taken every three
123 minutes at Sections S1, S3, S5 and at the tailgate to measure the sediment concentration.



124 The experiment was considered completed when no more riverbank materials were
 125 removed or eroded.

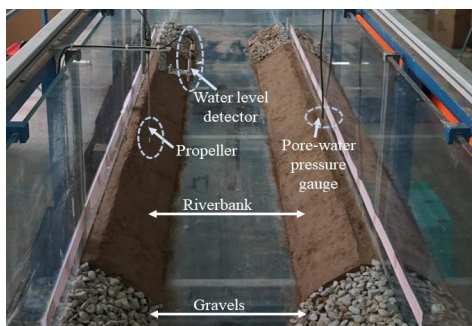


Figure 3. Actual experimental setup with bank slope 45°.

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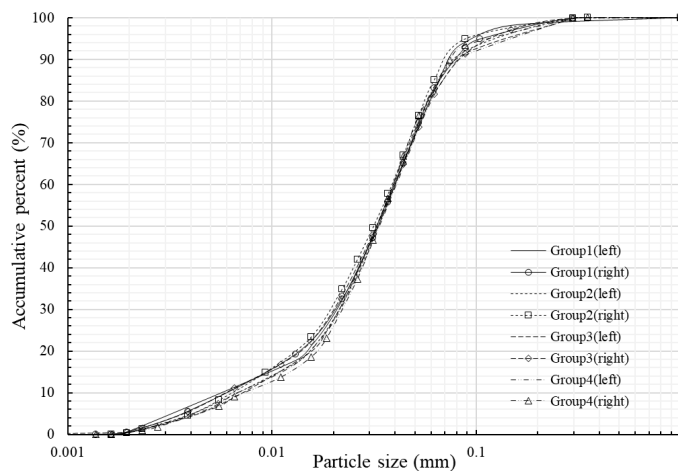


Figure 4. Particle size distribution of the materials.

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Table 1. Configurations and bank morphology details.

Group	Slope degree (°)	Bank morphology (left and right)			Flux (L/s)	Water discharge time (min)	Water level (cm)
		Bank top width (cm)	Bank height (cm)	Bank toe width (cm)			
No.1	45	5	15	20	38	30	11.5
					44	30	12.7
No.2	60	11.35	15	20	29.4	30	11
					40.9	30	12.75
No.3	75	16	15	20	27.8	30	10
					36.5	30	13.15
No.4	90	20	15	20	26	30	9.25
					33.8	30	12



132 **3. Results and Discussion**

133 **3.1 Results**

134 **3.1.1 Quantity of sediment transportation due to riverbank collapse**

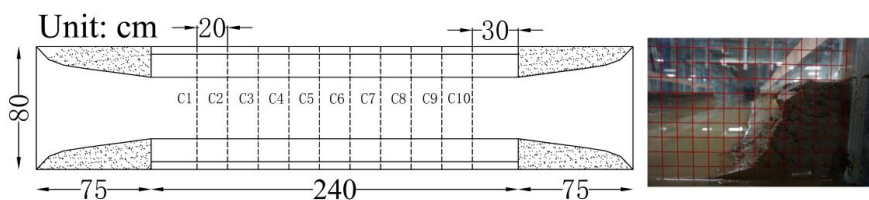
135 After collapsed materials entered the channel, the incipient sediments were then
 136 further activated and transported as bed and suspended loads, while the remaining
 137 sediments accumulated at the toe of the bank. In summary, collapsed materials will be
 138 transported in three patterns: accumulated sand, bed loads and suspended loads.

139 **(1) Quantity of collapsed materials**

140 The amount of collapsed materials was obtained by comparing the topography of
 141 the riverbank before and after the experiment. Ten sections (C1, C2, ..., C10) among
 142 riverbanks with 20 cm intervals along the flow direction were selected to measure the
 143 riverbank shape by using a glass plate with gridlines (Figure 5). Figure 8 shows the
 144 collapsed areas of the selected sections with a riverbank slope of 45°. Based on the unit
 145 weight of materials listed in Table 2, the quantities of the collapsed materials can be
 146 obtained in Table 3.

