Toward a general calibration of the Swiss plate geophone system for fractional bedload transport

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Abstract. Substantial uncertainties in bedload transport predictions in steep streams have encouraged intensive efforts to develop surrogate monitoring technologies. One such system, the Swiss plate geophone (SPG), has been deployed and calibrated in numerous steep water courses, mainly in the Alps. Calibration relationships linking the signal recorded by the SPG system to the transported bedload can vary substantially between different monitoring stations, likely due to site-specific factors such as flow velocity and bed roughness. Furthermore, recent controlled experiments on the SPG system have shown that site-specific calibration relationships can be biased by elastic waves resulting from impacts occurring outside the plate boundaries. Motivated by these findings, we present here a hybrid calibration procedure derived from flume experiments and an extensive dataset of 308 calibration measurements from four different SPG field monitoring stations. Our main goal is to investigate the feasibility of a general, site-independent calibration procedure for inferring fractional bedload transport from the SPG signal. First, we use flume experiments to show that sediment size classes can be distinguished more accurately using a combination of vibrational frequency and amplitude information than by using amplitude information alone. Second, we apply this amplitude-frequency method to field measurements to derive general calibration coefficients for ten different grain-size fractions. The amplitude-frequency method results in more homogeneous signal responses across all sites and significantly improves the accuracy of fractional sediment flux and grain-size estimates. We attribute the remaining site-to-site discrepancies to large differences in flow velocity, and discuss further factors that may influence the accuracy of these bedload estimates.

1 Introduction

Flood events across Europe in the summer of 2021 have illustrated the threat of flood-related hazards like bedload transport to human life and infrastructure, especially in small and steep mountainous catchments (Badoux et al., 2014; Blöschl et al., 2020). Understanding sediment transport processes is also essential for efforts to return rivers to their near-natural state by restoring their continuity and re-establishing balanced sediment budgets (e.g. Brouwer and Sheremet, 2017; Pauli et al., 2018; Logar et al., 2019; Rachelly et al., 2021). However, monitoring and predicting bedload transport still represents a considerable challenge because of its large spatio-temporal variability (e.g. Mühlhofer, 1933; Einstein, 1937; Reid et al., 1985; Rickenmann, 2018; Ancey, 2020). This is especially true for steep streams, because they are poorly described by traditional bedload transport equations, which have mainly been developed for lower-gradient channels (e.g. Schneider et al.,

2016). Predicting sediment transport in steep channels is challenging, notably due to the presence of macro-roughness elements affecting both the flow resistance and the flow energy (e.g. Manga and Kirchner, 2000; Yager et al., 2007, 2012; Bathurst, 2007; Nitsche et al., 2011; Rickenmann and Recking, 2011; Prancevic and Lamb, 2015). It is further complicated by a sediment supply that varies in both space and time, due in part to cycles of building and breaking of an armoring layer at the riverbed (e.g. Church et al., 1998; Dhont and Ancey, 2018; Rickenmann, 2020; Piantini et al., 2021).

Bedload transport equations established for lower-gradient streams typically result in multiple order-of-magnitude errors when applied to steep streams, motivating the development of new indirect monitoring techniques for steep mountain channels (e.g. Gray et al., 2010; Rickenmann, 2017). Indirect monitoring techniques provide large spatial coverage of river transects at high temporal resolution, reduce personal risk related to in-stream sampling, and enable consistent data collection at widely varying flow conditions, including during flooding events (e.g. Gray et al., 2010; Rickenmann, 2017; Geay et al., 2020; Bakker et al., 2020; Choi et al., 2020; Le Guern et al., 2021). The drawback of these monitoring technologies is that in order to provide quantitative measurements, they often require intensive calibration through direct bedload sampling with retention basins (Rickenmann and McArdell, 2008), slot samplers (e.g. Habersack et al., 2017; Halfi et al., 2020) or mobile bag samplers (e.g. Bunte et al., 2004; Dell'Agnese et al., 2014; Hilldale et al., 2015; Mao et al., 2016; Kreisler et al., 2017; Nicollier et al., 2021).

Among indirect monitoring techniques, the Swiss plate geophone (SPG) system has been deployed and tested in more than 20 steep gravel-bed streams and rivers, mostly in the European Alps (Rickenmann, 2017). Typically, linear or power-law calibration relationships have been developed between measured signal properties and bedload transport characteristics (Rickenmann et al., 2014; Wyss et al. 2016a; Kreisler et al., 2017; Kuhnle et al., 2017). Such calibration equations permit absolute quantification of bedload fluxes, their variability in time and space (i.e. across a river section), estimates of bedload grain-size distribution, and the detection of the start and end of bedload transport. However, these equations require a calibration procedure against independent bedload transport measurements at each individual field site, because until now we have lacked generally applicable signal-to-bedload calibration equations that are valid across field settings. Although similarities between calibration relationships at various field sites are encouraging, it is not well understood why the linear calibration coefficients for total mass flux can vary by about a factor of 20 among individual samples from different sites, or by about a factor of six among the mean values from different sites (Rickenmann et al., 2014; Rickenmann and Fritschi, 2017). Given the substantial field effort required for calibration campaigns, a generally applicable calibration equation would represent a significant advance.

Numerous studies have reported successful calibration of impact plate systems in laboratory flumes (e.g. Bogen and Møen, 2003; Krein et al., 2008; Tsakiris et al., 2014; Mao et al., 2016; Wyss et al., 2016b,c; Kuhnle et al., 2017; Chen et al., 2022), although transferring these flume-based calibrations to the field remains challenging. Nonetheless, controlled flume experiments are valuable because they allow to systematically explore relationships between the recorded signal, the transport rates of different sediment size fractions, and the hydraulic conditions. For example, the experiments of Wyss et al. (2016b) showed that higher flow velocities induce a weaker SPG signal response per unit of transported sediment. More recent controlled experiments have highlighted another important site-dependent factor influencing the SPG signal response, namely the grain-size distribution (GSD) of the transported bedload (Nicollier et al., 2021), where coarser grain mixtures were shown to yield a stronger signal response per unit bedload weight.

Subsequent impact tests and flume experiments showed that this grain-size dependence arises because the impacts plates are insufficiently isolated from their surroundings (Antoniazza et al., 2020; Nicollier et al., 2022). The elastic wave generated by an impact on or near a plate was found to propagate over several plate lengths, contaminating the signals recorded by neighboring sensors within a multiple plate array. Nicollier et al. (2022) introduced the notion of "apparent packets" (in opposition to "real" packets) to define the portions of the recorded signal that were generated by such extraneous particle impacts.

The main goal of this contribution is to examine the feasibility of a general, site-independent signal conversion procedure for fractional bedload flux estimates. We follow a comprehensive hybrid signal conversion approach that encompasses a set of full-scale controlled flume experiments conducted at an outdoor flume facility, as well as 308 field calibration measurements performed with direct sampling methods at four different bedload monitoring stations in Switzerland between 2009 and 2020. We present the amplitude-frequency (AF) method, aiming to reduce the bias introduced by apparent packets in the relationship between the signal characteristics and the particle size. Finally, we compare the performance of this novel AF method against the amplitude-histogram (AH) method developed by Wyss et al. (2016a) for both fractional and total bedload flux estimates.

2   Methods

2.1   The SPG system

The Swiss plate geophone (SPG) consists of a geophone sensor fixed under a steel plate of standard dimensions 492 mm x 358 mm x 15 mm (Fig. 1a; Rickenmann, 2017). The geophone (GS-20DX by Geospace technologies; www.geospace.com) uses a magnet moving inside an inertial coil (floating on springs) as an inductive element. The voltage induced by the moving magnet is directly proportional to its vertical velocity resulting from particle impacts on the plate. The SPG system can detect bedload particles with a diameter down to 10 mm (Rickenmann et al., 2014, 2020; Wyss et al., 2016a). Typically, a SPG array includes several plates next to each other, acoustically isolated by elastomer elements and covering the river cross-section. The array is either embedded in a concrete sill or fixed at the downstream face of a check dam. A detailed description of the SPG system can be found in Rickenmann et al. (2014). For all the calibration measurements and the outdoor flume experiments analyzed in this study, ranging from a few seconds to one hour, the full raw signal 10 kHz geophone signal was recorded (Fig. 1b). In the normal operational recording mode with continuous data storage, due to data storage limitations, field stations usually do not continuously record the full raw signal, but only preprocessed summary values (Rickenmann et al., 2014).
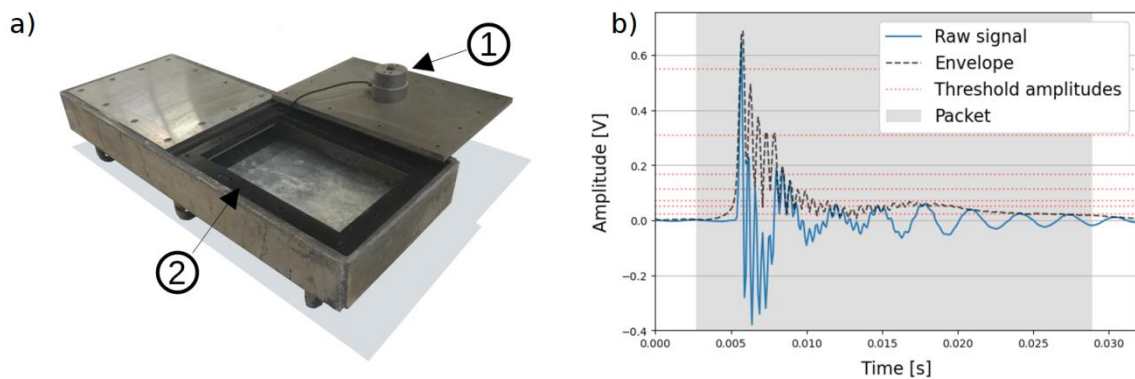

Figure 1: (a) Swiss plate geophone (SPG) system before installation (see Fig. 3). Each plate is equipped with a uniaxial geophone sensor fixed in a watertight aluminum box (1) attached to the underside of the plate. The plates are acoustically isolated from each other by elastomer elements (2). (b) Example of a packet (grey area) detected by the SPG system. A packet begins 20 time steps (i.e., 2 ms) before the signal envelope crosses the lowest amplitude threshold of 0.0216 V and ends 20 time steps after the last crossing of the lowest amplitude threshold (see Sect. 2.4).

2.2 Field calibration measurements

To test the AF and AH methods, this study uses 308 calibration measurements from four Swiss bedload monitoring stations equipped with the SPG system (Fig. 2; Table 1). Field calibration samples were collected at the Albula, Navisence and Avançon de Nant stations, and extensive calibration efforts have been undertaken at the fourth field station, the Erlenbach, since 2009 (Rickenmann et al., 2012). The Erlenbach offers an interesting comparison with the other sites due to different channel and flow characteristics upstream of the SPG plates. These are the only field sites equipped with an SPG system at which the full raw geophone signal has been recorded during calibration measurements. Field calibrations carried out at the four sites consisted of the following steps: (i) direct bedload sampling downstream of an impact plate using either crane-mounted net samplers adapted from Bunte traps (Bunte et al., 2004; Dell'Agnese et al., 2014; Nicollier et al., 2019; Fig. 2a, b), automated basket samplers (Rickenmann et al., 2012; Fig. 2d) or manual basket samplers (Fig. 2c; Antoniazza et al., 2022), (ii) synchronous recording of the raw geophone signal, (iii) sieving and weighing of bedload samples using ten sieve classes (see Sect. 2.4), and (iv) comparing the fractional bedload mass of each sample to the geophone signal to derive the corresponding calibration coefficients. A more detailed description of the sampling procedure is reported in Supporting Information S1, including the mesh sizes used for bedload sampling. For the analysis, only particles larger than 9.5 mm were considered, being close to the SPG detection threshold. Streamflow information was derived from various stage sensors (Table 1). Flow velocity V_w was introduced by Wyss et al. (2016c) as a possible governing parameter affecting the number of particles detected by the SPG system. Unfortunately, due to the lack of continuous flow velocity measurements at the Albula and Navisence sites, we were not able to account for the effect of the flow velocity in the signal conversion procedure described in the present study.
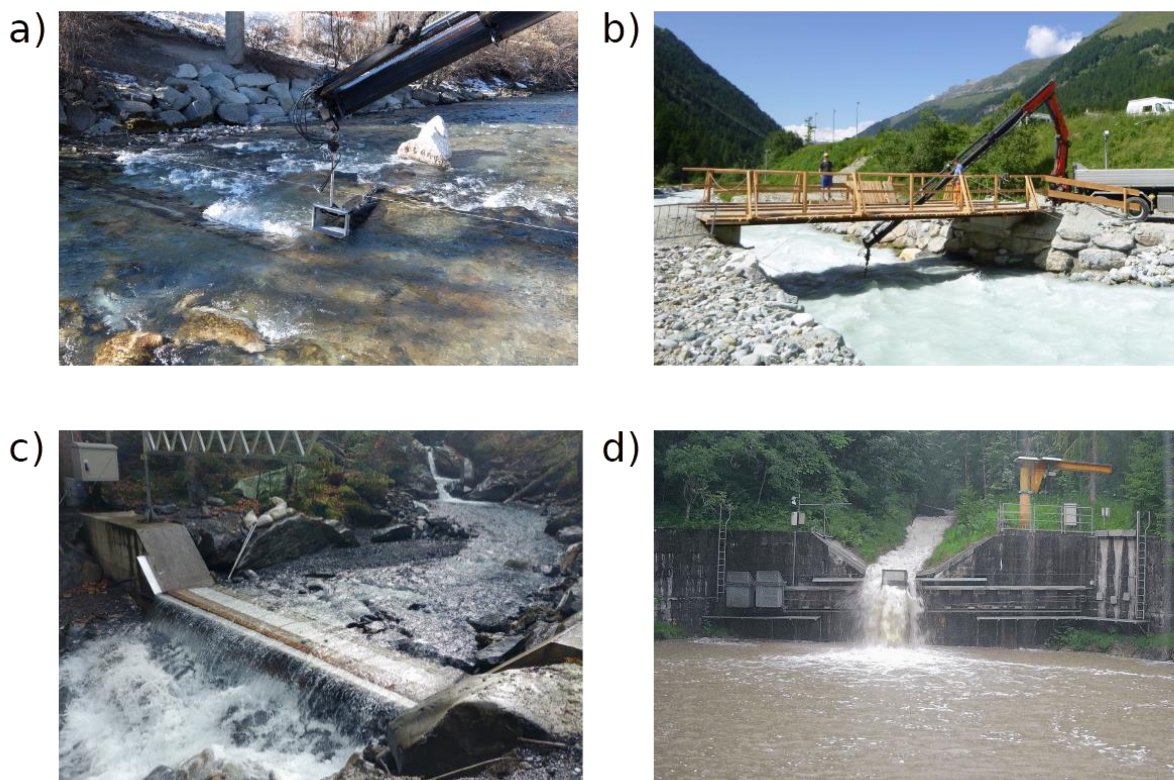
Figure 2: The four Swiss bedload monitoring stations at which raw Swiss plate geophone signals have been recorded during calibration measurements. The stations are installed at the following streams: a) Albula, b) Navisence, c) Avançon de Nant and d) Erlenbach. Pictures a) and c) were taken during low-flow conditions. Pictures b) and d) show calibration measurements with the crane-mounted net sampler and the automated basket sampler, respectively, at high flows.

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Table 1: Channel and flow characteristics based on *in situ* measurements during the calibration campaigns at the four field sites.
The year of the field calibration campaigns, the sampling technique and the number of collected samples are also indicated.

Field site	Location (canton)	Bed slope [%] [a]	Mean flow velocity V_f [m s^{-1}] [b]	No. of plates	Year	Sampling technique	No. of samples
Albula [c]	Tiefencastel (Grisons)	0.7	2.6	30	2018	crane-mounted net sampler	51
Navisence [c]	Zinal (Valais)	3	3.2	12	2019	crane-mounted net sampler	80
Avançon de Nant [d]	Les Plans-sur-Bex (Vaud)	4	1.3	10	2019/2020	manual basket sampler	55
Erlenbach [e]	Alpthal (Schwyz)	16	5.0	2	Since 2009	automatic basket sampler	122

[a] Gradient measured upstream of the SPG plates. At the Erlenbach, this gradient is the slope of the artificial approach flow channel upstream of the SPG system.

[b] Depth-averaged mean flow velocities measured during the calibration measurements using an magnetic-inductive flow meter OTT MF Pro (Albula and Navisence), a radar-based stage sensor Vegapuls WL 61 (Avançon de Nant), and a 2-D laser sensor TiM551 by SICK AG© (Erlenbach)[c] More information on the sites is available in Nicollier et al. (2021).

[d] More information on the site is available in Antoniazza et al. (2022).

[e] More information on the site is available in e.g. Rickenmann et al. (2012), Wyss et al. (2016c), Rickenmann et al. (2018).

2.3 Controlled flume experiments

The first part of the signal conversion procedure described in this study is based on controlled flume experiments conducted at the outdoor flume facility of the Oskar von Miller institute of TU Munich in Obernach, Germany. At this facility, we reconstructed the bed characteristics of the Albula, Navisence and Avançon de Nant field sites, one after another, in a flume test reach with dimensions of 24 m x 1 m equipped with two impact plates (Fig. 3). For each site reconstruction we tested bedload material collected during field calibration measurements, and we adjusted the flow velocity, flow depth, and bed roughness to match the respective field observations. A detailed description of the original flume setup and the performed experiments can be found in Nicollier et al. (2020). In this paper, we primarily use the single-grain-size experiments conducted in 2018 with the flume configured to match conditions at the Albula field site (Table 2). Single-grain-size experiments consisted of feeding the flume with a fixed number of grains for each of the ten particle-size classes described in Sect. 2.2 above. While these particles were transported over the SPG system, the full raw geophone signal was recorded. Up to 33 repetitions were conducted until a representative range of amplitude and frequency values for each grain-size class was obtained (Nicollier et al., 2021). The same procedure was repeated for two different flow velocities (V_f = 1.6 m s^{-1} and 2.4 m s^{-1}). The obtained information was then used to derive empirical relationships between the mean particle size $D_{m,j}$ and properties of the SPG signal, as described in Sect. 2.5.2 below.

To illustrate the AF and AH methods and their respective performance, we use flume experiments that mimic the Avançon de Nant field site, but with the addition of a 4 m wooden partition wall (Fig. 3) that shields one geophone plate from impacting particles (Nicollier et al., 2022). With this modified setup, single-grain-size experiments were run using

165 grains from each of the 10 particle-size classes and originating from the Avançon de Nant channel, resulting in a total of 51

166 runs (Table 2). The flow velocity was set to 3 m s^{-1} to facilitate particle transport through the narrower flume section and is

167 therefore not representative for the Avançon de Nant site, where typical flow velocities were roughly 1.3 m s^{-1}.

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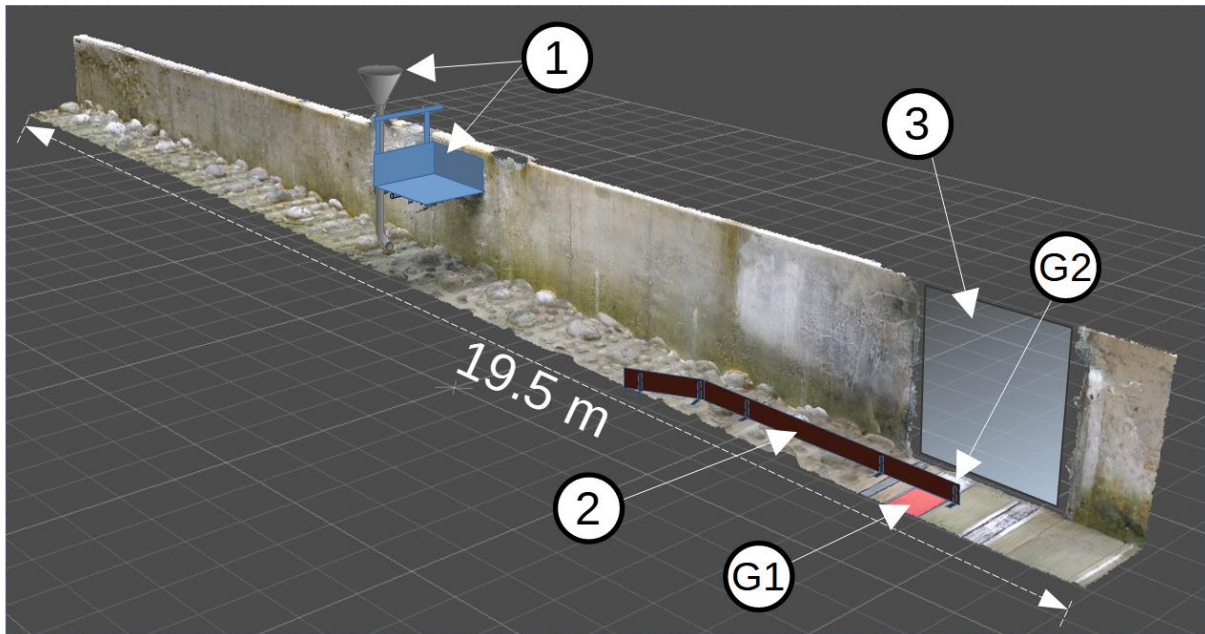
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170 **Figure 3: Oblique view of the Obernach flume test reach with total length of 24 m and width of 1 m. The bed surface is paved with**

171 **particles with diameters equaling the characteristic D_{67} and D_{84} sizes of the natural beds of the reconstructed sites. Grains were**

172 **fed into the channel 8 m upstream from the SPG system location (G1 and G2) using either a vertical feed pipe or a tiltable basket**

173 **(1). The sensor plate G1 (in red) was shielded from direct particle impacts by the 4 m long removable partition wall (2). The**

174 **partition wall and the impact plates were decoupled from each other by a 2 mm vertical gap to prevent disturbances of the**

175 **recorded signal. Plexiglas walls (3) on each side of the flume facilitated video recordings of the experiments.**

176

177 **Table 2: Flume and hydraulic characteristics for the reconstruction of the Albula and the Avançon de Nant field sites.**

Parameter	Units	Reconstructed field site setup	
		Albula (without partition wall)	Avaçon de Nant (with partition wall)
Flume width	m	1.02	1.02
Flume gradient of the natural bed	%	0.7	4.0
Bed surface D_{67} [a]	mm	120	200
Bed surface D_{84} [a]	mm	190	320
Number of D_{67}-particles/m^2	m^{-2}	15.0	5.0
Number of D_{84}-particles/m^2	m^{-2}	5.0	2.5
Min. water depth above SPG	m	0.79	0.35
Max. water depth above SPG	m	0.91	0.35
Min. flow velocity 10 cm above SPG [b]	m s^{-1}	1.6	3.0
Max. flow velocity 10 cm above SPG [b]	m s^{-1}	2.4	3.0
Min. unit discharge	m^2 s^{-1}	1.6	0.8
Max. unit discharge	m^2 s^{-1}	2.4	0.8
Number of different flow velocity settings	-	2	1

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Total number of single-grain-size experiments	-	355	51
Total number of tested particles	-	10705	2485

[a] On the basis of line-by-number pebble counts at the natural site and a photo-sieving based granulometric analysis with BASEGRAIN
179 software (Detert and Weitbrecht, 2013).
180 [b] Flow velocities measured with the OTT MF Pro magnetic-inductive flow meter.

181 **2.4 The amplitude-histogram method**

182 Wyss et al. (2016a) introduced the packet-based amplitude-histogram (AH) method to derive grain-size information from
183 geophone signals. A packet is defined as a brief interval, typically lasting 5 to 30 milliseconds, reflecting a single particle
184 impact on a plate (Fig. 1b); it begins and ends when the signal envelope crosses a threshold amplitude of 0.0216 V. The
185 signal envelope is computed in Python with the Hilbert transform (Jones et al., 2002), yielding the magnitude of the analytic
186 signal, i.e. the total energy in the signal. Each packet's maximum amplitude is then used to assign it to a predefined
187 amplitude class j delimited by amplitude-histogram thresholds $th_{ah,j}$ (Table 3), yielding a packet-based amplitude histogram
188 (e.g. Fig. 4 in Wyss et al., 2016a). Each amplitude class j is related to a corresponding grain-size class through the following
189 relationship between the mean amplitude $A_{m,j}$ [V] and the mean particle size $D_{m,j}$ [mm]:

190
$$A_{m,j} = 4.6 \cdot 10^{-4} \cdot D_{m,j}^{1.71} . \tag{1}$$

191 The coefficients in Eq. (1) were determined using 31 basket samples collected at the Erlenbach for which the maximum
192 geophone amplitude was analyzed as a function of the B-axis of the largest particle found in the sample (Wyss et al., 2016a).
193 The grain-size classes are delimited by the size of the meshes $D_{sieve,j}$ used to sieve the bedload samples from field
194 calibration measurements. For a given bedlaod sample, it is assumed that the number of packets between two amplitude-
195 histogram thresholds $th_{ah,j}$ is a good proxy for the fractional bedload mass between the respective sieve sizes (Wyss et al.,
196 2016a). In the present study, we have extended the seven size classes used by Wyss et al. (2016a) to ten classes, in order to
197 assess the performance of the AH and AF methods for larger particles.