147 **Table 2.** Physical properties of the material tested for each configuration.

Group	Soil position	Moisture content (%)	Unit weight (g/cm ³)	Cohesion (kPa)	Friction angle (°)
No.1	Left bank	16.11	1.63	14.77	19.46
	Right bank	16.51	1.85	14.45	19.19
No.2	Left bank	16.01	1.81	14.77	19.46
	Right bank	16.18	1.77	14.45	19.19
No.3	Left bank	16.86	1.81	13.66	18.54
	Right bank	16.39	1.83	12.93	17.92
No.4	Left bank	17.42	1.81	13.77	18.63
	Right bank	18.04	1.68	15.37	19.96

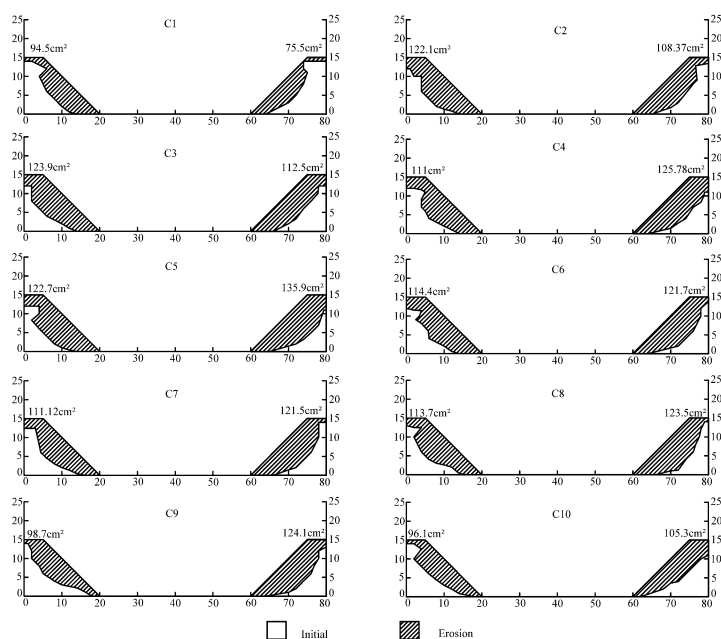


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Figure 5. The measurement of riverbank shape by using a glass plate with gridlines.



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Figure 6. Collapsed areas of selected sections with riverbank slope 45°.

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Table 3. Quantity of collapsed materials.

Group	Slope gradient (°)	Collapse amount (kg)
No.1	45	87.16
No.2	60	41.58
No.3	75	62.45
No.4	90	82.43

153 **(2) Quantity of collapsed sediments accumulated at the toe of the bank**

154 It is generally believed that the collapsed materials entering the channel can be
 155 treated as single-particle sediments, and the incipient motion particle size was
 156 calculated by the following equation (Qian and Wan, 1983):

$$157 \quad \frac{U_i}{\sqrt{gD}} = \sqrt{\frac{\gamma_s - \gamma}{\gamma} \left(6.25 + 41.6 \frac{h}{Ha} \right) + \left(111 + 740 \frac{h}{Ha} \right) \frac{Ha \delta_0}{D^2}} \quad (1)$$

158 where Ha is the atmospheric pressure expressed in terms of water column height, $Ha =$
 159 10 m; δ_0 is the thickness of a water molecule, $\delta_0 = 3.0 \times 10^{-8}$ cm; γ_s is the unit weight
 160 of sediment, $\gamma_s = 17542$ Nm⁻³; γ is the unit weight of water, $\gamma = 9800$ Nm⁻³; g is the
 161 gravitational acceleration, $g = 9.8$ ms⁻²; D is the sediment particle size, m; U_i is the



162 velocity for incipient sediment motion, ms^{-1} ; U is the velocity, ms^{-1} (for this study $U_i =$
 163 U), and h is the water depth, m.

164 Table 4 presents the percentage of accumulated sediments under different
 165 experimental conditions. It should be noted that particles between the lower and upper
 166 limits of incipient motion particle size could be incipient, whereas others were regarded
 167 as the accumulated sediments.