198

199 **Table 3: Characteristics of the size classes j according to Wyss et al. (2016a) with the sieve mesh sizes $D_{sieve,j}$, the mean particle**
200 **diameter $D_{m,j}$, and the amplitude-histogram thresholds $th_{ah,j}$ derived from Eq. (1). Additionally the lower and upper amplitude-**
201 **frequency thresholds $th_{af,low,j}$ and $th_{af,up,j}$ derived from Eq. (4) and (5), respectively (see Sect. 2.5.2). The value of $D_{m,j}$ for the**
202 **largest class (10) in brackets is an estimate, because this size class is open-ended and thus the mean varied somewhat from site to**
203 **site.**

Class j	$D_{sieve,j}$	$D_{m,j}$	$th_{ah,j}$	$th_{af,low,j}$	$th_{af,up,j}$
[-]	[mm]	[mm]	[V]	[V]	[V Hz^{-1}]
1	9.5	12.3	0.0216	0.0132	$1.55 \cdot 10^{-5}$
2	16.0	17.4	0.0527	0.0364	$2.33 \cdot 10^{-5}$
3	19.0	21.8	0.0707	0.0509	$4.45 \cdot 10^{-5}$
4	25.0	28.1	0.1130	0.0868	$7.67 \cdot 10^{-5}$
5	31.4	37.6	0.1670	0.1362	$1.78 \cdot 10^{-4}$
6	45.0	53.2	0.3088	0.2725	$3.93 \cdot 10^{-4}$
7	63.0	71.3	0.5489	0.5244	$7.05 \cdot 10^{-4}$
8	80.7	95.5	0.8378	0.8489	$1.56 \cdot 10^{-3}$
9	113.0	127.9	1.4919	1.6342	$2.79 \cdot 10^{-3}$
10	144.7	(171.5)	2.2760	2.6438	-

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2.5 The amplitude-frequency method

In a recent study, Nicollier et al. (2022) showed that the SPG system is sensitive to extraneous particle impacts despite the isolating effect of the elastomer. Extraneous signals at individual geophone plates can arise from impacts occurring on neighboring plates, or from impacts on the concrete sill surrounding the SPG array. While attenuated to some extent, the elastic waves generated by such impacts can reach multiple geophone sensors with enough energy to be recorded as apparent packets. Thus, packet histograms (i.e. counts of the number of packets per class j) are subject to a certain bias, especially in the lower size classes. The degree of bias was found to depend mainly on two factors. First, coarser grain sizes of transported bedload were shown to generate more apparent packets. Second, more apparent packets were recorded, for a given bedload mass, at transects containing more SPG plates. Nicollier et al. (2022) showed that packet characteristics such as the start time, the amplitude and the frequency help in identifying apparent packets and filtering them out from the final packet histograms. This filtering method was subsequently applied to all four field calibration datasets (Albula, Navisence, Avançon de Nant and Erlenbach) and helped to reduce the differences between the site-specific mean calibration relationships for the total bedload flux by about 30% (Nicollier et al., 2022). Based on these observations, the present study proposes an amplitude-frequency (AF) method as an adaptation of the amplitude-histogram (AH) method presented by Wyss et al. (2016a). By introducing two-dimensional (amplitude and centroid frequency) size class thresholds, the new method aims to reduce the effect of apparent packets and improve the accuracy of fractional bedload flux estimates. Note that the procedure does not allow to make the difference between particles impacting one plate simultaneously, but the high (10 kHz) recording frequency of the SPG system minimizes its probability of occurrence

2.5.1 Centroid frequency

According to the Hertz contact theory, the frequency at which a geophone plate vibrates is controlled by the size of the colliding particle (Johnson, 1985; Thorne, 1986; Bogen and Møen, 2003; Barrière et al., 2015; Rickenmann, 2017). In the present study, the frequency spectrum of a packet is characterized by the spectral centroid f_{centroid}. It represents the center of mass of the spectrum and is computed as

$$f_{\text{centroid}} = \frac{\sum f_n \cdot A_{\text{FFT},n}}{\sum A_{\text{FFT},n}} \tag{2}$$

where $A_{\text{FFT},n}$ [V·s] is the Fourier amplitude (computed with the Fast Fourier Transform FFT) corresponding to the frequency f_n [Hz]. Following Wyss et al. (2016b), before applying the FFT, each packet is preprocessed in two steps. First, a cosine taper is applied at the edges of a max. 8 ms time window around the peak amplitude of each packet. Second, the signal contained in this time window is zero-padded on either side to reach an optimal number of sample points $nFFT$. The taper is used to smooth the transition between the packet and the concatenated zeros, and to suppress spectral leakage, which results in a more accurate amplitude spectrum. The value of $nFFT$ was set to 2^7 in order to adequately resolve the amplitude spectrum of the raw signal contained in the max. 8 ms time window. This time window focuses on the first arrival waveform to obtain a more accurate evaluation of the high-frequency content of the packet (Nicollier et al., 2022). The single-sided Fourier transform of the processed packet is then computed in order to extract A_{FFT} and derive f_{centroid} (Eq. 2). A decrease in f_{centroid} with increasing particle size was observed for different bedload surrogate monitoring techniques (Belleudy et al., 2010; Uher and Benes, 2012; Barrière et al., 2015). Furthermore, f_{centroid} has the advantage of showing weaker dependency on the flow velocity and transport mode than the maximum registered packet amplitude (Wyss et al. 2016b; Chen et al., 2022). As shown by Nicollier et al. (2022), f_{centroid} also contains information about the impact location of a packet-triggering particle. Because high frequencies are more rapidly attenuated than low frequencies along the travel path of a

seismic wave, (apparent) packets triggered by impacts on a given plate typically have higher $f_{centroid}$ values than packets triggered by impacts occurring beyond that plate's boundaries.

2.5.2 Flume-based amplitude-frequency thresholds

The particle mass associated with an individual signal packet is strongly dependent on the size of the impacting particle. Inferring sediment transport rates from SPG signals thus requires assigning each packet to a corresponding sediment size class using threshold values of packet characteristics (Table 3). Wyss et al. (2016a) derived size class thresholds (or AH thresholds) of packet peak amplitude from field measurements (Eq. 1). In the present study, we take advantage from the single-grain-size experiments conducted at the flume facility (without the partition wall) (Nicollier et al., 2021) to derive size class thresholds combining packet amplitude and frequency (or AF thresholds). Each packet is assigned to a given class j delimited by a lower threshold $th_{af,low,j}$ based on the maximum amplitude of the packet's envelope $MaxAmp_{env}$ [V], and an upper threshold $th_{af,up,j}$ based on the ratio $MaxAmp_{env}/f_{centroid}$ [V Hz^{-1}]. Compared to the raw signal, the envelope has the advantage of returning the magnitude of the analytical signal and thus better outlines the waveform by omitting the harmonic structure of the signal (Fig. 2b). Similar combinations of amplitude and frequency have been used to infer particle sizes and improve the detectability of bedload particles in previous studies involving impact plates (Tsakiris et al., 2014; Barrière et al., 2015; Wyss et al., 2016b; Koshiba and Sumi, 2018) and pipe hydrophones (Choi et al., 2020).

The lower and upper amplitude-frequency thresholds are obtained as follows. First, all packets recorded during the single-grain-size experiments are filtered with respect to the following criterion adapted from Nicollier et al. (2022):

$$Criterion: f_{centroid} > a_c \cdot e^{(b_c \cdot MaxAmp_{env})}, \tag{3}$$

with a_c = 1980 Hz and b_c = -1.58 V^{-1}. The values for the linear coefficient a_c and the exponent b_c were obtained through an optimization process discussed below (Sect. 4.1), and were found to ideally set apparent packets apart from real ones. Packets that do not meet this criterion are considered as apparent packets and are ignored in the further analysis in order to obtain more accurate threshold values. Note that in the present study the criterion in Eq. 3 has not been applied to the data when implementing the AH method developed by Wyss et al. (2016a).

The next step consists in fitting a power-law least-squares regression line through the 75th percentile amplitude $MaxAmp_{env,75th,j}$ and amplitude-frequency $(MaxAmp_{env}/f_{centroid})_{75th,j}$ values of the packets detected for a given grain-size class j fed into the flume that met the filtering criterion (Fig. 4), resulting in the following two equations:

$$MaxAmp_{env,75th,j} = 1.66 \cdot 10^{-4} \cdot D_{m,j}^{1.95}, \text{ and} \tag{4}$$

$$\left(\frac{MaxAmp_{env}}{f_{centroid}}\right)_{75th,j} = 2.26 \cdot 10^{-8} \cdot D_{m,j}^{2.36}. \tag{5}$$

Finally, the lower threshold values $th_{af,low,j}$ are obtained by replacing $D_{m,j}$ in Eq. (4) with the lower sieve sizes $D_{sieve,j}$, while the upper threshold values $th_{af,up,j}$ are obtained by replacing $D_{m,j}$ in Eq. (5) with the upper sieve sizes $D_{sieve,j+1}$ (Table 3 and triangles in Fig. 5). The advantage in fitting functions such as Eq. (4) and (5) is that they allow the computation of thresholds for any classification of particle (sieve) sizes.

Particularly for the largest particles, apparent packets can greatly outnumber real packets. Due to their relatively small amplitudes, these apparent packets can substantially dilute the average signal response associated with the largest grain sizes (see the red boxplots in Fig. 5). However, filtering out apparent packets reveals a clear relationship, which would otherwise be obscured, between the mean particle size $D_{m,j}$ and both the amplitude $MaxAmp_{env}$ and the ratio $MaxAmp_{env}/f_{centroid}$

279 (see the blue boxplots in Fig. 5). Overall, the filtering with criterion (Eq. 3) at the Obernach flume site eliminated about 61%

280 of all the packets.

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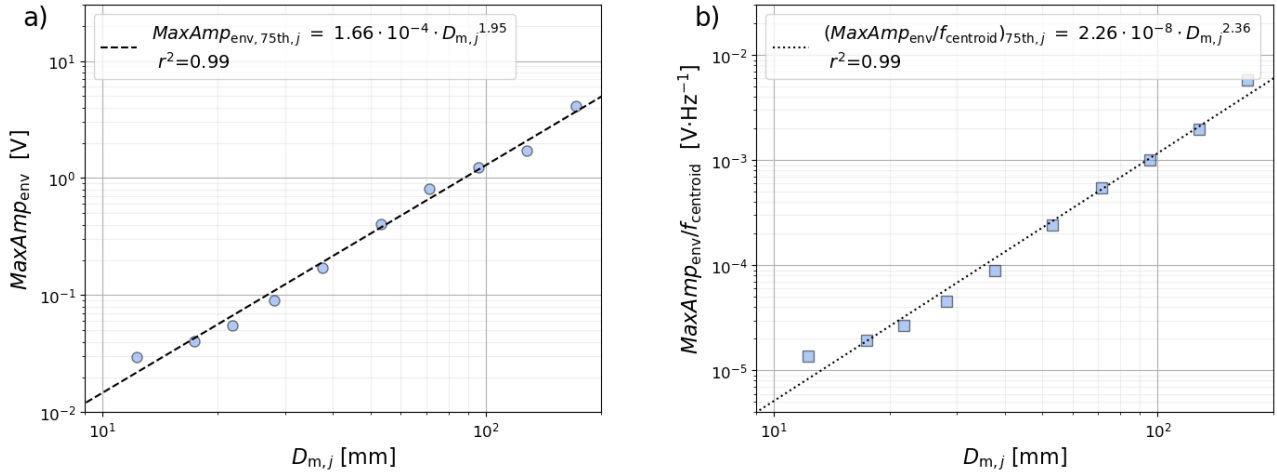
Figure 4: Power-law least-squares regression relationships between the mean particle diameter $D_{m,j}$ and the 75th percentile of the (a) amplitude $MaxAmp_{env,75th,j}$ and (b) amplitude-frequency $(MaxAmp_{env}/f_{centroid})_{75th,j}$ values obtained from the single-grain-size experiments after filtering out apparent packets using the filtering criterion in Eq. (3).

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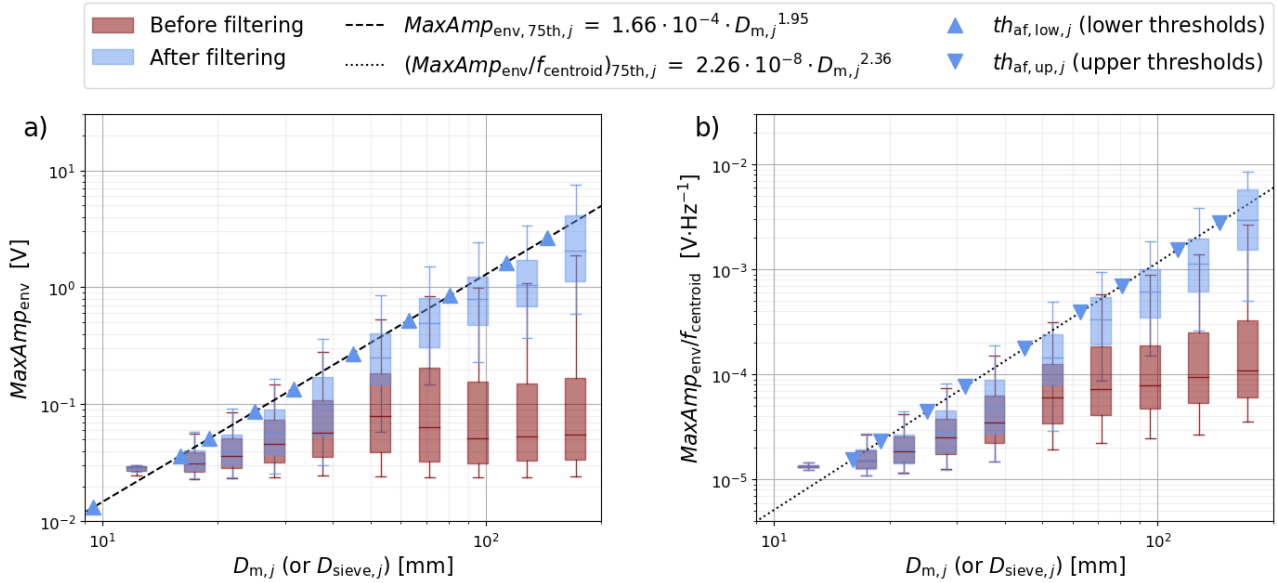
Figure 5: Range of signal responses obtained for each individual grain-size class fed into the flume before (red boxes) and after (blue boxes) filtering out apparent packets using the filtering criterion in Eq. (3), with (a) the maximum amplitude of the envelope $MaxAmp_{env}$ and (b) the ratio $MaxAmp_{env}/f_{centroid}$ as functions of the mean particle diameter $D_{m,j}$. In (a), the lower threshold values $th_{af,low,j}$ are obtained by replacing $D_{m,j}$ with the lower sieve sizes ($D_{sieve,j}$) in the equation of the dashed power-law regression line (Eq. 4). In (b), the upper threshold values $th_{af,up,j}$ are obtained by replacing $D_{m,j}$ with the upper sieve sizes ($D_{sieve,j+1}$) in the equation of the dotted power-law regression line (Eq. 5).

2.5.3 Application to field calibration measurements

294 The lower and upper thresholds $th_{af,low,j}$ and $th_{af,up,j}$ obtained from the filtered flume experiments can be transferred to the

295 field calibration datasets, if the SPG apparatus and the geophone data recording and preprocessing routines are identical in

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both cases. The following steps will now lead us to the final general calibration coefficients $k_{b,j,gen}$ (Fig. 6). First, for each field measurement i, the thresholds $th_{af,low,j}$ and $th_{af,up,j}$ are used for counting the number of packets per class j from the recorded geophone signal. Second, a sample- and class-specific calibration coefficient $k_{b,i,j}$ with units [kg^{-1}] is obtained by dividing the number of recorded packets $PACK_{i,j}$ by the sampled fractional mass $M_{meas,i,j}$ as follows:

$$k_{b,i,j} = \frac{PACK_{i,j}}{M_{meas,i,j}}.$$ (6)

Finally, the general calibration coefficient $k_{b,j,gen}$ is computed for each class j using

$$k_{b,j,gen} = \frac{1}{N_{stations}} \sum_{stations} k_{b,j,med,station},$$ (7)

where $k_{b,j,med,station}$ is the site-specific median calibration coefficient computed over all samples i, and $N_{stations}$ is the number of stations. Even though the number of calibration measurements differs from site to site, each coefficient $k_{b,j,med,station}$ in Eq. (7) is equally weighted in order to give the same importance to site-specific factors possibly affecting the signal response at each site.
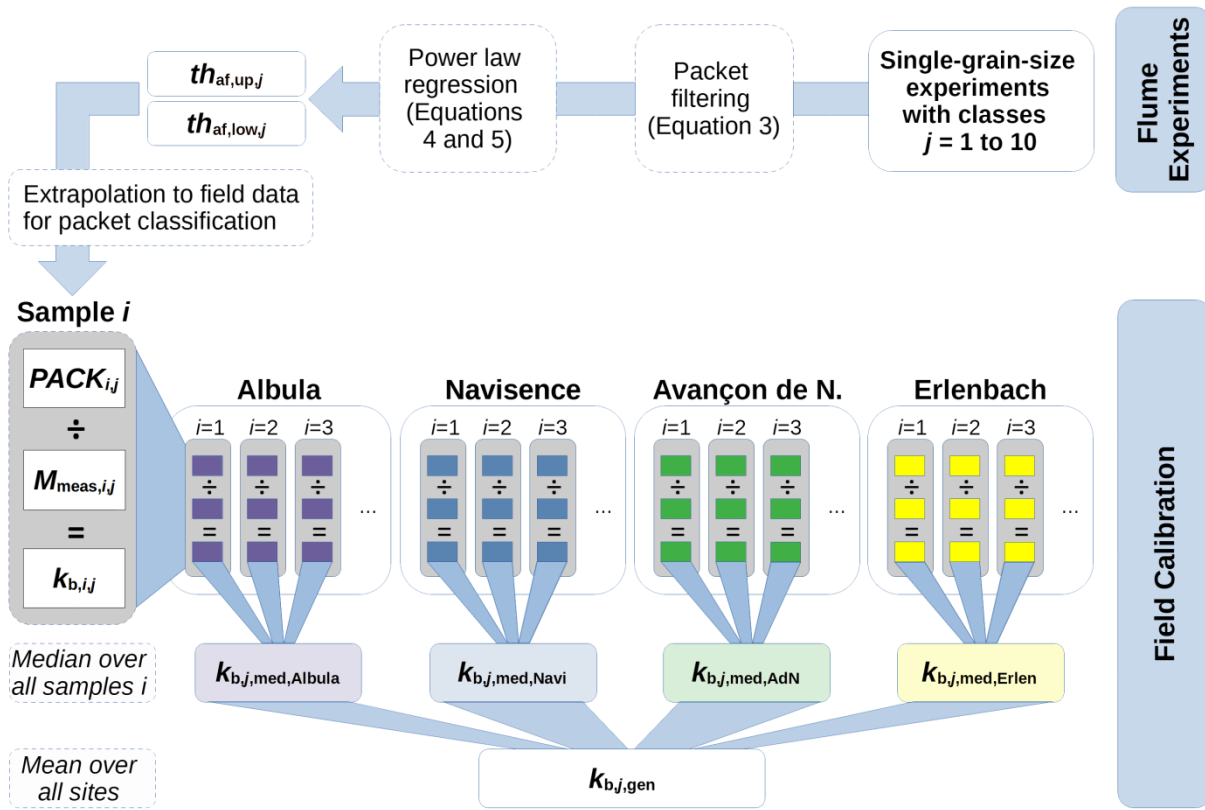
Figure 6: Workflow leading from the single-grain-size flume experiments with particles from ten size classes j (top right) to the final array of general calibration coefficients $k_{b,j,gen}$. Central elements are the lower and upper threshold values $th_{af,low,j}$ and $th_{af,up,j}$, the number of recorded packets $PACK_{i,j}$ per sample i and class j, the sampled fractional mass $M_{meas,i,j}$, the sample- and class- specific calibration coefficient $k_{b,i,j}$, and finally the site-specific median calibration coefficient $k_{b,j,med,station}$. To enable a comparison with the AH method developed by Wyss et al. (2016a), the "Field Calibration" part of the workflow was also carried out with the AH thresholds $th_{ah,j}$ (see Table 3).

At this point, the single array of calibration coefficients $k_{b,j,gen}$ is applied as follows to each field calibration measurement i in order to obtain fractional bedload mass estimates $M_{est,i,j}$:

$$M_{\text{est},i,j} = k_{\text{b},j,\text{gen}} \cdot PACK_{i,j} . \tag{8}$$

Rickenmann and Fritschi (2017) showed that bedload mass estimates derived from SPG measurements are more accurate at higher transport rates. The estimated fractional bedload mass $M_{\text{est},i,j}$ can be converted to a unit fractional transport rate $q_{\text{b},\text{est},i,j}$ [kg m^{-1} s^{-1}] using:

$$q_{\text{b},\text{est},i,j} = \frac{1}{w_{\text{p}} \cdot n_{\text{p}}} \cdot \frac{M_{\text{est},i,j}}{\Delta t_i} , \tag{9}$$

where w_{p} is the standard width of an impact plate (0.5 m), n_{p} is the number of plates (which may include the whole transect, or a section of particular interest), and Δt_i is the sampling duration in seconds. Finally, the estimated unit total bedload flux $q_{\text{b},\text{tot},\text{est},i}$ can be computed as follows:

$$q_{\text{b},\text{tot},\text{est},i} = \sum_{j=1}^{10} q_{\text{b},\text{est},i,j} \tag{10}$$

Note that the exact same procedure was followed using the AH thresholds $th_{\text{ah},j}$ derived from Wyss et al. (2016a) (Eq. 1; Table 3) to compare the performance between the AH method and the new AF method.