168 **Table 4.** Percentage of accumulated sediments under different experimental conditions.

Group	Slope gradient (°)	Flow discharge (L/s)	Average water level (cm)	Average flow rate (m/s)	Incipience motion particle size (lower limits) (μm)	Incipience motion particle size (upper limits) (mm)	Incipience motion percentage (%)	Accumulated sediment percentage (%)
No.1	45	38.00	11.50	0.61	9.48	3.40	88.06	11.94
		44.00	12.70	0.71	9.28	3.46	91.06	8.94
No.2	60	29.40	11.00	0.51	15.00	2.36	79.81	20.19
		40.90	12.75	0.59	10.40	3.12	82.91	17.09
No.3	75	27.80	10.00	0.57	11.00	3.03	85.56	14.44
		36.50	11.75	0.65	8.30	3.89	86.96	13.04
No.4	90	26.00	9.25	0.54	12.00	2.73	84.48	15.52
		33.80	12.00	0.59	10.19	3.17	87.24	12.76

169 **(3) Quantity of bed and suspended loads transformed from collapsed materials**

170 **Table 5.** The critical particle size of the collapsed riverbank.

Group	Bank slope (°)	Flow rate (L/s)	Critical particle size (mm)
No.1	45	38	0.018
		44	0.016
No.2	60	29.4	0.020
		40.9	0.018
No.3	75	27.8	0.018
		36.5	0.016
No.4	90	26	0.018
		33.8	0.016

171 In sediment-laden flow, coarse particles are usually transported as bed loads, while
 172 fine particles are transported as suspended loads. Although there were mutual
 173 transformations between these two in the transport processes, the quantities of bed and
 174 suspended loads transported by the water flow remained roughly the same under certain
 175 flow conditions. Thus, a critical particle size was introduced to divide the bed and
 176 suspended loads, with particles larger than the critical particle size were arranged as
 177 bed loads; otherwise, they were arranged as suspended loads. The method described in



178 detail in the literature (Shu et al., 2019) was adopted to obtain the critical particle size,
179 as shown in Table 5.

180 Based on the bank material particle size distribution in Figure 4, the percentage of
181 bed and suspended loads for each group can be obtained (Table 6).

182 **Table 6.** Mass percentage of sediment fractions.

Group	Bank slope (°)	Flow rate (L/s)	Incipient motion percentage (%)	Suspended load percentage (%)	Bed load percentage (%)
No.1	45	38	11.94	13.56	74.50
		44	8.94	15.26	75.80
No.2	60	29.4	20.19	7.88	71.93
		40.9	17.09	13.25	69.66
No.3	75	27.8	14.44	10.56	75
		36.5	13.04	11.3	75.66
No.4	90	26	15.52	9.39	75.09
		33.8	12.76	7.94	79.30

183 3.1.2 The transportation of collapsed materials in terms of energy dissipation

184 In this study, the bed load motion efficiency coefficient (e_b) and suspended load
185 motion efficiency coefficient (e_s) were applied to describe the transportation of collapsed
186 materials. Based on previous studies, e_b represents the transformation efficiency from
187 the water potential energy into bedload motion (Bagnold, 1966), while e_s represents the
188 transformation efficiency from turbulent kinetic energy into suspended load motion (Shu
189 et al., 2007). The sediment carrying capacity equation can be expressed as the following
190 (Qian & Wan, 1983):

$$191 S_* = k \left(U^3 / g R \omega \right)^m,$$

192 where S_* is the sediment carrying capacity, m^3s^{-1} ; k and m are parameters; U is the
193 velocity, ms^{-1} ; g is the gravitational acceleration, ms^{-2} ; R is the hydraulic radius, m; and
194 ω is the sediment settling velocity, m/s. The sediment carrying capacity factor ($U^3 g^{-1} R^{-1} \omega^{-1}$)
195 can be regarded as the ratio of $U^2 g^{-1} R^{-1}$ to ωU^{-1} , which represents the turbulence
196 intensity and action of effective gravity, respectively. For these three parameters
197 containing all kinds of energy factors, it is reasonable to study the transportation of the
198 collapsed materials by building the relationship between e_b and $U^3 g^{-1} R^{-1} \omega^{-1}$ and between
199 e_s and $U^3 g^{-1} R^{-1} \omega^{-1}$. The experimental data used were collected at two-minute intervals
200 in Section S3 after riverbank collapse occurred.