3   Results

3.1   Flume experiments

The flume experiments performed in the modified Avançon de Nant setup with the partition wall help to illustrate the two calibration methods. Fig. 7a and 7b show the amplitude and frequency characteristics of all packets detected by the SPG system during these experiments. Packets detected by the shielded sensor G1 all originate from impacts that occurred either on the concrete bed or on plate G2 (Nicollier et al., 2022). Packets detected by the unshielded sensor G2 are considered as apparent if they are located in the area of the amplitude-frequency graph (Fig. 7a) where G1 and G2 packets overlap. Such packets are presumed to have been triggered by impacts on the concrete bed too. This overlapping area arises from the fact that a seismic wave generated by an impact on the concrete bed follows a similar path towards both sensors, resulting in the recording of two apparent packets with comparable characteristics. The remaining packets, detected by G2 and located in the non-overlapping area of the amplitude-frequency graph, are considered as real, rather than apparent. The difference in f_{centroid} between real and apparent packets (Fig. 7a) reflects the faster attenuation of higher frequencies during wave propagation, as mentioned earlier. Size class boundaries derived by the AH method of Wyss et al. (2016a) encompass all of the packets, both apparent and real (Fig. 7a). This is because the boundaries are defined solely by AH thresholds ($th_{\text{ah},j}$). By contrast, in the AF method proposed here, the two-dimensional class boundaries given by $th_{\text{af},\text{low},j}$ and $th_{\text{af},\text{up},j}$ cover only a fraction of all detected packets (Fig. 7b). Applying the step-like AF thresholds leads to a strong reduction of the number of packets $PACK_j$ within each size class j for plate G1 (shielded), particularly for the smaller classes. Meanwhile, the AF thresholds had little effect on the number of detected packets for G2 (unshielded), except for a strong decrease for classes $j = 1$ and 2, and a slight increase for classes $j = 6$ to 10 (Fig. 7c and 7d). The AH thresholds encompass in total 1945 packets for the shielded geophone G1, and 4823 packets for the unshielded geophone plate G2. In comparison, the AF thresholds encompass in total 159 packets for the shielded geophone G1, and 2202 packets for the unshielded geophone plate G2 (counting the packets in the overlapping class boundaries only once). Considering apparent packets as noise and real packets as signal, applying the new AF method results in an increased signal to noise ratio, as shown by the larger vertical separation between the blue (signal) and red (noise) lines in Fig. 7d compared to Fig. 7c.
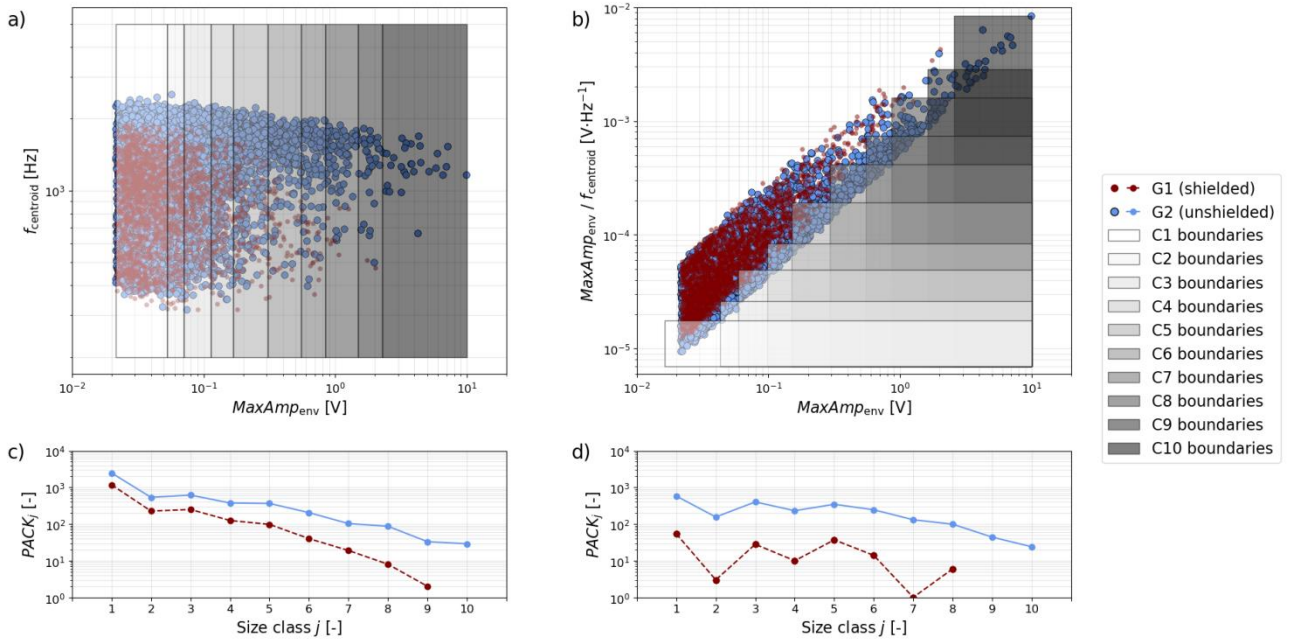
Figure 7: Characteristics of the packets recorded during single-grain-size experiments conducted with the Avançon de Nant flume setup using the partition wall, with the maximum amplitude of the envelope $MaxAmp_{env}$ and the centroid frequency $f_{centroid}$. The red and blue dots correspond to packets recorded by the shielded plate G1 and the unshielded plate G2, respectively. The grey rectangles are the class boundaries delimited by the thresholds obtained for the AH method (a) and the AF method (b). The number of packets $PACK_j$ located within the class boundaries delimited by the AH thresholds and the AF thresholds are indicated in (c) and (d), respectively. In (a), $f_{centroid}$ is shown as function of $MaxAmp_{env}$ for information purposes only.

3.2 Field calibration coefficients

As discussed in the previous section, the number of packets $PACK_{i,j}$ detected for a given class j varies together with the thresholds $th_{ah,j}$, $th_{af,low,j}$ and $th_{af,up,j}$. Because the measured fractional bedload mass $M_{meas,i,j}$ remains constant, the calibration coefficients $k_{b,i,j}$ will depend on the number of packets detected, and thus on the thresholds that are used to classify them. We can make the following observations regarding the calibration coefficients $k_{b,i,j}$ obtained using the AF method (Fig. 8b) compared to the AH method (Fig. 8a). First, the $k_{b,i,j}$ coefficients of the smaller size classes are substantially lower, meaning that fewer packets per unit mass are detected. Second, for the larger size classes, slightly more packets are detected per unit mass. Third, the overall scatter of the $k_{b,i,j}$ coefficients across all sites is smaller, in particular for the six smallest classes j. This is reflected in the decrease of the mean coefficient of variation (CV) across all classes j and all sites from CV = 1.17 (in the AH method) to CV = 0.93 (in the AF method). Fourth, the scatter of the site-specific $k_{b,i,j}$ coefficients is usually smaller. This is supported by the change of the mean CV across all classes from 0.89 to 0.54 for the Albula, from 0.83 to 0.75 for the Avançon de Nant and from 1.31 to 1.00 for the Erlenbach, between the AH and AF methods. The mean CV for the Navisence site however remains unchanged at 0.85. The general coefficients $k_{b,j,gen}$ obtained from the site-specific median coefficients $k_{b,j,med}$ using Eq. (7) are listed in Table 4.

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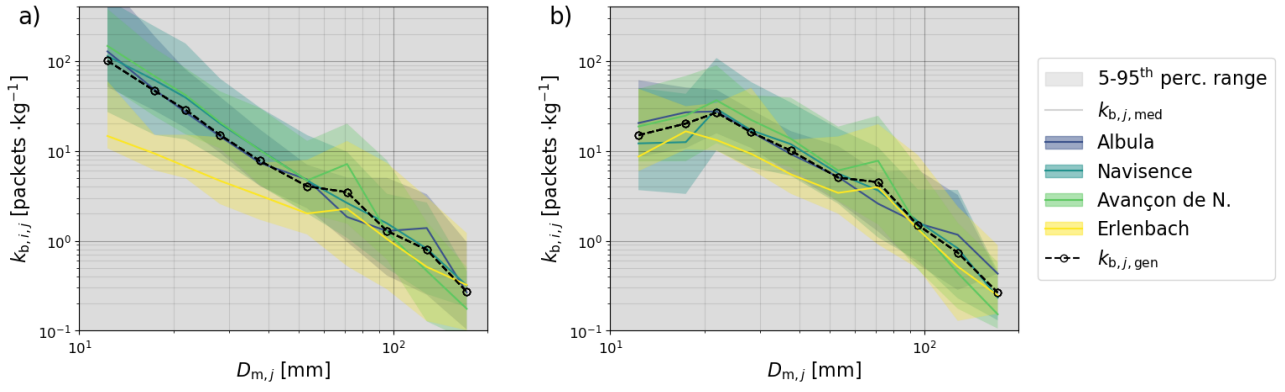
Figure 8: The $k_{b,i,j}$ calibration coefficients obtained with the AH method (a) and the AF method (b) for each field site. The colored areas indicate the range between the 5th and the 95th percentile $k_{b,i,j}$ values, the full lines indicate the site-specific median coefficients $k_{b,j,med}$ and the black dashed lines indicate the final general calibration coefficients $k_{b,j,gen}$ as a function of the mean particle diameter $D_{m,j}$ of each grain-size class j.

Table 4: General calibration coefficients $k_{b,j,gen}$ obtained for each grain-size class j with the AH method and the AF method using Eq. (7).

	Method	Units	$j = 1$	$j = 2$	$j = 3$	$j = 4$	$j = 5$	$j = 6$	$j = 7$	$j = 8$	$j = 9$	$j = 10$
$k_{b,j,gen}$	AH	kg^{-1}	100.67	46.43	28.68	15.03	7.76	4.04	3.47	1.29	0.79	0.27
	AF	kg^{-1}	14.97	20.15	26.65	16.15	10.06	5.05	4.49	1.50	0.74	0.27

3.3 Bedload flux estimates

We can now insert the general calibration coefficients $k_{b,j,gen}$ in Eq. (8) to compute fractional bedload mass estimates $M_{est,i,j}$ and subsequently the unit fractional flux estimates $q_{b,est,i,j}$ (Eq. 9) for every sample collected at the four field sites. Fig. 9 illustrates the accuracy of the bedload flux estimates obtained with the AF method for each sample across the grain-size classes and the field sites. The results obtained with the AH method can be found in Supplementary Information S3, and Table 5 provides further information on the performance of the two methods. The dashed colored power-law regression lines shown in Fig. 9, described by the corresponding linear coefficient a and exponent b (Table 5), indicate possible trends in over/under-estimation at each field site. The coefficient of determination R^2 describes the accuracy of the estimates relative to the 1:1 line. The root-mean-square error (*RMSE)* quantifies the expected error of the estimates and is expressed in [kg m^{-1} s^{-1}]. When applied to the field calibration data, the AF method generally yields more accurate flux estimates than the AH method does. This is most notably reflected by the R^2 values and the percentages p_{factor_2} and p_{factor_5} of all detected samples whose estimated bedload fluxes differ by less than a factor of 2 and 5, respectively, from the measured values (Table 5). The five smallest grain-size classes were most strongly affected by these improvements, whereas the estimates for the largest fractions ($j = 7$ to 10) were only slightly improved.

Aside from these comparative observations, it is also worth mentioning the following more general findings that are valid for both methods: (i) for most size fractions, the relative scatter of the estimates (on the log-log plots) decreases with increasing transport rates; (ii) at low transport rates, mass fluxes are generally overestimated, while at high transport rates they are generally underestimated; (iii) mass fluxes for the Erlenbach closely follow the 1:1 line but tend to be slightly underestimated; (iv) the number of measured ($N_{samples,meas}$) and estimated ($N_{samples,est}$) samples both decrease with

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increasing particle size. Samples for which either the measured or the estimated flux equals 0 are indicated as dots along the axes in Fig. 9. If the measured flux is zero but the estimated flux is positive, the sample can be regarded as false positive (Fawcett, 2006). The difference between $N_{\text{samples,meas}}$ and $N_{\text{samples,est}}$ in Table 5 indicates that the occurrence of such false positive samples increases with increasing particle size. Further performance metrics derived from the confusion matrix can be found in the Supporting Information (Table S2).
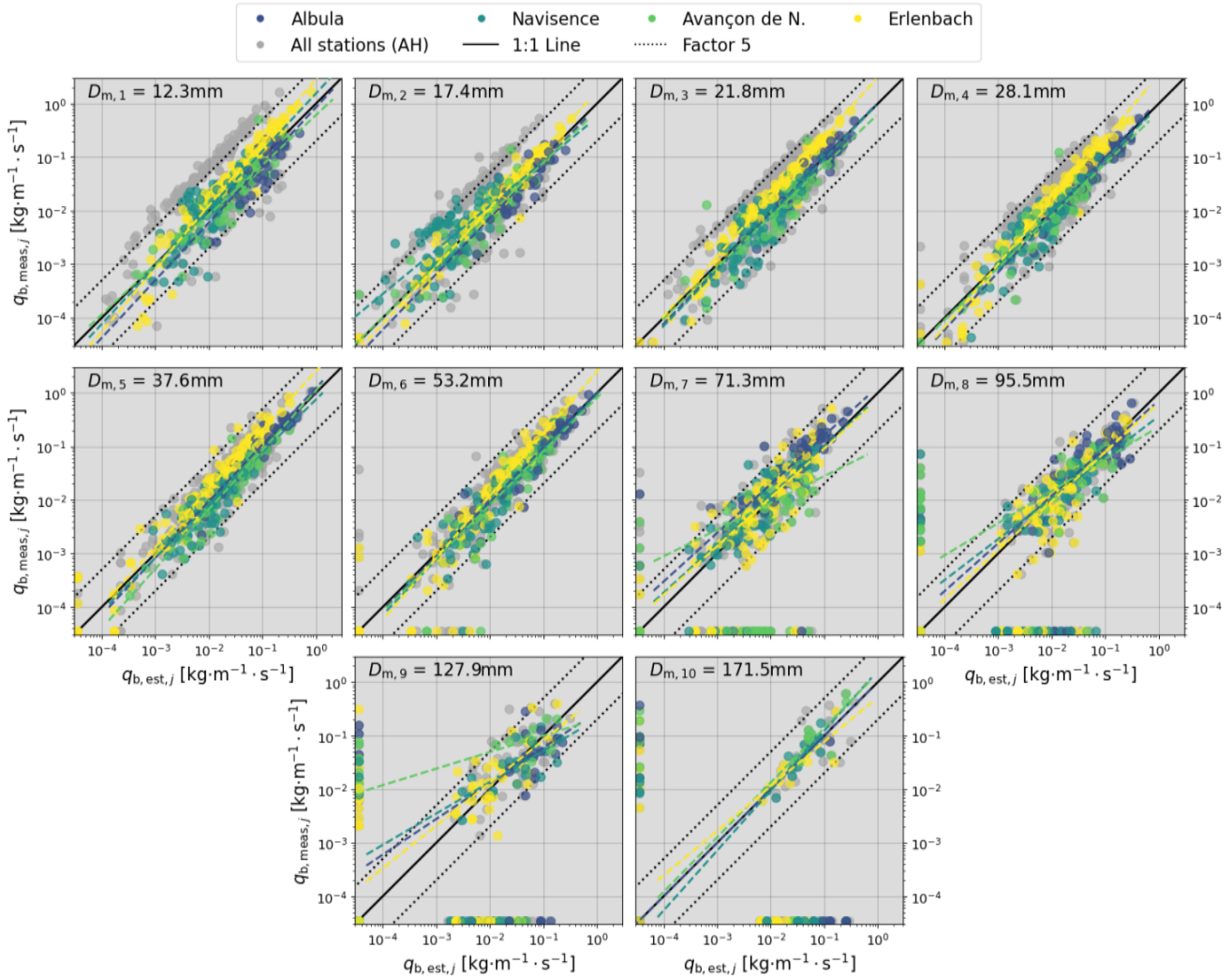
Figure 9: Unit fractional transport rate estimates obtained with the AF method for each size class *j* and each station. The light grey dots in the background indicate the estimates obtained with the AH method and are represented in more detail in the Supporting Information (Fig. S1). Each frame is annotated with the mean particle size $D_{\text{m},j}$ of the represented class. The solid black lines correspond to the reference 1:1 line while the dotted lines delimit factors of 5 above and below (from 0.2 to 5). The dashed colored lines are power-law regression lines; the mean coefficients over all four sites are listed in Table 5. The dots along the axes indicate samples for which either the measured or the estimated unit fractional flux equals 0. These samples are not considered for the computation of the trend lines.

Table 5: Performance of the AH method and the AF method regarding fractional flux estimates for each class *j* with following parameters: the linear coefficient *a*, the exponent *b* and the correlation coefficient *r* of the power-law regression lines visible in Fig. 9; the coefficient of determination R^2; the root-mean-square error *RMSE*; and the percentage of all detected samples for which the estimated value differs from the measured value by less than a factor of 2 and 5 $p_{\text{factor\_2}}$ and $p_{\text{factor\_5}}$, respectively. These values

were first computed for each site separately and then averaged over all four sites. The number of measured $N_{samples,meas}$ and the number of estimated samples $N_{samples,est}$ showing a positive unit fractional rate were summed over all four sites.

		Units	$j=1$	$j=2$	$j=3$	$j=4$	$j=5$	$j=6$	$j=7$	$j=8$	$j=9$	$j=10$
$N_{samples,meas}$		-	308	308	306	306	302	287	240	213	112	53
AH method	$N_{samples,est}$	-	308	305	307	301	299	289	267	237	149	117
	r	-	0.77	0.83	0.87	0.88	0.91	0.89	0.73	0.75	0.53	0.46
	a	-	3.6	2.02	1.95	2	1.39	1.54	0.85	0.53	0.42	0.58
	b	-	0.94	0.95	1	1.05	1.01	1.05	0.83	0.83	0.64	0.6
	R^2	-	0.4	0.51	0.64	0.70	0.78	0.81	0.36	0.57	-0.16	0.11
	$RMSE$	kg·m^{-1}·s^{-1}	0.094	0.031	0.044	0.036	0.052	0.048	0.038	0.037	0.04	0.06
	p_{factor_2}	%	50	54	54	58	64	72	50	58	37	57
	p_{factor_5}	%	72	84	92	93	96	95	86	81	68	73
AF Method	$N_{samples,est}$	-	308	305	307	305	301	295	279	242	161	84
	r	-	0.79	0.82	0.89	0.91	0.93	0.93	0.81	0.78	0.52	0.61
	a	-	1.46	0.96	1.44	1.54	1.41	1.3	0.73	0.49	0.3	1.16
	b	-	1.07	0.98	1.03	1.05	1.06	1.05	0.81	0.79	0.59	0.74
	R^2	-	0.71	0.72	0.8	0.84	0.85	0.83	0.42	0.55	-0.08	0.59
	$RMSE$	kg·m^{-1}·s^{-1}	0.068	0.021	0.035	0.027	0.045	0.040	0.035	0.039	0.042	0.061
	p_{factor_2}	%	69	74	69	78	75	81	53	58	43	47
	p_{factor_5}	%	96	93	98	98	97	97	91	83	68	56

As indicated by Eq. (10), the unit total flux estimates are computed as the sum of the unit fractional flux estimates over all 10 classes. Fig. 10 shows the ratio $r_{q_{b,tot}}$ between the estimated total flux $q_{b,tot,est}$ and the measured total flux $q_{b,tot,meas}$ for all 308 calibration samples, as a function of the sampled total mass $M_{tot,meas}$. Here, the estimates for the Albula, the Navisence and the Avançon de Nant sites are slightly more accurate with the AF method than with the AH method, whereas the estimates for the Erlenbach improve substantially, with the median $r_{q_{b,tot}}$ value increasing from 0.31 to 0.64. Note that the observations (i) to (iii) made earlier regarding the fractional flux estimates are also valid here. Fig. 10 also provides an interesting overview of the sampled masses at all four stations, reflecting the capacities of the different devices (automated and manual basket samplers and crane-mounted net sampler) used to collect the calibration samples.
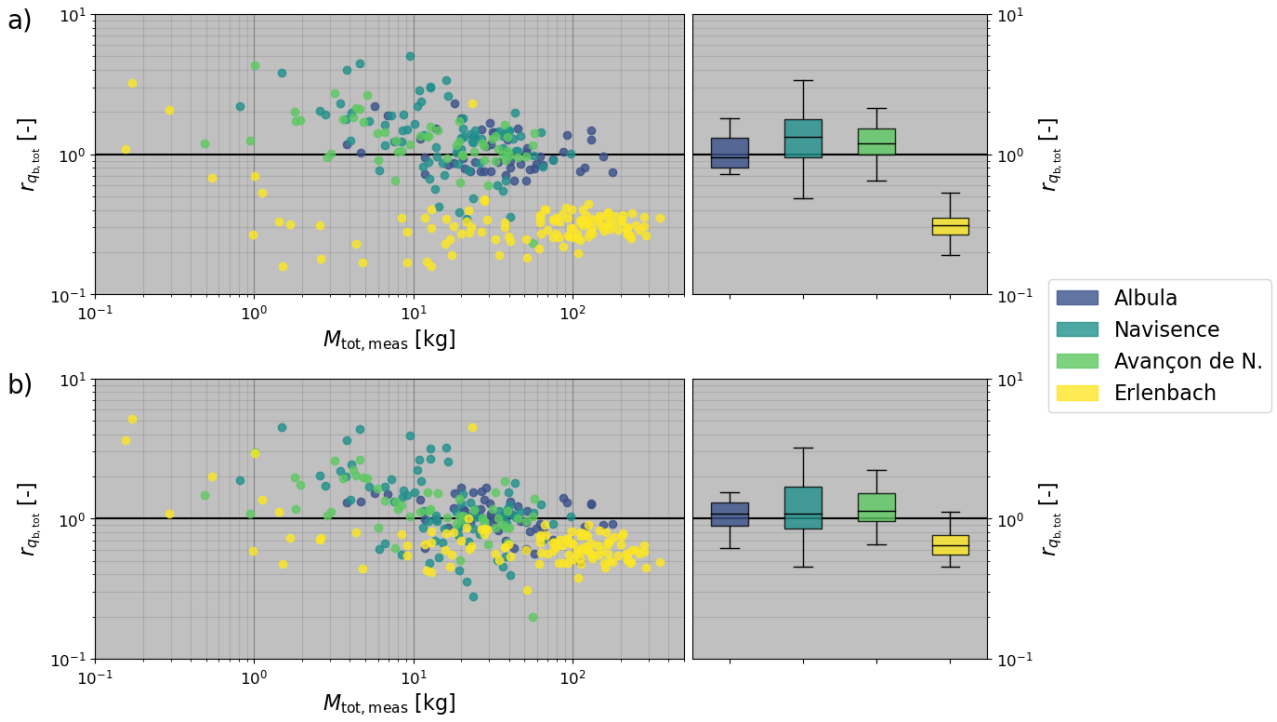
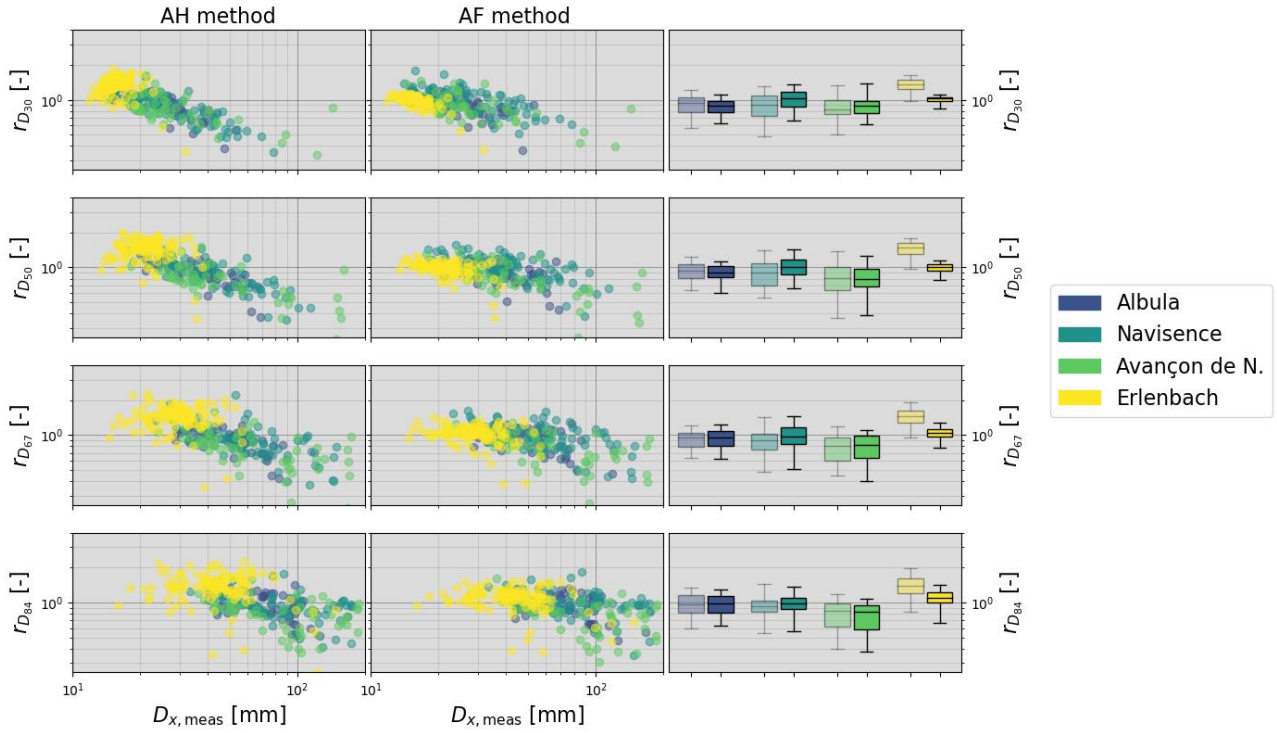Figure 10: Ratio $r_{q_{b,tot}}$ between the estimated and the measured unit total mass flux as a function of the total sampled mass $M_{tot,meas}$, for each collected sample i and each station, for the AH method (a) and the AF method (b). The boxplots on the right indicate the range of $r_{q_{b,tot}}$ values obtained for each station.