201 **(1) The relationship between e_b and $U^3 g^{-1} R^{-1} \omega^{-1}$**

202 The bedload motion efficiency coefficient (e_b) can be obtained by the following
 203 equations (Bagnold, 1966):

204
$$e_b = (u_* - u_{*c}) \left\{ 1 - \left[5.75 u_* \lg(0.4h/mD) + \omega \right] / U_L \right\} / u_* \quad (2)$$

205
$$m = K \left(\frac{u_*}{u_{*c}} \right)^{0.6} \quad (3)$$

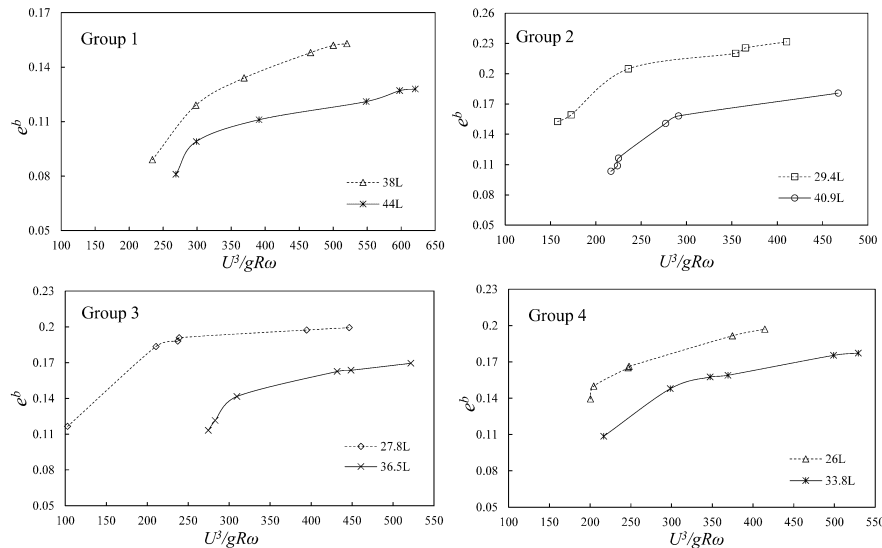
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$$\omega = \left[(13.95\nu/D)^2 + 1.09(\gamma_s - \gamma)gD/\gamma \right]^{1/2} - 13.95\nu/D \quad (4)$$

207
$$u_* = \sqrt{gRJ} \quad (5)$$

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$$u_{*c} = (\tau_c/\rho)^{1/2} \quad (6)$$

209 where u_* is frictional velocity, ms^{-1} ; U_L is mean vertical velocity at the location of 0.4
 210 h, m/s; h is the water depth, m; D is grain diameter, m; K is a constant coefficient
 211 ($K=1.4 \sim 2.8$); u_{*c} is critical shear velocity, m/s; γ_s is sediment unit weight, Nm^{-3} ; γ is
 212 water unit weight, Nm^{-3} ; ν is motion viscous coefficient, m^2s^{-1} , and $\nu = 1.31 \times 10^{-6} \text{m}^2\text{s}^{-1}$;
 213 J is hydraulic gradient; τ_c is flow shear stress, Nm^{-2} ; and ρ is water density, kgm^{-3} .

214 The relationships between e_b and $U^3 g^{-1} R^{-1} \omega^{-1}$ for different groups are shown in
 215 Figure 7.



216
 217 **Figure 7.** Relationship between e_b and $U^3/gR\omega$.