3.4 Grain-size estimates

We can combine the SPG bedload flux estimates for all grain-size fractions and thus derive grain-size distributions, which can then be compared to the measured size distributions of each calibration sample. Fig. 11 compares the performance of the AH and the AF methods in estimating the characteristic grain sizes D_{30}, D_{50}, D_{67} and D_{84} (where D_x is the grain diameter for which x percent of the sampled bedload mass is finer). The accuracy of the estimates is indicated by the ratio r_{D_x} between the estimated and the measured characteristic grain size D_x. Compared to the AH method, the AF method mainly improves the estimates of the four characteristic grain sizes for the Navisence and the Erlenbach sites, but has little effect at the other two sites. The largest improvement is achieved for the Erlenbach site, with the median $r_{D_{30}}$ changing from 1.37 to 1.02, the median $r_{D_{50}}$ changing from 1.48 to 1.01, the median $r_{D_{67}}$ changing from 1.46 to 1.05 and the median $r_{D_{84}}$ changing from 1.39 to 1.10. The overall accuracy of the estimates decreases with increasing characteristic size D_x for both methods, and for every characteristic size D_x, the D_x tends to be overestimated for finer grain mixtures and underestimated for coarser grain mixtures.

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Figure 11: Ratio r_{D_x} between the estimated and the measured characteristic grain sizes D_{30}, D_{50}, D_{67} and D_{84} as a function of the measured grain diameter $D_{x,meas}$ for each collected sample i and each station using the AH method (column 1) and the AF method (column 2). D_x is the grain diameter for which x percent of the sampled bedload is finer. The boxplots in column 3 indicate the range of r_{D_x} values obtained for each station. The boxes in faded colors show the results obtained with the AH method and the boxes in brighter colors show the results obtained with the AF method.

4   Discussion

4.1   The hybrid calibration procedure

Recent studies have pointed out the difficulty of transferring flume-based calibrations of the impact plate system to field applications (e.g. Mao et al., 2016; Wyss et al., 2016c; Kuhnle et al., 2017). In the hybrid calibration approach presented here, we took advantage of controlled flume experiments to obtain amplitude and amplitude-frequency thresholds for each particle-size class, which were subsequently applied to field calibration datasets to derive the general calibration coefficients $k_{b,j,gen}$.

The entire hybrid calibration procedure was run iteratively until the optimal linear coefficient and exponent of the criterion (Eq. 3) used to filter out apparent packets were found (Fig. 6). As objective function we used an equally weighted combination of parameters describing the accuracy of bedload flux and grain-size estimates, i.e. r, R^2, p_{factor_2}, p_{factor_5}, and *RMSE* as shown in Table 5, r_{D_x} as shown in Fig. 11, and the accuracy derived from the confusion matrix (Fawcett, 2006) as shown in Table S2 in Supporting Information. We looked for two types of optimal calibrations. The first type is a general calibration, for which we have presented the results in Sect. 3. This calibration combines all four stations in order to investigate the feasibility of a general signal conversion procedure applicable to multiple sites equipped with SPG systems. The second type is a site-specific calibration aiming to improve the accuracy of bedload transport rate estimates at a single monitoring station, to be used for a more detailed analysis of bedload-related processes at a given site (details of these site-specific calibrations are available in Supporting Information Sect. S4 and S5).

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469   The biases introduced by apparent packets can be removed by site-specific calibration of the coefficients $k_{b,i,j}$, so the
470 AF and AH methods perform about equally well when calibrated separately to each individual site (see Supporting
471 Information Sect. S4 and S5). This result supports the use of the AF method, considering the important number of packets
472 left out by the AF thresholds. However, the abundance of apparent packets varies considerably from site to site, owing to
473 differences in the channel geometry, the bedload grain-size distribution, and the construction details of the individual SPG
474 installations. Because the AF method filters out a substantial fraction of these apparent packets, it yields substantially better
475 general calibrations than the AH method does (see Table 5).

476   We also tested the performance of an adapted version of the AH method introduced by Rickenmann et al. (2018). This
477 method was originally developed for the Erlenbach site and aimed to correct for the relationship between the signal response
478 and the transport rate. In the present study, we applied this method to each field site. The only notable improvement
479 introduced by the adapted AH method is the increased number of detected samples at the Erlenbach station, leading to more
480 accurate estimates of the various characteristic grain sizes D_x at this site (Tables S8 and S9 in Supporting Information); the
481 results for the other sites were not substantially improved.

482   While the lack of accurate flow velocity measurements is certainly one of the critical points of the study, one could
483 argue that another lack is the low variability between the site-specific calibration relationships of the three natural sites
484 already before implementing the AF method (Fig. 8a). It would have been interesting to test the method on a larger number
485 (and variety) of sites. Unfortunately, these four chosen sites are the only ones at which a full geophone signal has been
486 recorded during calibration measurements.

4.2 Two-dimensional size class thresholds

488 To understand the performance of the new AF method it is worth taking a closer look at the role of the size class thresholds.
489 As shown in Fig. 7, replacing the upper amplitude thresholds with amplitude-frequency values results in the following two
490 important changes. First, a dimension is added, which facilitates focusing on the narrow range of signal responses
491 characteristic for real packets, and filtering out many of the apparent packets. Second, the areas of the amplitude-frequency
492 domain covered by two adjacent classes can now overlap. Packets located in overlapping areas are assigned once to each
493 class and therefore counted twice. This explains why both the number of detected packets $PACK_j$ (Fig. 7c and 7d) and
494 subsequently the $k_{b,j}$ values (Fig. 8) are slightly higher when the AF method (instead of the AH method) is applied to the
495 larger size classes. Counting such packets twice is not unreasonable, given that the ranges of signal responses recorded
496 during single-grain-size flume experiments for two contiguous grain-size classes significantly overlap, even after apparent
497 packets are filtered out (Fig. 5). Overlapping class boundaries therefore results in a less strict classification of the few
498 packets that are on the edges of the classes. In Fig. 7b, out of 2256 packets recorded by G2 (blue), 144 packets have been
499 counted twice. But interestingly, not a single of the 153 packets recorded by G1 (red) encompassed by the class boundaries
500 has been counted twice. A further result supports the use of the two-dimensional size class thresholds. When applying the
501 AF method, the $k_{b,j}$ coefficients obtained for the different sites (Fig. 8b) reach a maximum value at the third smallest size
502 class. A similar yet stronger decrease towards the two smallest classes was described by Wyss et al. (2016b) and was related
503 to the reduced detectability of the smallest particle sizes.

504   Through the reduced area covered by the new amplitude-frequency thresholds in Fig. 7b, a certain percentage of all the
505 packets recorded during the field calibration experiments is neglected for general calibration: 55% at the Albula site, 63% at
506 Navisence, 58% at Avançon de Nant and only 9% at Erlenbach. This suggests that the plates embedded at Erlenbach pick up
507 less noise from their surroundings. A similar trend was observed by Nicollier et al. (2022) when comparing the maximum
508 amplitude registered by two adjacent plates for a given impact at the same location. This difference in noise detection levels
509 is possibly accentuated by the number of impacted plates during bedload transport events. The SPG array embedded in the

artificial U-shaped channel of the Erlenbach has the particularity that only 2 out of its 12 plates are usually impacted by bedload particles during floods (and only sediment crossing these two plates is caught by the automatic basket sampler), while at the other stations all 10 to 30 embedded plates are submerged by the flow and thus can potentially be impacted.

4.3 Sampling uncertainties

Even though the AF method improved the overall accuracy of flux estimates for most classes (Table 5), some trends addressed in Sect. 3 suggest that factors other than the noise level also control the accuracy of the estimates. The dataset presented in this study includes 308 calibration measurements and is in our knowledge the largest dataset gathered for an impact plate system. Still, it appears that the number of collected samples is not sufficient to accurately assess the performance of the two methods for the three largest particle-size classes (Fig. 9; Table 5). This is mainly due to the fact that in typical sediment mixtures, large particles are rarer than fine particles (Rickenmann et al., 2014; Mao et al., 2016). Earlier investigations have shown that a larger number of detected bedload particles reduces the scatter of total mass estimates by averaging over stochastic factors such as the impact location on a given impact plate, the particle transport mode (sliding, rolling, saltating, etc.), and the impact velocity (Rickenmann and McArdell, 2008; Turowski et al., 2013). A further uncertainty arises because these larger particles are transported at higher bed shear stresses (Einstein, 1950; Wilcock and Crowe, 2003), which also mobilize more total material and thus pose a serious challenge regarding the sampling efficiency of the calibration bedload samplers. Bunte and Abt (2005) and Bunte et al. (2019) have demonstrated that reducing the sampling duration with a bedload trap from 60 to 2 minutes decreases both the sampled unit total bedload flux $q_{b,tot}$ and the sampled maximum particle size D_{max} by about half. In the present study, total bedload fluxes up to 4 kg m^{-1} s^{-1} were measured with the net sampler, meaning that the measurement duration had to be minimized to avoid overloading the sampler. At the Albula stream, for instance, only four samples contained particles of the largest class, and all four were sampled over a duration ranging from 1 to 2 minutes. As a comparison, the longest sampling duration was reached at the Navisence site and lasted 25 minutes. All this suggests that an optimal calibration of the SPG system requires balancing the sampling duration and the number of collected particles. Note that uncertainties in the direct measurements have a direct impact on the accuracy of fractional sediment flux and grain-size estimates. Flume experiments could potentially be used to assess the sampling efficiency of the various calibration sampling methods, along with the detection efficiency of the SPG system.

4.4 Transport rate

Two further trends are evident in the unit fractional flux estimates obtained for the seven smallest classes, for which most samples were detected ($N_{samples,est}$ / $N_{samples,meas}$ > 96%; Table 5). First, the relative scatter (on the log-log plots) of the fractional flux estimates around the power-law regression lines in Fig. 9 is smaller at higher transport rates. Second, both total and fractional fluxes are generally overestimated at low transport rates and underestimated at high transport rates (Fig. 9 and 10), which also correspond to the largest calibration samples. These findings agree with results from previous calibration campaigns with the SPG system (Rickenmann and Fritschi, 2017; Rickenmann et al., 2018) but a comprehensive explanation for these trends is still missing. The following hypotheses can be put forward to explain the relationship between the mass flux estimates and the transport rate q_b: (i) The SPG system may suffer from signal saturation when the transport rate is too high, as has been document in the Japanese pipe microphone system (Mizuyama et al., 2011; Choi, 2020). In our SPG data, we have observed long packets containing multiple large peaks corresponding to several impacts occurring so quickly after one another that they were not detected as separate packets. One can expect that the probability of occurrence of such packets increases together with the transport rate, with the transport of large particles (which typically generate packets of longer durations), and with the occurrence of sliding and rolling particles (Chen et al., 2022). The long packets take the place

of multiple shorter packets that would otherwise be individually counted; thus, they lead to underestimated mass fluxes for a given $k_{b,j}$ value. The development of a procedure to identify such packets and attribute the therein contained peaks to individual impacts could represent an interesting goal for future research. (ii) Field observations of bedload sheets being transported over plates at high transport rates were made at the Vallon de Nant site. In the presence of bedload sheets, one can expect that the detection rate of transported particles is hampered by multiple particle layers (Rickenmann et al. 1997; Turowski and Rickenmann, 2009), kinetic sieving (e.g. Frey and Church, 2011) or percolation processes (e.g. Recking et al., 2009). Given these hypotheses, it would be reasonable to expect a stronger signal response at lower transport rates (Fig. 10)

We are not able to give a clear explanation for the overestimates of the characteristic grain size D_x for finer grain mixtures and underestimates for coarser grain mixtures (as shown in Fig. 11). A similar trend was also observed by Rickenmann et al. (2018) for calibration measurements originating from the Erlenbach. We speculate that the decrease of the detection rate along with increasing transport intensity, as mentioned above, may partly explain this phenomenon.

4.5 Effect of the flow velocity

A recurrent feature in the results presented above is an offset between the estimates obtained for the Erlenbach and those obtained for the three other stations. A similar offset was observed earlier for linear calibration relations for total bedload mass between the Erlenbach and other field sites with more natural approach flow conditions (Rickenmann et al., 2014). Although applying the new amplitude-frequency method has reduced the offset in the present study significantly, it remains visible for both fractional and total bedload flux estimates (Fig. 9, 10, and 12). At the Erlenbach site, the last 35 meters upstream of the SPG system consist of an artificial bed with a steep channel slope of 16%, made of large flat embedded boulders (Roth et al., 2016). This explains the supercritical flow regime with a Froude number around 5.1 (Wyss et al., 2016c) and a flow velocity V_f around 5 m s^{-1} at the check dam with the geophone sensors (Table S1). Bedload particle velocity V_p was introduced by Wyss et al. (2016b, c) as a possible governing parameter affecting the number of particles detected by the SPG system, fast moving particles being less likely to collide against the Swiss plate geophone than slower moving ones, which are more frequently in contact with the bed. For the present study, we used V_f as a proxy for V_p, even though bedload particles generally travel more slowly than the fluid that surrounds them (Ancey et al., 2008; Chatanantavet et al., 2013; Auel et al., 2017). Past flume experiments (Wyss et al., 2016b; Kuhnle et al., 2017) have shown that the calibration coefficient $k_{b,j}$ can vary with the flow velocity V_f, such that a three-fold increase in V_f can lead to a two-fold decrease of $k_{b,j}$. The better detectability of particles that one could expect from the higher impact energy (Wyss et al. 2016b) seems to be insufficient to compensate the strong reduction of the number of impacts on a plate with increasing flow velocities. This possibly arises from the fact that larger flow velocities (without increased turbulence) may also lead to flatter saltation trajectories, thus decreasing the vertical component of the impact force. Furthermore, bed morphology, bed roughness and flow velocity play important roles in determining particle transport mode, i.e., sliding, rolling, or saltating (e.g. Bagnold, 1973; Lajeunesse et al., 2010). Although high flow velocities generally favor the saltating mode (Ancey et al., 2002; Chen et al., 2022), the shallow flow depths measured at the Erlenbach (in average 0.1 m; Wyss et al. 2016b) may limit the hop height of larger particles (Amir et al., 2017). Considering all these aspects, we hypothesize that the generally underestimated transport rates observed for the Erlenbach site mainly arise from the exceptionally high flow velocity and the related transport mode (Fig. 12). Continuous flow velocity measurements are lacking at the Albula and Navisence sites, hampering a more detailed analysis of their relationships between flow velocities and detection rates.
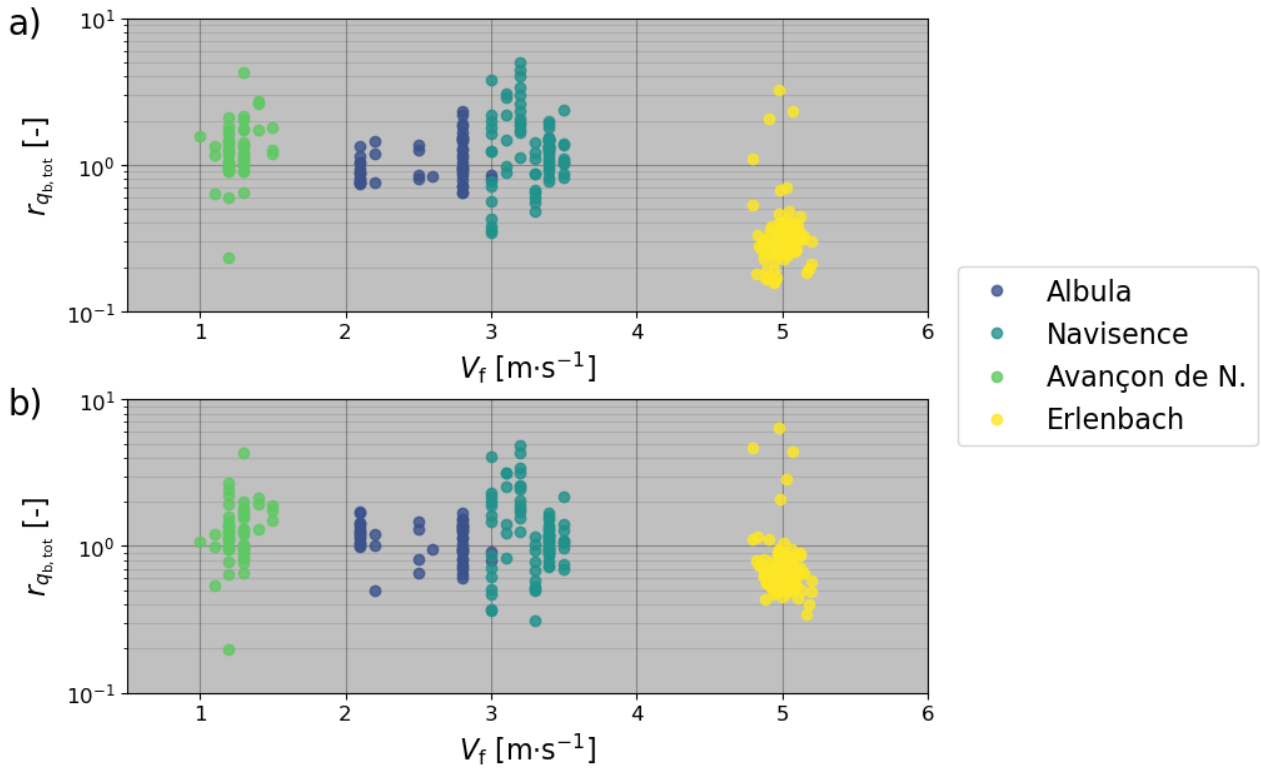
Figure 12: Ratio $r_{q_{b,tot}}$ between the estimated and the measured unit total mass flux as a function of the mean flow velocity V_f, for each collected sample and each station, for the AH method (a) and the AF method (b). The indicated flow velocity corresponds to in situ measurements made during (or close in time to) the corresponding calibration measurement. For better readability, a random scatter ranging from -0.2 m s⁻¹ to 0.2 m s⁻¹ was added to the stable flow velocity of 5 m s⁻¹ measured at the Erlenbach site.

4.6 K-fold cross-validation

In a last stage, we tested the robustness of the AH and AF methods by splitting the dataset into calibration and validation data. Given that the number of calibration measurements is relatively small and varies between stations, we applied a 4-fold cross-validation technique (e.g. Khosravi et al., 2020). The field calibration measurements were distributed over four folds, each containing an equal number of calibration measurements from each site (Supporting Information Fig. S4). One after another, the folds were used as validation datasets while the remaining three folds were used for calibration. General calibration coefficients $k_{b,j,gen}$ were obtained from the calibration dataset and subsequently applied to the validation data to derive flux estimates. Even though each fold contains a total of only 48 samples (12 per site), the results obtained with the 4-fold cross-validation procedure support our conclusion that including frequency information in the packet classification procedure improves the mean accuracy of the estimates over all sites, in particular for the smaller five to six size classes j (Supporting Information Table S10). Nicollier et al. (2022) found that most apparent packets are detected as belonging to smaller size classes than the particles that caused them, due to the attenuation of the vibrations as they propagate (see Fig. 7). It is therefore reasonable that the AF method mainly improves the flux estimates for these smaller classes.

5   Conclusion

The Swiss plate geophone (SPG) is a bedload surrogate monitoring system that has been installed in several gravel-bed streams and was calibrated using direct sampling techniques. While most site-specific calibration relationships for total mass flux are robust across multiple orders of magnitude, the mean calibration coefficients can still vary by about a factor of six between different sites. In this study, we derived a general procedure to convert SPG signals into fractional bedload fluxes

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609 using an extensive dataset comprising controlled flume experiments as well as 308 field calibration measurements from four

610 field sites. The proposed hybrid approach is based on previous findings (Antoniazza et al., 2020; Nicollier et al., 2022) that

611 the SPG system is biased by elastic waves that propagate through the apparatus and generate noise in the form of spurious

612 "apparent" packets. We introduced the amplitude-frequency (AF) method as an alternative to the amplitude-histogram (AH)

613 method developed by Wyss et al. (2016a). Packets recorded during single-grain-size flume experiments were first filtered to

614 exclude apparent packets, and then used to derive grain-size class thresholds for packet classification. We found that filtering

615 out apparent packets results in more consistent relationships between particle diameter and amplitude-frequency

616 characteristics of the SPG signal. Furthermore, we showed that including frequency information in size class thresholds

617 helps in excluding apparent packets and thus improves the signal-to-noise ratio. In a second stage, we applied these flume-

618 based thresholds to field calibration measurements and derived general calibration coefficients applicable at all four sites for

619 ten different grain-size fractions. The AH method, by contrast, requires site-specific calibration because it cannot account for

620 the site-to-site differences in the abundance of apparent packets. Averaged over the ten grain-size fractions, the bedload

621 masses of 69% and 96% of the samples were estimated within an offset of a factor of two and five, respectively, relative to

622 the measured sampled masses. The remaining discrepancies between the site-specific results are mainly attributed to large

623 differences in flow (and probably particle) velocity. Finally, the sampled mass, the transport rate and the sampling efficiency

624 were identified as further factors possibly influencing the accuracy of mass flux and grain-size estimates.

625 The presented results are highly encouraging regarding future applications of surrogate monitoring methods to

626 investigate bedload transport processes. The findings also underline the valuable contribution of flume experiments to our

627 understanding of the relationship between bedload transport and the recorded SPG signal. But above all, this study highlights

628 the requirements for obtaining calibrations that are transferable across sites: accurate and numerous direct sampling

629 measurements with long sampling durations and large sampled masses, sensors insulated from surrounding noise sources,

630 and highly resolved temporal information about the stream flow, to identify and account for variations in the transport

631 conditions.

632 **Notation**

633 a_c Linear coefficient of the criterion

634 A_{FFT} Fourier amplitude

635 $A_{m,j}$ Mean amplitude registered for particle-size class j

636 b_c Linear coefficient of the criterion

637 Δt_i Sampling duration

638 $D_{m,j}$ Mean particle diameter for particle-size class j

639 $D_{sieve,j}$ Lower sieve size retaining particle class j

640 D_x Characteristic grain size

641 $f_{centroid}$ Centroid frequency

642 i Sample index

643 j Particle-size class index

644 $k_{b,i,j}$ Sample- and class-specific calibration coefficient

645 $k_{b,j,med,station}$ Median calibration coefficient for particle-size class j and a given station

646 $k_{b,j,gen}$ General calibration coefficient for particle-size class j

647 $M_{est,i,j}$ Estimated fractional mass per sample and per class

648 $M_{meas,i,j}$ Sampled fractional mass per sample and per class

649 $MaxAmp_{env}$ Maximum registered amplitude within a packet

650	$N_{\text{samples,est}}$	Number of detected samples
651	$N_{stations}$	Number of stations
652	$PACK_{i,j}$	Number of recorded packets per sample and per class
653	$p_{\text{factor\_x}}$	Percentage of all detected samples for which the estimated and the measured values differ from each
654		other by less than a factor of x
655	$q_{\text{b,est},i,j}$	Estimated unit fractional transport rate per sample and per class
656	$q_{\text{b,meas},i,j}$	Measured unit fractional transport rate per sample and per class
657	$q_{\text{b,tot,est},i}$	Estimated unit total bedload flux per sample
658	$q_{\text{b,tot,meas},i}$	Measured unit total bedload flux per sample
659	R^2	Coefficient of determination
660	r	Correlation coefficient
661	r_x	Ratio between estimated and measured values x
662	$th_{\text{ah},j}$	Amplitude-histogram thresholds
663	$th_{\text{af,low},j}$	Lower amplitude-frequency thresholds
664	$th_{\text{af,up},j}$	Upper amplitude-frequency thresholds
665	V_{f}	Mean flow velocity
666	w_{p}	Standard width of an impact plate

667 **Data availability**

668 The dataset presented in this paper is available online on the EnviDat repository

669 https://www.envidat.ch/#/metadata/sediment-transport-observations-in-swiss-mountain-streams.

670 **Author contribution**

671 Tobias Nicollier designed and carried out the field and flume experiments, developed the presented workflow and prepared

672 the manuscript with contributions from all co-authors. Gilles Antoniazza designed and carried out the field experiments at

673 the Vallon de Nant site. Lorenz Ammann helped developing the methodology and contributed to the formal analysis. Dieter

674 Rickenmann contributed to the conceptualization and the supervision of the presented work, contributed to the design of the

675 methodology, and provided support during the field and flume experiments. James W. Kirchner contributed to the

676 development of the methodology and significantly contributed to the preparation of the initial draft.

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