218 The range of e_b was 0.11 ~ 0.25, which was similar to Bagnold's result of 0.11 ~
 219 0.15, and e_b had a noticeable positive correlation relationship with $U^3 g^{-1} R^{-1} \omega^{-1}$ (Bagnold,
 220 1966). For each curve, e_b first quickly increased and then stabilized because after the



221 riverbank collapsed, the collapsed materials first accumulated at the toe of the bank and
 222 then transformed into bed loads. With increasing sediment carrying capacity, the energy
 223 of bed load motion increases. While the river gradually transferred from the
 224 nonequilibrium state to the equilibrium state, e_b tended to be stable.

225 In each group, the e_b value of the lower flow was larger than that of the higher
 226 flow, because as the flow increased, a portion of the bed load would transform into
 227 suspended load. Additionally, part of the energy for the bed load motion would convert
 228 into the particles' potential energy with the change of particles' position.

229 **(2) The relationship between e^s and $U^3g^{-1}R^{-1}\omega^{-1}$**

230 The suspended load motion efficiency coefficient (e_s) can be obtained by the
 231 following (Shu et al., 2008):

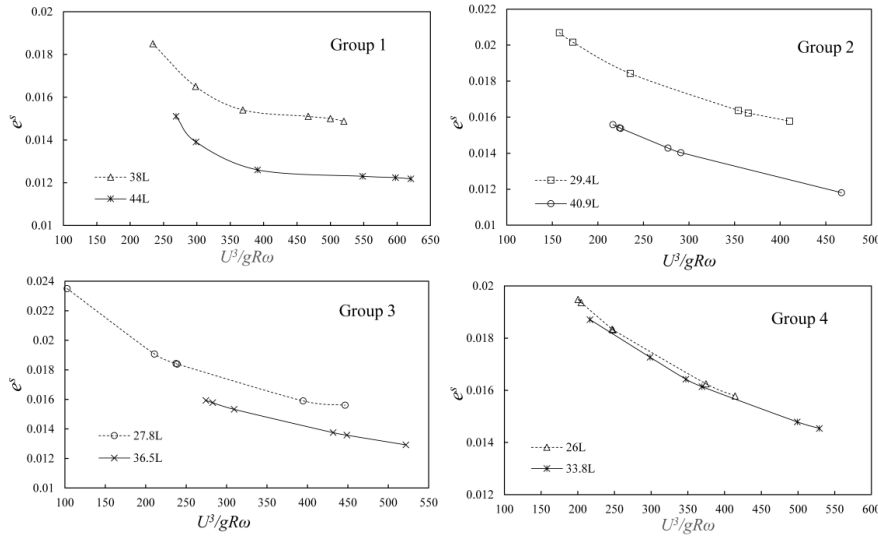
$$232 \quad e_s = p \cdot \frac{[\lg(\mu_r + 0.1)]^N}{\kappa^2 k_t} \left(\frac{f_m}{8}\right)^{\frac{1}{2}} \cdot \left[\frac{1}{\kappa^2} \left(\frac{f_m}{8}\right)^{\frac{3}{2}} \frac{\gamma_m}{\gamma_s - \gamma_m} \frac{U^3}{gR\omega} \right]^{N-1} \quad (7)$$

$$233 \quad k_t = 1 - 2\mu_r k_d U / \tau_c h \quad (8)$$

$$234 \quad f_m = 0.11\alpha \left(\frac{k_s}{4R} + \frac{68}{R_{em}} \right)^{0.25} \quad (9)$$

$$235 \quad R_{em} = \frac{u_* D}{\nu} = \frac{\sqrt{ghJD}}{\nu} \quad (10)$$

236 where μ_r is the relative dynamic viscosity coefficient, $\mu_r = 1 + 2.5S_v$; S_v is the volume
 237 sediment content; κ is the Karman constant, $\kappa=0.4$, $p=0.3551$, $N=0.72$, k_t is the turbulent
 238 kinetic energy conversion efficiency; $k_d U$ is the vertical maximum velocity, m/s; f_m
 239 is the drag coefficient of sediment laden flow; α is the reduced drag coefficient, which is
 240 smaller than 1; k_s is the riverbed roughness coefficient, $k_s=2D$; and R_{em} is the muddy
 241 water Reynolds number.



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Figure 8. Relationship between e_s and $U^3/gR\omega$.

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The range of e_s is 0.0129 ~ 0.0235, which was slightly different from Bagnold's result of 0.023 ~ 0.046 (Bagnold, 1966), but the values were still in the range of 0.00004–0.20 presented by Qian & Wan (1965). For each curve, e_s had a noticeably negative correlation relationship with $U^3g^{-1}R^{-1}\omega^{-1}$. After the riverbank collapsed, the river would transfer from a nonequilibrium state to equilibrium, and the suspended load concentration would increase compared with that of the noncollapse. However, sediment suspension energy decreased because of the drag reduction of suspended sediments provided by Zhang (1963). Moreover, in each group, e_s of the lower flow charge is larger than that of the higher flow, as when the flow charge increased, more bed loads would transform into suspended loads, with the drag reduction of suspended sediments (e_s decreased).

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3.2 Discussion

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In this study, riverbanks were built on both sides of the water flume, which was different from previous correlated studies (Yu et al., 2013; Shu et al., 2019; Zhao et al., 2020). The similar channel shape and on-site materials made this study more scientific for monitoring riverbank collapse processes. The quantities of the collapsed materials, bed and suspended loads obtained by the critical particle size method presented a good reference to predict the channel evolution process. The bed load motion efficiency coefficient (e_b), suspended load motion efficiency coefficient (e_s) and sediment carrying



263 capacity factor ($U^3 g^{-1} R^{-1} \omega^{-1}$) were used to describe the transportation of collapsed
264 materials, which differed from previous literature. Thus, this study can be considered a
265 valuable attempt to scientifically describe the transportation of collapsed materials.

266 There are still limitations that need to be addressed within future research. First,
267 the quantity of the collapsed materials, bed and suspended loads in this study were
268 obtained under specific flow conditions. For the complicity of natural rivers, more
269 bank shapes, angles and flow conditions should be considered. Second, although the
270 law of energy dissipation is a promising approach to describe the transportation of
271 collapsed materials, studies of sediment transportation in terms of energy dissipation
272 are usually qualitative. More accurate measurement tools need to be explored and
273 applied to obtain the energy consumed by the bed and suspended loads. Finally, both
274 quantities and energy dissipation should be studied comprehensively to analyze the
275 transportation of collapsed materials and benefit channel evolution prediction.

276 4. Conclusions

277 A series of experiments with a constructed riverbank on both sides were conducted
278 to quantify the transportation of the collapsed materials. Transportation was also
279 studied from the point of energy dissipation. The findings can be concluded as follows:

280 (1) After the riverbank collapsed, the three main processes of the collapsed
281 materials were deposited on-site and transported as bed and suspended load. In terms
282 of the quantities, the percentages of these three were 12 ~ 20%, 70 ~ 80% and 8 ~ 14%,
283 respectively.

284 (2) In the transportation of the collapsed materials, the ranges of e_b and e_s were
285 0.11 ~ 0.25 and 0.0129 ~ 0.0235, respectively. The drag reduction of the suspended
286 loads was verified by the relationships between e_b , e_s and $U^3 g^{-1} R^{-1} \omega^{-1}$.

287 (3) In terms of energy dissipation, the transportation of collapsed materials follows
288 the law of river transition from a nonequilibrium to an equilibrium state. After the
289 riverbank collapsed, the collapsed materials first transformed into bed loads. With the
290 increase in the sediment carrying factor ($U^3 g^{-1} R^{-1} \omega^{-1}$) toward the river equilibrium state,
291 more bed load sediment transformed into suspended loads. At the same time, part of
292 the energy for bed load motion would convert into the particles' potential energy.

293 The results can help reveal the mechanisms of channel bend evolution and provide
294 valuable theoretical and practical benefits to river channel embankments.



295 **Data availability**

296 All raw data can be provided by the corresponding authors upon request.

297 **Author contributions**

298 GD performed the measurements and wrote the manuscript draft; HL reviewed
299 and edited the manuscript.

300 **Competing interests**

301 The authors declare that they have no conflict of interest.

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